## B Mathematical Society of Japan

## **2014 ANNUAL MEETING**

# **Titles and Short Summaries of the Talks**

March, 2014

at Gakushuin University

## $2014 \ \text{Mathematical Society of Japan}$

# ANNUAL MEETING

Dates: March 15th (Sat)–18th (Tue), 2014 Venue: Gakushuin University

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	Algebra	Functional Analysis	Found. of Math. and History of Math.	Topology	Functional Equations	Statistics and Probability	Geometry	Complex Analysis	Applied Mathematics				
15th	9:00-12:00 14:15-16:30	9:30-11:50	9:30–11:30 14:15–17:00	10:00-12:00 14:15-16:30	9:00-12:00 14:15-16:30	9:30-12:00	9:20-12:00 14:30-15:25	9:30–11:45 14:15–15:45	9:30-11:50 14:30-16:40				
(Sat)		Featured Invited Talks 13:00–14:00											
	Invited Talk	Invited Talk		Invited Talk	Invited Talk	Invited Talks	Invited Talk	Invited Talk	Invited Talk				
	16:45-17:45	14:15-15:15		17:00-18:00	16:45-17:45	$\begin{array}{c} 14{:}30{-}15{:}30\\ 15{:}45{-}16{:}45\end{array}$	15:40-16:40	16:00-17:00	16:50-17:50				
	Algebra	Functional Analysis	Found. of Math. and History of Math.	Topology	Functional Equations	Statistics and Probability	Geometry	Complex Analysis	Applied Mathematics				
	9:00-12:00	10:00-11:50	9:30-11:40	9:30-11:45	9:00-12:00	9:00–11:25 9:40–11:50		9:30-10:45	9:30-11:30 13:00-14:30				
16th	Invited Talk	Invited Talk	Invited Talk	Invited Talk	Invited Talk		Invited Talk	Invited Talk					
(Sun)	13:15-14:15	13:15-14:15	13:10-14:10	13:30-14:30	13:15-14:15		13:00-14:00	11:00-12:00					
	MSJ Prizes Presentation (Conference Room I) · · · · · · · · · · · · · · · · · ·												
	Plenary Talks (Conference Room I) MSJ Spring Prize Winner												
	Noriko Mizoguchi (Tokyo Gakugei Univ.)(16:45-17:45)Official Party(Mejiro Club)(18:00-20:00)												
	Algebra	Functional Analysis	Real Analysis	Topology	Functional Equations	Statistics and Probability	Geometry	Infinite Analysis	Applied Mathematics				
17th	9:30-12:00 14:15-15:00	9:30-12:00 14:15-15:00	9:00-12:05 14:15-16:25	$\substack{10:00-12:00\\14:15-15:15}$	9:00-12:00 14:15-16:15	9:00-12:00	10:00-11:50	$\begin{array}{c} 10:00{-}11:30\\ 14:15{-}15:00 \end{array}$	9:00-12:00 14:30-16:30				
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18th	Algebra	Functional Analysis	Real Analysis		Functional Equations			Infinite Analysis	Applied Mathematics				
	9:00-12:00 14:15-16:45	10:00–11:40 14:15–15:15	9:00–12:20 14:15–15:55		9:00–12:00 14:15–15:15			10:00-11:30	$\begin{array}{c} 10:00{-}11:30\\ 14:15{-}15:45\end{array}$				
(Tue)				Featured Invit	ed Talks	13:00-14:00	)						
			Invited Talk		Invited Talk			Invited Talk	Invited Talk				
			16:15-17:15		15:30-16:30			14:15-15:15	16:00-17:00				

## Contents

Plenary Talks	1
Featured Invited Talks	1
Foundation of Mathematics and History of Mathematics	4
March 15th (Sat)	4
March 16th (Sun)	7
Algebra	9
March 15th (Sat)	9
March 16th (Sun)	13
March 17th (Mon)	15
March 18th (Tue)	18
Geometry	<b>24</b>
March 15th (Sat)	24
March 16th (Sun)	27
March 17th (Mon)	28
Complex Analysis	<b>31</b>
March 15th (Sat)	31
March 16th (Sun)	34
Functional Equations	36
March 15th (Sat)	36
March 16th (Sun)	41
March 17th (Mon)	43
March 18th (Tue)	48
Real Analysis	53
March 17th (Mon)	53
March 18th (Tue)	56

Functional Analysis	61
March 15th (Sat)	61
March 16th (Sun)	63
March 17th (Mon)	64
March 18th (Tue)	67
Statistics and Probability	69
March 15th (Sat)	69
March 16th (Sun)	71
March 17th (Mon)	74
Applied Mathematics	78
March 15th (Sat)	78
March 16th (Sun)	82
March 17th (Mon)	84
March 18th (Tue)	89
Topology	92
March 15th (Sat)	92
March 16th (Sun)	96
March 17th (Mon)	98
Infinite Analysis	101
March 17th (Mon)	101
March 18th (Tue)	103

## **Plenary Talks**

#### March 16th (Sun) Conference Room I

MSJ Spring Prize Winner		(15:30-16:30)
Noriko Mizoguchi	Blow-up in nonlinear parabolic equations	(16:45-17:45)
(Tokyo Gakugei Univ.)		

Summary: The blow-up of solutions has been one of the subjects most actively studied in nonlinear parabolic equations and systems for several decades. Various factors affect the determination of whether a solution blows up in finite time or exists globally in time. One needs to investigate the mathematical structures behind phenomena. It is very useful in the process to make use of methods in other fields in addition to analysis. I will give a talk about my recent results on the blow-up of solutions to nonlinear parabolic equations and systems.

## **Featured Invited Talks**

## March 15th (Sat)

#### **Conference Room I**

Summary: A spectacular development is going on in the theory of the distribution of primes. Luckily enough, I am witnessing the event as a contemporary specialist. The purpose of my talk is to share this excitement of mine with my audience. Any mathematical discovery is an eventual outcome of rich and long history of our cherished discipline, and the recent amazing discoveries by D. A. Goldsto–J. Pintz–C. Y. Yildirim, Y. Zhang, J. Maynard, and T. Tao are typical instances. I shall quickly overview the relevant history of the distribution of primes, especially that of sieve methods. You will find all basic ideas are so simple that you will certainly be persuaded that the proverb "small things stir up great" is indeed a truth.

## Conference Room V

Akimichi Takemura (Univ. of Tokyo)	On recent developments of computational algebraic statistics	
		(13:00-14:00)

Summary: We discuss some recent developments of computational algebraic statistics. In particular we explain holonomic gradient method, which was recently introduced by the members of the JST CREST Hibi project team, and show how the method leads to fundamental reformulation of classical distribution theory of statistics.

#### 2 Featured Invited Talks

#### Conference Room VII

Summary: The purpose of this talk is to discuss special domains in several complex variables. Special domains in  $\mathbb{C}^n$  are those domains which are called Reinhardt domains, tube domains, circular domains, Hartogs domains, and so on. These domains may be characterized as domains whose holomorphic automorphism groups contain canonical continuous subgroups. For example, a Reinhardt domain in  $\mathbb{C}^n$  admits an *n*dimensional compact torus action, while a tube domain in  $\mathbb{C}^n$  admits an *n*-dimensional real vector group action. In this talk, we mainly take up Reinhardt domains and tube domains, and explain about their different aspects as well as the complementary relations between them.

### March 17th (Mon)

#### Conference Room V

Summary: Elliptic curve cryptography was proposed independently by Koblitz and Miller around 1986. Since then, it has evolved into a powerful tool for new applications. In the early stage, it provided a more compact realization of public key cryptography than RSA. The need for its security evaluation and appropriate parameter generation has opened a fruitful research area in algorithmic number theory. Around 2000, a pairing operation on an elliptic curve began to be used for new cryptographic functionalities like ID-based encryption, attribute-based encryption, etc. This new trend further enriched the elliptic curve algorithm research. Very recently, isogenies between elliptic curves were incorporated in a quantum-resistant public key cryptosystem. In this talk, I will survey the evolution of elliptic curve cryptography in terms of three central one-way functions, i.e., scalar multiplication, pairing operation, and isogeny sequence computation.

#### Conference Room VII

Takashi Shioya (Tohoku Univ.) Concentration, convergence, and dissipation of spaces ..... (13:00–14:00)

Summary: For a given sequence of compact Riemannian manifolds (or more generally metric measure spaces), we consider the following three situations.

(1) The sequence converges to a one-point space.

(2) The sequence dissipates, i.e., the manifolds in the sequence are decomposed into small pieces and all such pieces are going to be far apart each other.

(3) The sequence converges to some nontrivial space.

We are mainly interested in the case where the dimension is divergent to infinity. For example, for the sequence of the *n*-spheres in a Euclidean space, parametrized by the dimension n = 1, 2, ..., we observe (1) if the radius is smaller than the order of  $\sqrt{n}$ . We observe (3) if the radius is larger than the order of  $\sqrt{n}$ . If the radius has order of  $\sqrt{n}$ , then we observe (3) and the limit is an infinite-dimensional Hilbert space with a Gaussian measure in some sense. This is similar to the phase transition phenomenon in the statistical mechanics. In this talk, we explain Gromov's theory of metric measure geometry and discuss such phase transition phenomenon.

#### March 18th (Tue)

### Conference Room V

Yoshitsugu Takei (Kyoto Univ.)

Summary: Algebraic analysis of singular perturbation theory deals with singularly perturbed differential equations and their solutions obtained in a perturbative way. A typical example is a one-dimensional Schrödinger equation and its WKB solution. As is well-known, a WKB solution is a divergent solution. Such a divergent solution is traditionally handled by using Poincare's theory of asymptotic expansions, but the treatment of exponentially small terms (e.g., Stokes phenomena) then becomes a very subtle problem. In our approach exponentially small terms can be treated in a neat and exact manner through the Borel resummation method. Roughly speaking, exponentially small terms are controlled by a graph called "a Stokes graph".

In this talk, mainly using some concrete examples, we explain an outline of the exact WKB analysis, that is, the analysis of WKB solutions of a one-dimensional Schrödinger equation. We also discuss its generalization to higher order equations. If time permits, some recent advances and future problems will be referred as well.

#### Conference Room VII

Summary: Let f(t) be a real continuous function defined on an open interval I of the real axis. Then f(X) is well-defined for any bounded selfadjoint operator (or Hermitian matrix) X whose spectrum is in I. f is called an operator monotone function and denoted by  $f \in \mathbf{P}(I)$  if the mapping  $X \mapsto f(X)$  preserves operator order.  $t^{\lambda} \in \mathbf{P}(0, \infty)$  for  $0 < \lambda \leq 1$ , but  $t^{\lambda} \notin \mathbf{P}(0, \infty)$  for  $\lambda > 1$ . The Löwner (Loewner) theorem is fundamental on the study of this area:

 $f \in \mathbf{P}(I)$  if and only if f has a holomorphic extension to the upper half plane  $\Pi_+$  of **C** which is a Pick function.

g(t) is said to majorize h(t) if  $h \circ g^{-1}$  is operator monotone. This was named after the classical majorization between two sets of real numbers. We first establish Product Theorem and then extend the Furuta inequality. We last refer to the principal inverses of polynomials and one of the gamma function.

## Foundation of Mathematics and History of Mathematics

March 15th (Sat)

Conference Room III

## 9:30 - 11:30

1 Shigeru Masuda (Kyoto Univ.) The Sturm–Liouville type problem in the modeling of the Schrödinger

Summary: We discuss the modeling of the Schrödinger equations or the quantum equations. The classical mechanics of model, which they put in, are: the wave motion from Huygens' principle of wave, atomic motion from Kepler's law and Kepler motion, eigenvalue problems from the perturbation problem on Kepler motion, collision and transport between electron and nucleus, and entropy and probability from the gas theories like Maxwell and Boltzmann, etc. We document especially that the Sturm–Liouville type problems in the modeling of the Schrödinger equations, for which Schrödinger 1926 refers to, and these Sturm–Liouville's works 1836–37 on the boundary value problems of heat diffusion are based on the same sort of boundary value problems in the Poisson's mathematical theory of heat 1835.

Summary: After Lagrange expressed the theory of propagation of sound 1759–61 by the trigonometric series, Fourier 1822 proposes the analytical theory of heat, including the trigonometric series without proving the convergence. Since then, many mathematicians, like Poisson 1823, Cauchy 1823, et al. try the proof problem on the describability of trigonometric series until the success by Carlson 1966 of  $L^2$  and by Hunt 1968 of  $L^p$ . At first, Dirichlet 1837 introduces especially Cauchy 1823 as the only challenging one, however, falls himself into a circular argument. Liouville 1836 introduces Poisson 1823 as the first study of this sort. Kummer 1860, in the mourning paper of Dirichlet, evaluates Dirichlet's work 1837 on this problem. We focus on the earlier triers, such as Lagrange, Fourier, Poisson, Cauchy, Dirichlet, Liouville, et al., of proving trials on the describability of trigonometric series.

Summary: In early 20th century, Schwarzschild and Epstein applied the Hamilton–Jacobi theory to their examinations of the Stark effects. In this process they introduced new mathematical ideas: action-angle variables, an idea of degeneracy and so on. Their work illustrates that the Hamilton–Jacobi theory was not prepared for the quantum theory in the 19th century but was developed to be applicable to the quantum theory.

4 Hideyuki Majima (Ochanomizu Univ.)<sup>♭</sup> On the problem in the appendix of the "Tetsujutsu-Sankei (Mathematical Treatise on the Technique of Linkage)" · · · · · · · · · · · · · · · · · · 30

Summary: In the appendix of the "Tetsujutsu-Sankei (Mathematical Treatise on the Technique of Linkage)", Nakane solves the following problem: to find the sides of a triangle that shall have the values n, n+1 and n+2, and such that the perpendicular upon the longest side from the opposite vertex shall be rational. Citing his solution in the book "A History of Japanese mathematics", Mikami and Smith assert that "Whether or not he made the induction complete does not, however, appear." We discuss on the induction employed by Seki, Takebe and Nakane.

#### 5 Foundation of Mathematics and History of Mathematics

Summary: Example: rational function  $f(z) = (6z^2 - 2z + 1)/(z+1)(2z-1)^2 = 1/(z+1) + 1/(2z-1) + 1/(2z-1)^2$ . In  $\{1/2 < |z| < 1\}$ , by the definition we have Laurent expansion:  $\Sigma_0 : n \to \infty$  $f(z) = \Sigma_0\{(-1)^n z^n\} + \Sigma_0(1/2^{n+1})(1/z^{n+1}) + \Sigma_0\{(n+1)/2^{n+2}\}(1/z^{n+2}), (A)$ by Wada's theorems, power series:  $\Sigma_1 : k = 1 \to \infty$ 

#### 14:15-17:00

6 Takahiro Seki (Niigata Univ.) A Gentzen-style formulation for non-associative substructural logics II

Summary: Associativity (of fusion) is regarded as one of the important structural rules. Recently, some studies on non-associative substructural logics have been developed. In this talk, we consider a Gentzenstyle formulation for some non-associative substructural logics including distributive substructural logics and prove the cut elimination theorem by a proof-theoretic method.

Summary: In 2010, we list all the exact S4-models for  $\mathbf{F}(n)$  in S4, where  $\mathbf{F}(n)$  is the set of modal formulas with finite propositional variables  $p_1, \dots, p_m$  and with finite modal degree  $\leq n$ . However, considering the case that n = 0, we can easily observe that an exact model for  $\mathbf{F}(0)$  in S4 does not have to be reflexive (i. e. S4-model). For example if m = 1,  $W = \{\alpha, \beta\}, R = \emptyset$ , and  $P(p_1) = \{\alpha\}$ , then  $M = \langle W, R, P \rangle$  is an exact model for  $\mathbf{F}(0)$  in S4, but it is not S4-model. Here, we give a method to list all the exact K4-models for  $\mathbf{F}(n)$  in S4.

8 <u>Ken-etsu Fujita</u> (Gunma Univ.) Intermediate lambda-terms between Church and Curry ..... 15 Aleksy Schubert (Univ. of Warsaw)

Summary: It is well known that the type-checking and type-inference problems are undecidable for 2nd-order lambda-calculus in the Curry style, although those for the Church style are decidable. We introduce three intermediate structures between the Church and Curry styles, and show that one intermediate structure called a style of hole application becomes decidable for the type-related problems. We extend this idea to the omega-order calculus F-omega, and then prove that the type-related problems become undecidable at third order. It turns out that the decidable result on the problems is to be tight at order 2.

9 Taishi Kurahashi (Kobe Univ.) On Henkin sentences based on Rosser provability predicates ..... 15

Summary: We investigate Henkin sentences based on Rosser provability predicates, that is, sentences asserting their own provability in the sense of Rosser. We give a necessary and sufficient condition that a sentence is a Rosser-type Henkin sentence, and prove that any Rosser sentence can be a Rosser-type Henkin sentence. Also we prove the existence of a Rosser provability predicate whose Henkin sentences are all provable or refutable.

- 6 Foundation of Mathematics and History of Mathematics
- 10 Satoru Kuroda On minimal three-sort theories for PSPACE and EXPTIME · · · · · · 20 (Gunma Pref. Women's Univ.)

Summary: We construct three-sort theories of bounded arithmetic which captures PSPACE and EXPTIME. Our theories are minimal in the sense that they are contained in other theories capturing the corresponding classes. The idea for constructing such theories is succinctly represented versions of combinatorial problems.

11 Keita Yokoyama (JAIST) Finite iterations of infinite and finite Ramsey's theorem ...... 20

Summary: In this talk, we study a slightly strengthened version of infinite Ramsey's theorem, which has a better correspondence to the Paris–Harrington principle and its finite iteration.

12 <u>Takayuki Kihara</u> (JAIST) Algorithmic randomness and null-additivity ...... 15 Kenshi Miyabe (Univ. of Tokyo)

Summary: We say that a set A of natural numbers preserves  $\mathcal{R}$ -randomness if for every  $\mathcal{R}$ -random set  $B \subseteq \mathbb{N}$ , the symmetric difference  $A \triangle B$  of A and B is again  $\mathcal{R}$ -random, where  $\mathcal{R}$  is an arbitrary randomness notion. By using characterizations of null-additivity in the set theory of the real line, we determine the condition fulfilling  $\mathcal{R}$ -randomness preservation for several randomness notions  $\mathcal{R}$ .

13 Kenshi Miyabe (Univ. of Tokyo/JSPS) Characterization of being a Lebesgue point for integral tests ..... 20

Summary: The effectivization of almost-everywhere-type theorems usually give randomness notions. Some randomness notions have been characterized via differentiability, via the Lebesgue density theorem and via the Lebesgue differentiation theorem. In this talk, I will give some recent development on this topic. In particular, a new randomness notion of density randomness is characterized via the differentiation theorem for integral tests. Furthermore, I will discuss why the definition of density randomness requires ML-randomness explicitly.

14 Akitoshi Kawamura (Univ. of Tokyo) Distance trisector curves via the contraction mapping theorem · · · · · · 15

Summary: The (distance) trisector between two points p and q in the Euclidean plane is the pair of curves A and B such that A is the set of points equidistant from p and B, and B is the set of points equidistant from q and A. Such a pair of curves exists, is unique, and can be computed in polynomial time in a certain sense, as was shown by Asano, Tokuyama and Matoušek in 2006. A somewhat simpler and more general existence and uniqueness proofs based on the Tarski fixed point theorem were given later by Imai et al. and Kawamura, Tokuyama and Matoušek. We give yet another, short proof of these facts (in the original special setting) by showing that the trisector is the fixed point of a contraction mapping in a certain metric space.

## March 16th (Sun) Conference Room III

#### 9:30 - 11:40

15 Takashi Oyabu

Summary: 1. Algebraic function and Riemann surface:

2. O(n) = G::homotopy equivalent ==> O(n) = G: isomorphic: homeomorphic:

3.  $C^{\infty}(G) = \bigoplus \Sigma Hi$ :  $L2(G) = \bigoplus \Sigma Vi$ : representation of Diff(M):::Aut(R):

- 4. Differential equations in thermodynamics and mathematics:
- 5. General H: -theorems: introduction of entropy in mathematics:
- 6.  $J: X(1) = > S \cup C\{\infty\} = = > C = = > C/L = E: K(V) \sum_{0} (N) = K(V):$
- 7.  $C^{\infty}(M) = C^{\infty}(M')$ : homotopy equivalent =>  $C^{\infty}(M) = C^{\infty}(M')$ ::linearly equivalent:
- 8. G: compact real Lie group: G == G': homotopy equivalent => G == G': isomorphic:: homeomorphic::
- 9. Entropy: *H*-theorem:::and of parabolic type:
- 10. Inconsistency of the axioms of group and algebras: some considerations:

11. O(n) = G: homotopy equivalent ====> O(n)G::isomorphic: homeomorphic:

12. G == G': compact::real Lie groups: homotopy equivalent ===> G == G': isomorphic::homeomorphic.

13.  $J: X(1) = S = C \cup \{\infty\} = C = C/L = E: K(V) \sum_{0} (N) = K(V)$ 

- 14. Entropy in mathematics is introduced: and *H*-theorems: of parabolic type: dH/dt = < 0 = = > 0:
- 15. Differential equations in thermodynamics and mathematics:
- 16. Entropy in mathematics is introduced.::H-theorems: of parabolic type: dH/dt = <0 = = = >0:
- 17. Differential equations in thermodynamics and mathematics:
- 18. Entropy in mathematics is introduced.::H-theorems: of parabolic type: dH/dt = <0 = = >0:

Summary: In 1988, Hrushovski constructed new strongly minimal generic structure to give a counterexample to the Zilber conjecture. In his paper, Hrushovski pointed out that the theory of his structure is nearly model complete. In this talk, we give a characterization of model completeness in generic structures. Using the characterization, we want to consider model completeness of Hrushovski's strongly minimal structure.

Summary: We consider hyper-graphs with 3-hyper-edges. Let A be such a hyper-graph. Let  $\delta(A) = |A| - e(A)$ where e(A) is the number of hyper-edges in A. Suppose A is a hyper-subgraph of C. If  $A \subsetneq X \subset C$  implies  $\delta(A) < \delta(X)$ , then we write A < C. Let  $f(x) = \log_3(x+1)$ . Let  $K_f = \{A \mid B \subset A \Rightarrow \delta(B) \ge f(|B|)\}$ . Then the theory of the generic structure of  $(K_f, <)$  is model complete. More generally, if f is a concave function almost satisfying  $f^{-1}(x+1) \ge 3f^{-1}(x)$  with certain conditions then we get the same result.

#### 8 Foundation of Mathematics and History of Mathematics

Summary: According to the Kochen–Specker theorem some statements on a quantum system are not speakable in the sense that they cannot be assigned truth values. In order to solve a fundamental problem as to what are speakable about quantum reality, here, it is proved that there exists a unique subuniverse of the Takeuti universe of quantum set theory such that it satisfies every theorem of ZFC set theory in a given state, it contains a given observable, and that it is invariant under all automorphisms that preserve the given state and the given observable. It is also proved that the real numbers in this maximal subuniverse coincides with the maximal beable subalgebra previously determined by Halvorson and Clifton.

Summary: It is proved that if it is consistent that there exists a supercompact cardinal, then it is consistent that there are no S-spaces, the P-ideal dichotomy holds, and the pseudo-intersection number is equal to  $\aleph_1$ . This answers the question due to Stevo Todorčević.

20 Sakaé Fuchino (Kobe Univ.) Rado's conjecture and reflection principles compatible with MM · · · · · 40

Summary: We propose a new reflection principle, a variant of strong Chang's Conjecture, which is strong enough to deduce all known common consequences of Rado's Conjecture and MA<sup>+</sup>( $\sigma$ -closed) including FRP and SSR.

#### 13:10–14:10 Talk invited by Section on Foundation and History of Mathematics

Yasushi Hirata (Kanagawa Univ.) Comparing some topological properties of ordinals, LOTS', motonically normal spaces, and their products

Summary: It is well-known that every GO-space (=genralized ordered space) and every metrizable space are orthocompact and monotonically normal. And subspaces of ordinals are typical examples of GO-spaces. In this talk, we compare topological properties among subspaces of ordinals, GO-spaces, and monotonically normal spaces and their products. For instance, Kemoto and Smith proved that  $A \times B$  is countably metacompact for every subspaces A and B of ordinals. On the other hand, I and Kemoto found an example of a LOTS (=linearly ordered space)  $L_{\kappa}$  for each regular uncountable cardinal  $\kappa$  such that  $\kappa \times L_{\kappa}$  is not countably metacompact. For a monotonically normal space X and a subspace B of an ordinal, I, Kemoto and Yajima characterized orthocompactness of  $X \times B$  and normality with rectangularity of  $X \times B$  by observing neighborhood properties of spaces and closed sets which are homeomorphic to stationary sets. We will talk about these results.

March 15th (Sat) Con

Conference Room I

## 9:00-12:00

Summary: Yujiro Kawamata already showed at around 1992 that there exist semi-stable minimal models of three-folds over positive and mixed characteristic in terms of characteristic-free arguments by Shuichiro Tsunoda and Masayoshi Miyanishi around 1980's. Recently János Kollár et al showed that the contractibility of dual complexes, including similar result of Thuillier by using Berkovich spaces. In this talks, the author will consider a projectivity criterion for certain three-dimensional Shimura varieties of semi-stable singularities in the sense of J. Kollár and Shigefumi Mori, based on the quotient space by groupoids in the sense of S. Keel and S. Mori, with regards to these previous works.

Summary: The set of all the cyclic homogeneous polynomial inequalities of real three variables of degree d form a closed convex cone. We observe the structure of such cones for d = 3, 4, 5 and 6. Especially, we determine the algebraic structure of the boundaries of such cones. As corollary, we present some conditions to determine whether given inequality holds or not.

Summary: We consider dynamical systems over finite fields. Structure of maximal ideals of a crossed product A is discussed. Hasse zeta function of the category of A-modules is discussed.

Summary: On the Fermat quintic Calabi–Yau threefold and the theory of stability conditions due to Bridgeland and Douglas, we affirmatively answer physically motivated mathematical aims due to Hosono, Kontsevich, Thomas–Yau, and Walcher. Our method is based on homological mirror symmetry and stability conditions of Bridgeland type, which we introduce with their spaces. As a consequence, we obtain a quasimodular form attached to periods of the mirror family of the quintic by motivic Donaldson–Thomas invariants. The original motivation to attach quasimodular forms to these periods goes back to Dijkgraaf.

6 Makoto Sakurai Chiral algebras and algebraization of Higgs bundles' stability ..... 15

Summary: Several notions of stability conditions including the Deligne–Mumford compactification of smooth projective curves are being discussed in different contexts. In this talk, I will report my algebraic framework that will incorporate the BPS stability condition of Hitchin's stable Higgs bundles in addition to the chiral scalar fields of quantum field theory inspired by the Higgs mechanism of theoretical physicists and its algebraic geometry. I will especially try to build a "quasi-projective" algebraic geometry which includes, but is not limited to, the parabolic geometry of the well-known parabolic geometry. The examples include the blowups of the complex projective plane, which seem to be the underlying geometry of recent developments by theoretical particle physicists.

- 8 Osamu Matsuda Classification of curves on irrational ruled surfaces by mixed plurigenera (Tsuyama Nat. Coll. of Tech.) 15

Summary: Let S be a non-singular irrational surface with positive irregularity q and D an non-singular curve on S. If any exceptional curve E (of first kind) on S satisfies  $E \cdot D \ge 2$  ( $E \ne D$ ), then a pair (S, D) is said to be relative minimal. Suppose that  $m \ge a \ge 1$ . Then  $P_{m,a}[D] = \dim|mK + aD| + 1$  are called mixed plurigenera, where K indicates a canonical divisor on S. We shall give a classification of relative minimal pairs (S, D) by  $P_{m,a}[D]$ .

on X is called Arithmetically Cohen-Macaulay (ACM for short) if the cohomology groups  $H^i(X, \mathcal{E}(l))$  for  $1 \leq i \leq \dim(X) - 1$  and  $l \in \mathbb{Z}$  vanish, where  $\mathcal{E}(l) := \mathcal{E} \otimes \mathcal{O}_X(l)$ . In this talk, we give a complete classification of initialized and ACM line bundles on a smooth quartic hyper surface on  $\mathbb{P}^3$ .

 10
 Shigeru Mukai (Kyoto Univ.)
 The automorphism groups of Enriques surfaces covered by symmetric

 <u>Hisanori Ohashi</u> (Tokyo Univ. of Sci.)
 quartic surfaces
 15

Summary: We compute the full automorphism group of the Enriques surface S covered by some explicitly defined symmetric quartic K3 surface X. We give both the presentation and the realization of Aut(S). At the same time, we classify curves of genus 0 and 1 on S up to automorphisms.

11 Kazuki Utsumi (Hiroshima Univ.) Jacobian fibrations on the singular K3 surface of discriminant  $3 \cdots 10$ Summary: We give the Weierstrass equations and the generators of Mordell–Weil groups for Jacobian fibrations on the singular K3 surface of discriminant 3.

12 Katsuhisa Furukawa (Waseda Univ.) On general fibers of Gauss maps in arbitrary characteristic · · · · · · 15

Summary: We investigate general fibers of the Gauss map  $\gamma$  of a projective variety X in  $\mathbb{P}^N$ , in terms of the degeneracy map  $\kappa$  from X to a Grassmann variety. As a result of our previous work, if  $\gamma$  is separable, then a general fiber of  $\gamma$  coincides with the linear subvariety  $\kappa(x)$  of  $\mathbb{P}^N$  for general x in the fiber. In this talk, we explain: (1) Equivalence of the separability of the two maps  $\gamma$  and  $\kappa$ . (2)  $\kappa(x)$  is constant on  $x \in F$  for each irreducible component F of a general fiber of  $\gamma$ ; in particular, F is contained in this constant linear subvariety even if  $\gamma$  is inseparable. (3) The inseparability of Gauss maps of strange varieties.

### 14:15-16:30

13 Kiwamu Watanabe (Saitama Univ.)\* Characterization of the complete flag manifold of type  $F_4 \cdots 15$ 

Summary: Let X be a Fano manifold whose elementary contractions are smooth  $\mathbb{P}^1$ -fibrations, which is not a product. In the previous meeting of MSJ, I explained how to construct a simple Lie group associated to X, and X is homogeneous, provided that G is not of type  $F_4$ . In my talk, under the additional assumption that the tangent bundle of X is nef, I shall show that the same holds for the case of type  $F_4$ . Furthermore, I will explain the relation between the result and the Campana–Peternell Conjecture on Fano manifolds with nef tangent bundles. This is a joint work with G. Occhetta, L. E. Solá Conde and J. Wiśniewski.

14 Tadashi Takahashi (Konan Univ.) On the application of elimination ideal V ..... 10

Summary: We consider the normal forms and the restrictions of singular plane quartic curves in the two dimensional complex projective space. Then we can get the restrictions by using the Groebner basis of the elimination ideal, we show the restrictions of singular plane quartics.

 15 Yusuke Nakajima (Nagoya Univ.)
 Dual F-signature of Cohen-Macaulay modules over rational double points

 15 Yusuke Nakajima (Nagoya Univ.)
 Dual F-signature of Cohen-Macaulay modules over rational double points

Summary: The notion of F-signature is defined by Huneke and Leuschke. It is known that the F-signature characterizes some singularities. This notion is extended to finitely generated modules and called dual F-signature. In this talk, we determine the dual F-signature of Cohen–Macaulay modules over two-dimensional rational double points.

16	Shiro Goto	(Meiji Univ.)	Huneke–Wiegand conjecture and change of rings 15
	Ryo Takahashi	(Nagoya Univ.)	
	Naoki Taniguch	i (Meiji Univ.)	
	Hoang Le Truor	ng (IMVAST)	

Summary: Let R be a Cohen-Macaulay local ring of dimension one with a canonical module  $K_R$ . Let I be a faithful ideal of R. We explore the problem of when  $I \otimes_R I^{\vee}$  is torsionfree, where  $I^{\vee} = \operatorname{Hom}_R(I, K_R)$ . We prove that if R has multiplicity at most 6, then I is isomorphic to R or  $K_R$  as an R-module, once  $I \otimes_R I^{\vee}$  is torsionfree. This result is applied to monomial ideals of numerical semigroup rings. A higher dimensional assertion is also discussed.

17 Shiro Goto (Meiji Univ.)\* The first Euler characteristics versus the homological degrees · · · · · · 15 Kazuho Ozeki (Yamaguchi Univ.)

Summary: The notion of homological degree was introduced by W. V. Vasconcelos and his students in 1998, and since then, many authors have been engaged in the development of the theory. Recently, Ghezzi, Hong, Phuong, Vasconcelos, and the authors also make use of homological degrees to obtain bounds for the Hilbert coefficients of parameters. The purpose of this talk is to study the relationship between the first Euler characteristics and the homological degrees of modules.

 

 18
 Shiro Goto
 (Meiji Univ.)\*
 Relation between the first Hilbert coefficients and the homological tor-Kazuho Ozeki (Yamaguchi Univ.)

 sions
 10

Summary: We study homological torsions of modules and give a criterion for a certain equality of the first Hilbert coefficients of parameters and the homological torsions of modules.

19 <u>Kei-ichiro Iima</u> \* Linkage of modules over a Gorenstein local ring · · · · · · · · · 15 (Nara Nat. Coll. of Tech.) Ryo Takahashi (Nagoya Univ.)

Summary: The notion of linkage of modules was first studied by Yoshino and Isogawa. Later on it was explored by Martsinkovsky, Strooker and Nagel. Recently it has been investigated by many authors. In this talk, we aim at reconsidering a theorem of Yoshino and Isogawa by introducing the notion of linkage with respect to a perfect module.

20 Tokuji Araya (Okayama Univ. of Sci.) Thick subcategories of stable categories over graded Gorenstein rings

Summary: R. Takahashi classified the thick subcategories of the stable category of maximal Cohen–Macaulay modules over a hypersurface local ring. By his classification, we can see that if the base ring has an isolated singularity, then the thick subcategories are trivial. On the other hand, if the base ring is graded, then there exist non-trivial thick subcategories. In this talk, we will classify the thick subcategories of the stable category of graded maximal Cohen–Macaulay modules over a graded Gorenstein rings of finite Cohen–Macaulay representation type.

Summary: For a **Q**-domain A and a nonzero locally nilpotent derivation  $\delta$  of A, we consider the automorphism group  $\operatorname{Aut}(A/A^{\delta})$  of the  $A^{\delta}$ -algebra A, where  $A^{\delta} := \{a \in A \mid \delta(a) = 0\}$ . Let  $N_{\delta}$  be the set of the exponential automorphisms for the locally nilpotent  $A^{\delta}$ -derivations of A. Then,  $N_{\delta}$  is a normal subgroup of  $\operatorname{Aut}(A/A^{\delta})$ . In this talk, we discuss the structure of the quotient group  $\operatorname{Aut}(A/A^{\delta})/N_{\delta}$ . Our main result implies that, if A is a UFD such that  $A^{\times} \cup \{0\}$  is a field, then  $\operatorname{Aut}(A/A^{\delta})/N_{\delta}$  is isomorphic to  $A^{\times}$  or a finite cyclic subgroup of  $A^{\times}$ . Takehiko Yasuda (Osaka Univ.) Perspectives on the wild McKay correspondence

Summary: I will talk about my recent works (partly joint with Melanie Wood) on the McKay correspondence in the wild situation, and also about possible applications and future problems.

In the late 90's, Batyrev formulated the McKay correspondence in arbitrary dimension in characteristic zero by using stringy invariants, and proved it. Later Denef and Loeser gave an alternative and more conceptual proof using the motivic integration. A few years ago, I started to generalize their works to positive characteristics, in order to understand wild quotient singularities, that is, quotient singularities such that the relevant finite group has order divisible by the characteristic of the base field. It has turned our that although there is a significant difference, the basic strategy of Denef and Loeser is valid in positive characteristic too. Because of some technical difficulties, the final statement is still a conjecture. However, if it is true, it would relate singularities and the number theory. In the talk, I will also mention possible applications to desingularization problems, and also future problems including the globalization problem and explicit computations.

March 16th (Sun) Conference Room I

#### 9:00-12:00

Summary: We introduce a result on a question when the bounded-below complexes are J-cofinte, where J is an ideal of a regular ring of finite dimension.

Summary: A Toeplitz determinant whose entries are described by a *q*-analogue of the Narayana polynomials is evaluated by means of Laurent biorthogonal polynomials which allow of a combinatorial interpretation in terms of Schröder paths. As an application, a new proof is given to the Aztec diamond theorem by Elkies, Kuperberg, Larsen and Propp concerning domino tilings of the Aztec diamonds. The proof is based on the correspondence with non-intersecting Schröder paths developed by Johansson.

 

 24
 Takayuki Hibi
 \* A necessary and sufficient condition for strong Koszulness of edge rings (Osaka Univ./JST CREST)

 <u>Kazunori Matsuda</u> (Rikkyo Univ./JST CREST)
 associated with finite graphs

 Hidefumi Ohsugi (Rikkyo Univ./JST CREST)

Summary: We classify the finite connected simple graphs whose edge rings are strongly Koszul. It then follows that if the edge ring is strongly Koszul, then its toric ideal possesses a quadratic Gröbner basis.

Summary: In this talk, we define Cameron–Walker graphs and discuss some algebraic properties on edge ideals of Cameron–Walker graphs.

26 Akihiro Higashitani (Osaka Univ.) Minkowski sum of edge polytopes and its normality ..... 15

Summary: In this talk, we discuss the normality or the integer decomposition property of Minkowski sum of edge polytopes.

27 <u>Noritsugu Kameyama</u> (Shinshu Univ.) Categories including all G-projective modules ...... 10 Yuko Kimura (Shinshu Univ.) Kenji Nishida (Shinshu Univ.)

Summary: We generalize the some results of Ryo Takahashi to the categories of modules over noncommutative noetherian rings. Let the subcategories  $\mathcal{A}_k$ ,  $\mathcal{B}_k$   $(k \ge 1)$  of mod $\Lambda$  be  $\mathcal{A}_k = \{M \in \text{mod}\Lambda | \text{Ext}^i_{\Lambda}(\text{Tr}M, \Lambda) = 0, 1 \le i \le k\}$  and  $\mathcal{B}_k = \{N \in \text{mod}\Lambda | \text{Ext}^i_{\Lambda}(N, \Lambda) = 0, 1 \le i \le k\}$ . Let  $\mathcal{G}$  be the category of all G-projective modules. Then we study what properties of  $\mathcal{G}$  are succeeded to  $\mathcal{A}_k \cap \mathcal{B}_k$ . We also study the category equivalence between  $\mathcal{A}_k$  and  $\mathcal{B}_k$ .

<u>Takahide Adachi</u> (Nagoya Univ.)
 <u>Takuma Aihara</u> (Nagoya Univ.)
 Aaron Chan (Univ. of Aberdeen)
 Classifying two-term tilting complexes for Brauer graph algebras · · · · · 15

Summary: In this talk, we study two-term tilting complexes for Brauer graph algebras which are special biserial algebras defined by graphs. We classify two-term pretilting complexes by the special notion of walk, called admissible weighted line, on a graph. One of the main result we obtained is a bijection between the set of indecomposable two-term pretilting complexes and the set of admissible weighted lines. Furthermore, we use this bijection to obtain a combinatorial description for two-term tilting complexes. As an application, we can easily calculate the graph of the endomorphism ring of a two-term tilting complexes.

Summary: In this talk, we study a combinatorial structure of the class of tilting complexes for Brauer graph algebras, which is a representation-tame symmetric algebra. The class of tilting complexes possess a partial ordering. Then the following question arises naturally: When is the corresponding Hasse quiver connected? Our aim of this talk is to give a partial answer to the question. Brauer graph algebras are defined by graphs. A graph is said to be of type odd if it is a tree, or has only one subcycle of odd length and none of even length. We show that, if the graph of a Brauer graph algebra is of type odd, then the corresponding Hasse quiver is connected.

 30
 Hiroshi Nagase (Tokyo Gakugei Univ.)\*
 Counting regular prehomogeneous vector spaces associated with Dynkin

 <u>Makoto Nagura</u>
 quivers
 10

 (Nara Nat. Coll. of Tech.)
 (Nara Nat. Coll. of Tech.)
 (Nara Nat. Coll. of Tech.)

Summary: We count the number of isomorphism classes of hom-orthogonal partial tilting modules over path algebras of Dynkin quiver of type  $\mathbb{A}_n$ ,  $\mathbb{D}_n$ , or  $\mathbb{E}_n$ . This number is independent on the choice of an orientation of the arrows, and the number for  $\mathbb{A}_n$  or  $\mathbb{D}_n$ -type can be expressed as a special value of a hypergeometric function. As a consequence of our theorem, we obtain a minimum value of the number of basic relative invariants of corresponding regular prehomogeneous vector spaces.

 31
 Hideto Asashiba (Shizuoka Univ.)
 Tilted algebras and configurations of self-injective algebras of Dynkin

 Ken Nakashima (Shizuoka Univ.)
 type ······ 10

Summary: All algebras are assumed to be basic, connected finite-dimensional algebras over an algebraically closed field. We give a direct formula for a bijection from the set of isoclasses of tilted algebras of Dynkin type  $\Delta$  to the set of configurations on the translation quiver  $\mathbb{Z}\Delta$ .

Summary: The notion of unimodular finite tensor categories, introduced by Etingof, Nikshych and Ostrik, is a categorical generalization of the notion of finite-dimensional unimodular Hopf algebras. In this talk, I give a new characterization for unimodularity: A finite tensor category C is unimodular if and only if the forgetful functor from  $\mathcal{Z}(C) \to C$ , where  $\mathcal{Z}(C)$  is the monoidal center of C, is a Frobenius functor. This result is a categorical generalization of a theorem due to Caenepeel, Militaru and Zhu. I also give a generalization of the construction of commutative Frobenius algebra in a braided monoidal category due to Ishii and Masuoka.

#### 13:15–14:15 Talk invited by Algebra Section

Takeshi Ikeda (Okayama Univ. of Sci.) K-theory of the flag varieties of classical type

Summary: We introduce a family of polynomials that is identified with the basis consisting of the structure sheaves of the Schubert varieties in the torus equivariant K-theory of the flag variety of the classical types. We also review the corresponding results for the equivariant cohomology.

March 17th (Mon) Conference Room I

#### 9:30 - 12:00

33 Ryo Kanda (Nagoya Univ.)  $^{\flat}$  Specialization orders on atom spectra of Grothendieck categories  $\cdots 15$ 

Summary: The notion of the atom spectra of Grothendieck categories is a generalization of the prime spectra of commutative rings. We develop a theory of the specialization orders on the atom spectra of Grothendieck categories and introduce systematic methods to construct Grothendieck categories from colored quivers. We show that any partially ordered set is realized as the atom spectrum of some Grothendieck category, which is an analog of Hochster's result in commutative ring theory.

Summary: Taillefer gave the dimension formula of the cyclic homology of truncated quiver algebras over a field of characteristic zero. We show the dimension formula of the cyclic homology of truncated quiver algebras over an arbitrary field by means of a spectral sequence and chain maps given by Ames, Cagliero and Tirao. Our result generalizes the above result by Taillefer.

Summary: We calculate the dimensions of the Hochschild cohomology groups of a self-injective special biserial algebra  $\Lambda_s$  obtained by a circular quiver with double arrows, and determine the Hochschild cohomology ring of  $\Lambda_s$  modulo nilpotence with the Yoneda product.

36 <u>Takahiko Furuya</u> (Meikai Univ.) On Snashall's question about Hochschild cohomology · · · · · · · 10 Takao Hayami (Hokkai-Gakuen Univ.)

Summary: The purpose of this talk is to study the Hochschild cohomology groups and rings for some finitedimensional Koszul algebra  $\Lambda_t$  for integers  $t \geq 3$ . In fact we determine the dimensions of the Hochschild cohomology groups of  $\Lambda_t$ , and give a set of generators of the Hochschild cohomology ring modulo nilpotence of  $\Lambda_t$  as an algebra. This result tells us that the Hochschild cohomology ring modulo nilpotence of  $\Lambda_t$  is not finitely generated.

37 Hirotaka Koga (Univ. of Tsukuba) Clifford extensions ..... 15

Summary: In this talk, we generalize the construction of Clifford algebras and introduce the notion of Clifford extensions. Clifford extensions are constructed as Frobenius extensions which are Auslander–Gorenstein rings if so is a base ring.

Summary: In this talk, we introduce a notion of ampleness of a group action G on a noetherian graded algebra A. We show that if  $S = k[x_1, \ldots, x_d]$  is a polynomial algebra generated in degree 1, then a finite subgroup  $G \leq \text{SL}(d,k)$  is ample for S if and only if  $S^G$  is an isolated singularity. Moreover, if S is an AS-regular algebra and G is a finite ample group acting on S, then we show that  $\mathsf{D}^{\mathsf{b}}(\mathsf{tails}\,S^G) \cong \mathsf{D}^{\mathsf{b}}(\mathsf{mod}\,(\nabla S) * G)$  where  $\nabla S$  is the Beilinson algebra of S.

Summary: Let k be a field and consider the bicategory k-Cat<sup>b</sup> of small k-linear categories whose 1-morphisms are the bimodules over them (1-morphisms from A to B are the B-A-bimodules  ${}_{B}M_{A}$ ) and whose 2morphisms are the bimodule morphisms. We define a notion of derived equivalences and Grothendieck constructions for lax functors from a small category I to k-Cat<sup>b</sup>, and have the following result: Let X, X' be lax functors  $I \to k$ -Cat<sup>b</sup>. If X and X' are derived equivalent, then so are their Grothendieck constructions. This will be applied to triangular matrix algebras and tensor algebras of k-species.

Summary: S. Endo and Y. Watanabe proved that every separable R-algebra which is a finitely generated projective R-module is a symmetric, hence a Frobeniu R-algebra. However, K. Sugano showed that this is not always true in the case of ring extensions of non commutative rings. Y. Miyashita gave characterizations of a separable polynomial and a Frobenius polynomial in skew polynomial rings and he posed the following question: Is any separable polynomial in skew polynomial rings Frobenius? In this talk, we show some recent results with respect to this question in skew polynomial rings.

41 Tsunekazu Nishinaka On primitivity of group algebras of amalgamated free products · · · · · 10 (Okayama Shoka Univ.)

Summary: Let R be a ring with the identity element. A ring R is right primitive if and only if there exists a fathful irreducible right R-module  $M_R$ . Formanek proved that if G be a free product of non-trivial groups (except  $G = \mathbb{Z}_2 * \mathbb{Z}_2$ ), then KG is primitive for any field K. In particular, if G is a free group then KG is primitive for any field K. Motivated by the result, Balogun gave a result on primitivity of group rings of amalgamated free product, and the present author obtained a result on primitivity of group rings of locally free groups. However, the above two results are not complete generalizations of Formanek's one. In this talk, by making use of our recent method, we shall state two theorems which are complete generalizations of Formanek's results on free products and on free groups, respectively.

## 14:15-15:00

Summary: A rational method to tackle simultaneously two different kinds of 2-tuple problem is introduced. The first problem is regarding the gaps with even numbers  $(= 2, 4, 6, \cdots)$  between coupled primes which is known as Polignac conjecture or twin prime problem. The second one is regarding the sum of coupled primes which is known as Goldbach problem. A set of probable prime function is introduced to highlight the specified relationships between the coupled numbers. The probability of the number of the couples is determined in terms of the function then it is modified to the probability of the coupled primes on the basis of the prime theory.

43 Kenichi Shimizu \* On SP number · · · · · · · · 10 (Kenmei Girls' Junior and Senior High School)

Summary: Let a be any divisor of a natural number d and b = d/a, then we call d SP number if (a + b)/n is a prime, where n = 2, 1, 4 as  $d \equiv 1, 2, 3 \pmod{4}$ , respectively. We consider properties of SP number.

Summary: Waring's problem in number theory asks whether every natural number can be expressed as a sum of r-th powers of integers. The problem goes back to Edward Waring in 1770, as a natural generalization of Lagrange's four square theorem. After many efforts by hundreds of mathematicians, the problem was finally solved by Hilbert in 1909. A key step in Hilbert's proof was to show a lemma on the existence of a certain algebraic identity, called a Hilbert identity. In this talk, we shall review how such identities are closely connected with Waring's problem, and then point out Ellison's error in his proof of Hilbert's lemma.

#### 15:30–16:30 Award Lecture for 2014 Algebra Prize

Hidekazu Furusho (Nagoya Univ.) Various topics around associators

Summary: I will explain recent various topics related to associators. Particularly I will talk about 4 groups related to associators; the Grothendieck–Teichmüller group, the double shuffle group, the Kashiwara–Vergne group and the motivic Galois group.

## 16:45–17:45 Award Lecture for 2014 Algebra Prize

Yuji Yoshino (Okayama Univ.) Cohen-Macaulay modules over Cohen-Macaulay rings

Summary: I will present an introductory lecture on the theory of Cohen–Macaulay modules over Cohen–Macaulay rings. If possible, I will give some new results on the related topics.

March 18th (Tue) Conference Room I

## 9:00 - 12:00

45 Soichi Ikeda (Nagoya Univ.)<sup>♭</sup> Characterization of the Euler double zeta function · · · · · · · · · 10 Kaneaki Matsuoka (Nagoya Univ.)

Summary: We give an analogue of Hamburger's theorem for the Euler double zeta function.

Summary: The number of zeros and the distribution of the real part of non-real zeros of the derivatives of the Riemann zeta function have been investigated by Berndt, Levinson, Montgomery, and Akatsuka. Berndt, Levinson, and Montgomery investigated the general case, meanwhile Akatsuka gave sharper estimates for the first derivative of the Riemann zeta function under the truth of the Riemann hypothesis. In this paper, we generalize the results of Akatsuka to the k-th derivative (for positive integer k) of the Riemann zeta function.

Summary: Let f be a holomorphic cusp form of weight k with respect to  $SL_2(\mathbb{Z})$  which is a normalized Hecke eigenform,  $L_f(s)$  the *L*-function attached to the form f. In this talk, we shall give the approximate functional equation and mean value formula for the derivatives of  $L_f(s)$ . 49 Kalyan Chakraborty \* An inequality for Hecke multiplicative functions ...... 10 (Harish-Chandra Research Inst.) <u>Makoto Minamide</u> (Kyoto Sangyo Univ.)

Summary: Let f be an arithmetical function satisfying  $f(m)f(n) = \sum_{d|(m,n)} f(mn/d^2)$ . Soundararajan gave an inequality for  $\sum_{n \le x/y} |f(n)|^2$   $(1 \le y \le x)$  to settle the "Quantum ergodicity problem." We will derive an inequality for  $\sum_{n \le x/y} |f(n)|^k$  (for any k > 0).

Summary: We prove the mean square formula for the double zeta-function of Euler-Zagier type.

Summary: We first introduce in the talk a certain double holomorphic Eisenstein series of two complex variables; its transformation formulae and asymptotic expansions, both involving confluent hypergeometric functions, are presented. Various closed form evaluations for specific values (at positive and negative integer lattice points) of the double Eisenstein series in question are further given upon yielding some 'double analogues' of the classical Kronecker limit formulae.

52 Jun Furuya \* Mean values of the error term with shifted arguments in the circle (Okinawa Nat. Coll. of Tech.) problem ······ 10 Yoshio Tanigawa (Nagoya Univ.)

Summary: In this talk, we show the relation between the shifted sum of the error term in the circle problem and its continuous mean. In particular, we obtain a certain expression of the shifted sum as a linear combination of the continuous mean with the Bernoulli polynomials as the coefficients.

Yoshio Tanigawa (Nagoya Univ.)*	Mean square of	the	$\operatorname{error}$	$\operatorname{term}$	in	the	$\operatorname{asymmetric}$	$\operatorname{many}$	dimensional	
Xiaodong Cao	divisor problem					• • •				10
(Beijing Inst. of Petro-Chemical Tech.)										
Wenguang Zhai										
(China Univ. of Minig and Tech.)										
	Yoshio Tanigawa (Nagoya Univ.)* Xiaodong Cao (Beijing Inst. of Petro-Chemical Tech.) Wenguang Zhai (China Univ. of Minig and Tech.)	Yoshio Tanigawa Xiaodong Cao(Nagoya Univ.)* divisor problem divisor problem(Beijing Inst. of Petro-Chemical Tech.)Wenguang Zhai (China Univ. of Minig and Tech.)	Yoshio Tanigawa Xiaodong Cao(Nagoya Univ.)* divisor problem ···· divisor problem ···· (Beijing Inst. of Petro-Chemical Tech.)Wenguang Zhai (China Univ. of Minig and Tech.)	Yoshio Tanigawa (Nagoya Univ.)*Mean square of the errorXiaodong Caodivisor problem(Beijing Inst. of Petro-Chemical Tech.)Wenguang Zhai(China Univ. of Minig and Tech.)	Yoshio Tanigawa (Nagoya Univ.)*Mean square of the error termXiaodong Caodivisor problem(Beijing Inst. of Petro-Chemical Tech.)Wenguang Zhai(China Univ. of Minig and Tech.)	Yoshio Tanigawa (Nagoya Univ.)*Mean square of the error term in divisor problemXiaodong Caodivisor problem(Beijing Inst. of Petro-Chemical Tech.)Wenguang Zhai (China Univ. of Minig and Tech.)	Yoshio Tanigawa (Nagoya Univ.)*       Mean square of the error term in the divisor problem	Yoshio Tanigawa (Nagoya Univ.)*Mean square of the error term in the asymmetric divisor problemXiaodong Caodivisor problem(Beijing Inst. of Petro-Chemical Tech.)Wenguang Zhai (China Univ. of Minig and Tech.)	Yoshio Tanigawa (Nagoya Univ.)*       Mean square of the error term in the asymmetric many divisor problem         Xiaodong Cao       divisor problem         (Beijing Inst. of Petro-Chemical Tech.)       Wenguang Zhai         (China Univ. of Minig and Tech.)       (China Univ. of Minig and Tech.)	Yoshio Tanigawa (Nagoya Univ.)*       Mean square of the error term in the asymmetric many dimensional divisor problem         Xiaodong Cao       divisor problem         (Beijing Inst. of Petro-Chemical Tech.)       Wenguang Zhai         (China Univ. of Minig and Tech.)       (China Univ. of Minig and Tech.)

Summary: Let  $\Delta(\boldsymbol{a}; x)$  be the error term in the asymmetric many dimensional divisor problem. In this talk we show an asymptotic formula of the mean square of  $\Delta(\boldsymbol{a}; x)$  under a certain condition. In particular in the two and three dimensional cases, we give unconditional asymptotic formulas for these mean squares.

Summary: Borel proved that almost all nonnegative real numbers are normal in any integral base b. Borel also conjectured that every algebraic irrational number is normal in any integral base b, which is still unsolved. On the other hand, Wall proved for any integer  $b \ge 2$  that each nonnegative real number  $\xi$  is normal if and only if the geometric progression  $\xi b^n$  (n = 0, 1, ...) is uniformly distributed modulo one. In this talk, we study the fractional parts of  $\xi \alpha^n$  (n = 0, 1, ...) for general algebraic integer  $\alpha > 1$  and algebraic numbers  $\xi$ , which generalizes the problem of the normality of algebraic irrational numbers in integral base  $b \ge 2$ .

55 Taka-aki Tanaka (Keio Univ.) A new class of Mahler functions ..... 10

Summary: Mahler's method gives algebraic independence results for the values of functions of several variables satisfying certain functional equations under the transformations of the variables represented as a kind of multiplicative action of matrices with integral entries. In the Mahler's method, the entries of those matrices must be nonnegative; however, in the special case, those matrices are admitted to have a negative entry. We show the algebraic independence of the values of certain functions satisfying functional equations under the transformation represented by such matrices.

Summary: We study the supplementary formulas for the Sheffer sequences. As applications of that study, we consider characterizations of the Bernoulli, Euler and poly-Bernoulli polynomials.

57 <u>Takao Komatsu</u> (Hirosaki Univ.) A note on the denominators of Bernoulli numbers ..... 10 Florian Luca (UNAM) Claudio de J. Pita Ruiz V. (Univ. Panamericana)

Summary: We show that  $gcd(2!S(2n + 1, 2), ..., (2n + 1)!S(2n + 1, 2n + 1)) = denominator of B_{2n}$ , where S(n, k) is the Stirling number of the second kind and  $B_n$  is the Bernoulli number.

58 Takafumi Miyazaki (Nihon Univ.)\* On the system of Diophantine equations  $a^2 + b^2 = (m^2 + 1)^r$  and  $a^x + b^y = (m^2 + 1)^z \cdots 15$ 

Summary: Let r, m be positive integers with r > 1, m even, and A, B integers satisfying  $A + B\sqrt{-1} = (m + \sqrt{-1})^r$ . We prove that the Diophantine equation  $|A|^x + |B|^y = (m^2 + 1)^z$  has no positive integer solutions in (x, y, z) other than (x, y, z) = (2, 2, r), whenever  $r > 10^{74}$  or  $m > 10^{34}$ . This result is an explicit refinement of a theorem due to F. Luca in 2012.

#### 14:15-16:45

59	Yûsuke Okuyama (Kyoto Inst. Tech.)	A quantitative logarithmic equidistribution in non-archimedean ar	ıd
		complex dynamics	$\cdot \cdot 15$

Summary: Let  $f \in K(z)$  be a rational function of degree more than one over an algebraically closed field K of characteristic 0 and complete with respect to a non-trivial and possibly non-archimedean absolute value  $|\cdot|$ . In this talk, we establish a quantitative approximation of the Lyapunov exponent L(f) of f with respect to the canonical measure  $\mu_f$  of f using the multipliers  $(f^n)'(w)$  of non-superattracting fixed points w of  $f^n$ ,  $n \in \mathbb{N}$ .

Summary: Let k be a field, and  $k_s$  the separable closure of k in the algebraic closure  $\overline{k}$  of k. An algebraic zeros divisor (P) on the projective line  $\mathbb{P}^1(\overline{k})$  over  $\overline{k}$ , which is by definition the zeros divisor on  $\mathbb{P}^1(\overline{k})$  of a homogeneous polynomial P of two variables over k, generalizes both the Galois conjugacy class of a point in the affine line  $\mathbb{A}^1(\overline{k})$  over  $\overline{k}$  and the roots divisor of the equation f = a on  $\mathbb{P}^1(\overline{k})$  for distinct rational functions  $f, a \in k(z)$  satisfying min $\{\deg f, \deg a\} > 0$ . We will state a result on the asymptotic behavior of a sequence  $((P_n))$  of algebraic zeros divisors on  $\mathbb{P}^1(k_s)$  having small diagonals and small heights.

61 Tetsuya Uematsu (Chuo Univ.) On zero-cycles on diagonal cubic surfaces over *p*-adic fields ..... 10

Summary: The Chow groups of varieties are fundamental invariants in the study of their arithmetic and geometry. In this research, we explicitly compute the Chow group of zero-cycles on some diagonal cubic surfaces over p-adic fields by using Milnor-K-theoretic symbolic generators of their Brauer groups constructed by Manin and the author, and by applying some results for the Brauer–Manin pairings due to Colliot-Thélène, Saito and Sato. Moreover, we find that some of them are generated only by the class of rational points. Besides symbolic generators and the Brauer–Manin pairings, a certain reduction to elliptic curves plays an impotant role in the proof of this result.

Summary: In this presentation, we study asymptotic behaviors for sums of class numbers of discriminants which give soluble Pell-type equations.

Summary: It is known that there are linear relations over  $\mathbb{Q}$  among periods of elliptic modular forms which are called 2-cycle and 3-cycle relations developed by Eichler and Shimura. This theory often appears in the context of multiple zeta values. In 2006, Gangl, Kaneko and Zagier gave a direct correspondence between coefficients of a linear relation among periods and coefficients of a linear relation among double zeta values. Their result may well be generalized to the higher depth, however it is still pending. In my talk, we will show an indirect relationship between the period theory and multiple zeta values.

64 Hirofumi Nagoshi (Gunma Univ.)\* Combining three theorems on the joint universality of L-functions  $\cdots$  10

Summary: We combine Bagchi–Gonek–Voronin's theorem, Laurinčikas–Matsumoto's theorem and Mishou's theorem, which are concerning the joint universality of *L*-functions.

Summary: In this talk, as a generalization of reciprocity formulas for Dedekind sums, we consider the one due to Halbritter. We show how the formula is interpreted from a combinatorial-geometric viewpoint.

66 <u>Aiichi Yamasaki</u> (Kyoto Univ.) Class numbers and algebraic tori · · · · · · · · · · · · · · · 10 Akinari Hoshi (Niigata Univ.) Ming-chang Kang (Nat. Taiwan Univ.)

Summary: Let p be an odd prime number,  $D_p$  be the dihedral group of order 2p,  $h_p$  and  $h_p^+$  be the class numbers of  $\mathbb{Q}(\zeta_p)$  and  $\mathbb{Q}(\zeta_p + \zeta_p^{-1})$  respectively. Theorem.  $h_p^+ = 1$  if and only if, for any field k admitting a  $D_p$ -extension, all the algebraic tori over k and split by some dihedral extension K/k are always stably rational. A similar result for  $h_p = 1$  and  $C_p$ -tori is valid also.

Summary: Ramakrishnan and Rogawski gave an asymptotic formula for a mean of central *L*-values attached to the imaginary quadratic base change of elliptic holomorphic cusp forms with prime level as the level tends to infinity. Feigon and Whitehouse extended their result to the case of Hilbert cusp forms with square free level when the quadratic extention involved is totally imaginary. In this talk, we report our recent generalization of their asymptotic formula for Hilbert cusp forms to arbitrary levels, dropping the totally imaginary condition of the quadratic extension at the same time. As an application of this, we obtain a subconvexity bound of quadratic base change L-functions for Hilbert cusp forms in the weight aspect. This is a joint work with Masao Tsuzuki (Sophia University).

Summary: We show that the Galois group of the maximal unramified pro-2-extension over the  $\mathbb{Z}_2$ -extension of a real quadratic field is never isomorphic to a semidihedral group.

69 Yasushi Mizusawa \* Isometric embeddings of finite fields · · · · · · · · · · · · 10 (Nagoya Inst. of Tech.)

Summary: By regarding a finite field as a vector space over the prime field with a power basis, a Hamming distance is defined on the finite field with respect to the power basis. We give an equivalent condition of existence of isometric homomorphisms between such finite fields of characteristic 2.

70 <u>Shota Kojima</u> (Rikkyo Univ.) Nested square roots and Poincaré functions ..... 10 Noboru Aoki (Rikkyo Univ.)

Summary: Nested square roots of 2 are expressed by using a trigonometric function and its zeros. This result was obtained by Wiernsberger and Lebesgue. In this talk, we give an expression of nested square roots of c > 2 by using a Poincaré function and its zeros.

## Geometry

March 15th (Sat) Confe

Conference Room VII

## 9:20 - 12:00

1 Hirotaka Ebisui (Oval Research Center) About Descartes Oval as the pure extension of Ellipse ..... 5

Summary: Theoretical extenssion of ellipse to 4th oder curve (Descartes Oval named as Doval) have not been expressed yet. Now we got them by Geomebra Soft and its figure. We can show Doval is the theoretical extension of Ellipse that is exchanged from "line" (infinity radius circle) to "circle" in the Ellipse-definition: the curve that has constant ratio between two distance from fixed point and fixed "line". We know the importance of Ellipse in many field. Now we can say that Doval is the same position as Ellipse.

Summary: We classify Hopf hypersurfaces with  $\eta$ -parallel Ricci tensor in a nonflat complex space form  $\widetilde{M}_n(c), n \geq 2$ . Note that there exist nonhomogeneous Hopf hypersurfaces with  $\eta$ -parallel Ricci tensor in  $\widetilde{M}_2(c), c \neq 0$ .

Summary: We characterize the horosphere, the homogeneous real hypersurface of type (B) having two distinct constant principal curvatures and the homogeneous ruled real hypersurface in a complex hyperbolic space.

Summary: We list up all the possible local orbit types of hyperbolic or elliptic orbits for the s-representations of semisimple pseudo-Riemannian symmetric spaces. It is key to give a recipe to determine the local orbit types of hyperbolic principal orbits by using three kinds of Satake diagrams associated with semisimple pseudo-Riemannian symmetric spaces.

5 <u>Hiroyuki Kurihara</u> (Ibaraki Univ.) Involutions on a compact 4-symmetric space of exceptional type ..... 15 Koji Tojo (Chiba Inst. of Tech.)

Summary: Let  $(G/H, \sigma)$  be a compact 4-symmetric space of inner and exceptional type. Suppose that the dimension of the center of H is one and H is not a centralizer of a toral subgroup. In this talk, we talk about the classification of involutions  $\tau$  of G satisfying  $\tau \sigma = \sigma \tau$ .

Summary: In this talk, we state some results for the (regularized) mean curvature flow starting from invariant hypersurfaces in a Hilbert space equipped with an isometric almost free Hilbert Lie group action whose orbits are minimal regularizable submanifolds. First we prove that the (regularized) mean curvature flow starting from a certain kind of invariant hypersurface uniquely exists in short time. Next I state the evolution equation for some geometric quantities along the regularized mean curvature flow. Also, by using the evolution equations, we prove a horizontally strongly convexity preservability theorem for the regularized mean curvature flow. From this theorem, we derive the strongly convexity preservability theorem for the regularized mean curvature flow starting from a compact Riemannian suborbifold in the orbit space (which is a Riemannian orbifold) of the Hilbert Lie group action.

Summary: We are studying a relationship between isoparametric hypersurfaces in spheres with four distinct principal curvatures and the moment maps of certain Hamiltonian actions. In this talk, we consider the isoparametric hypersurfaces obtained from the isotropy representations of Grassmannian manifolds of rank two.

8 Akira Kubo (Hiroshima Univ.) Geometry of polar actions on complex hyperbolic spaces ..... 10

Summary: An isometric action on a Riemannian manifold is said to be *polar* if there exists a complete connected closed submanifold which meets all the orbits and intersects them orthogonally. In this talk, I will talk about polar actions without singular orbits on complex hyperbolic spaces, and minimality of their orbits.

Summary: It is known that there exist SO(n+1)-invariant complete Ricci-flat Kähler metrics on the cotangent bundle  $T^*S^n$  of the standard sphere  $S^n$ , so called the Stenzel metrics. We are studying cohomogeneity one special Lagrangian submanifolds in the cotangent bundle of the sphere with respect to the Stenzel metric. In this talk, we discuss a description of all cohomogeneity one special Lagrangian submanifolds which are invariant under the group actions induced by isotropy representations of Riemannian symmetric spaces of rank 2.

Summary: We study area-minimizing cones in the Euclidean space constructing area-nonincreasing retractions. We obtain new examples of area-minimizing cone over minimal R-spaces.

#### 14:30 - 15:25

Summary: We determine three-dimensional locally homogeneous nondegenerate centroaffine hypersurfaces with null Tchebychev vector field.

Summary: In this paper, we introduce a new variational problem on the space  $\mathfrak{T}_2^0 \times \mathfrak{T}_2^{0*}$  of the tensor product of the bundle of smooth (0, 2)-tensors and the bundle of smooth (0, 2)-tensors with non-zero determinant. Given a  $(P, \eta) \in \mathfrak{T}_2^0 \times \mathfrak{T}_2^{0*}$ , fixing P we consider the functional  $E(\eta)$ . Varying the tensor  $\eta$ , we calculate the 1st and 2nd variational formulaes for the variational problem.

Summary: We obtain an inequality involving the first Chern class of the normal bundle and the conformal area for a twistor holomorphic surface. Using this inequality, we can improve an inequality obtained by T. Friedrich for the Euler class of the normal bundle of a twistor holomorphic surface in the four-dimensional space form. Moreover, as a corollary, we see that the area of a superminimal surface in the unit sphere is an integer multiple of  $2\pi$ , which is essentially proved by E. Calabi.

14 Mitsuhiro Itoh (Univ. of Tsukuba) Barycenter and information geometry ...... 10 Hiroyasu Satoh (Tokyo Denki Univ.)

Summary: By applying barycenter of probability measures on the ideal boundary of an Hadamard manifold X we obtain a theorem which states that under certain assumptions a homeomorphism  $\Phi$  of the ideal boundary yields a Riemannian isometry of X.

#### 15:40–16:40 Talk invited by Geometry Section

Yu Kawakami (Yamaguchi Univ.) Value distribution of the Gauss map of surfaces

Summary: We elucidate the geometric background of function-theoretic properties (e.g. ramification theorem, unicity theorem) for the Gauss maps of several classes of immersed surfaces in three-dimensional space forms, for example, minimal surfaces in Euclidean three-space, flat surfaces in hyperbolic three-space and improper affine spheres in the affine three-space.

## March 16th (Sun) Conference Room VII

#### 9:40 - 11:50

Summary: Motivated by a fundamental geometrical object, cut locus, we introduce and study a new combinatorial structure on graphs, called cut locus structure. We present all distinct cut locus structures on 3-graphs with 2 or 3 generating cycles.

Summary: An (I, J, K)-generalized Finsler structure on a 3-manifold is a generalization of a Finslerian structure, introduced by R. Bryant in order to separate and clarify the local and global aspects in Finsler geometry making use of Cartan's method of exterior differential systems. In this talk, we show that there is a close relation between (I, J, 1)-generalized Finsler structures and a class of contact circles, namely the so-called *Cartan structures*. This correspondence allows us to determine the topology of 3-manifolds that admit (I, J, 1)-generalized Finsler structures and to single out classes of (I, J, 1)-generalized Finsler structures induced by standard Cartan structures.

 17
 Jun-ichi Inoguchi (Yamagata Univ.)
 Discrete mKdV and discrete sine-Gordon flows on discrete space curves

 17
 Kenji Kajiwara (Kyushu Univ.)
 Discrete mKdV and discrete sine-Gordon flows on discrete space curves

 17
 Nozomu Matsuura (Fukuoka Univ.)
 To serve mKdV and discrete sine-Gordon flows on discrete space curves

 18
 Nozomu Matsuura (Fukuoka Univ.)
 To serve mKdV and discrete space curves

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 Yasuhiro Ohta
 (Kobe Univ.)

Summary: We investigate discrete deformations of discrete space curves with constant torsion, and present a formula which describes torsion-preserving deformation. Especially, we show that the direction of the deformation is determined by the discrete mKdV equation or the discrete sine-Gordon equation at each time-step. We also show that our formula produces the discrete K-surfaces, which is a discrete analogue of the surfaces with constant negative Gaussian curvature.

Summary: A triharmonic map is a critical point of the 3-energy in the space of smooth maps between two Riemannian manifold. We study the generalized Chen's conjecture for a triharmonic isometric immersion  $\varphi$ into a space form of non-positively constant curvature. We show that if the domain is complete and both the 4-energy of  $\varphi$ , and the  $L^4$ -norm of the tension field  $\tau(\varphi)$ , are finite, then such an immersion  $\varphi$  is minimal.

#### 28 Geometry

- 19 Shigehiro Sakata (Tokyo Metro. Univ.) Uniqueness of a center of a body and geometry of the heart ······ 15 Summary: We consider the dual intrinsic volume of order alpha of a convex body K and investigate the uniqueness of its maximum point. It is easy to show that the dual intrinsic volume is proportional to the Riesz potential. Using the moving plane method, we can restrict the location of a maximum point of the Riesz potential into a smaller region in K, which is called the heart of K. Using geometric properties of the heart of K, we give a sufficient condition for the uniqueness of a maximum point of the Riesz potential.

21<u>Hiroki Sako</u> (Tokai Univ.)Group approximation in Cayley topology and coarse geometry, Part I:<br/>Masato Mimura (Tohoku Univ.)Coarse embeddings of amenable groups.15

Summary: Objective of this series is to study metric geometric properties of coarse disjoint union of Cayley graphs. We employ the Cayley topology and observe connection between large scale structure of metric spaces and group properties of Cayley limit points. In this part I, we prove that a coarse disjoint union has property A of G. Yu if and only if all Cayley limit groups are amenable. As an application, we construct a coarse disjoint union of finite special linear groups which has property A but is of very poor compression into all uniformly convex Banach spaces.

#### 13:00–14:00 Talk invited by Geometry Section

Kei Funano (Kyoto Univ.) Eigenvalues of Laplacian and multi-way isoperimetric constants on Riemannian manifolds

Summary: In this talk, I will discuss the distribution of eigenvalues of the weighted Laplacian on closed weighted Riemannian manifolds of nonnegative Bakry–Émery Ricci curvature. As an application of the curvature dimension condition, I will derive some universal inequalities among eigenvalues of the weighted Laplacian on such manifolds. These inequalities are quantitative versions of the previous theorem by the speaker with Shioya. I will also discuss some geometric quantity, called multi-way isoperimetric constants, on such manifolds and obtain similar universal inequalities among them. Multi-way isoperimetric constants are generalizations of the Cheeger constant. I will explain the relation between the k-th eigenvalue and the k-way isoperimetric constant.

March 17th (Mon) Conference Room VII

### 10:00 - 11:50

Summary: In this talk, we study the prequantization problem to manifolds with Dirac structures, called a Dirac manifolds. After reviewing the foundations of Dirac manifolds, we endow the space of admissible functions with Poisson structure in a different way from the usual and construct the representation of the space of admissible functions. Additional to this, we provide a necessary and sufficient condition for the non-commutative brackets to be preserved under the representation.

#### 29 Geometry

23 Yushi Okitsu (Tokyo Tech) The cutting construction of weakly convex contact toric manifolds · · · 10

Summary: We introduce the cutting construction of toric symplectic cones that correspond to a weakly convex good cone. Since the symplectization of a toric contact manifold is a toric symplectic cone, we can also construct toric contact manifolds that correspond to a weakly convex good cone by the cutting construction. (Note that these toric contact manifolds can not be constructed by Delzant construction.) We further prove there are no toric Sasakian structures on these contact manifolds. From this, contact toric manifolds of K-contact type are of toric Sasakian type.

24 Homare Tadano (Osaka Univ.) Gap theorems for compact gradient Sasaki–Ricci solitons · · · · · · · 15

Summary: In this talk we give some necessary and sufficient conditions for compact gradient Sasaki–Ricci solitons to be Sasaki–Einstein. Our result [3] may be considered as a Sasaki geometry version of recent works by H. Li [2] and M. Fernández-López and E. García-Rio [1].

References

M. Fernández-López and E. García-Rio, Some gap theorems for gradient Ricci solitons, Internat. J. Math., 23 (2012), no. 7, 1250072, 9 pages.

[2] H. Li, Gap theorems for Kähler-Ricci solitons, Arch. Math. (Basel), 91 (2008), no. 2, 187–192.

- [3] H. Tadano, Gap theorems for compact gradient Sasaki-Ricci solitons, preprint, 2013.

Summary: A Lie foliation  $\mathcal{F}$  is transversely modeled on a Lie group G with the canonical left G-action. Lie foliations have been studied motivated by the fact that the classification of Riemannian foliations is reduced to the case of Lie foliations by Molino theory. In this talk, we will present a rigidity result for Lie foliations whose leaves are symmetric spaces which do not have a Poincaré disk as an irreducible component. It says that such foliation is homeomorphic to a foliation on a double coset space whose leaves are cosets. The result can be regarded as an improvement of a preceding result of Zimmer.

Summary: Birkhoff normal form is a power series expansion associated with the local behavior of the Hamiltonian systems near a critical point. It is known to be convergent for integrable systems under some non-degeneracy conditions. By means of an expression of the inverse of Birkhoff normal form by a period integral, analytic continuation of the Birkhoff normal forms is considered for the free rigid body dynamics on SO(3). The global behavior of the Birkhoff normal forms is clarified in relation to the monodromy of an elliptic fibration which naturally arises from the free rigid body dynamics.

27	Akira Ushijima (Kanazawa Univ.)	On the maximal volume of three-dimensional hyperbolic complete or-
	Kazuhiro Ichihara (Nihon Univ.)	thoschemes sharing the same base 10

Summary: A three-dimensional orthoscheme is defined as a tetrahedron whose base is a right-angled triangle and an edge joining the apex and a non-right-angled vertex is perpendicular to the base. A generalization, called complete orthoschemes, of orthoschemes is known in hyperbolic geometry. Roughly speaking, complete orthoschemes consist of three kinds of polyhedra; either compact, ideal or truncated. We consider a particular family of hyperbolic complete orthoschemes, which share the same base. They are parametrized by the "height", which represents how far the apex is from the base. We prove that the volume attains maximal when the apex is ultraideal in the sense of hyperbolic geometry, and that such a complete orthoscheme is unique in the family.

### 14:20–15:20 Talk invited by Geometry Section

Tatsuya Tate (Tohoku Univ.) One and two dimensional quantum walks

Summary: The notion of discrete-time quantum walks are defined as a non-commutative analogue of the usual random walks. These are intensively investigated in computer sciences, probability theory and quantum physics. Recently, in a joint work with T. Sunada, the author obtained various local asymptotic formulas for the one-dimensional discrete-time quantum walks. From this, one obtains a concrete formula of the rate function for the large deviation of discrete-time quantum walks. In the beginning of the talk, these asymptotic result for one-dimensional quantum walks will be roughly explained. There are another notion of the quantum walks, namely continuous-time quantum walks. These are defined as a unitary evolution for the transition operators of classical random walks. It was asked by Ambainis in computer sciences the relation between continuous-time and discrete-time random walks. In the talk, a direct relation between two object for one-dimension will be explained. In a high-dimensional case, there are only a few result are known. According to a recent result, the one-dimensional discrete-time quantum walks are obtained from the regular representation of the infinite dihedral group. In the talk, certain class of two-dimensional quantum walks are introduced using a representation of a discrete group. Asymptotic results for these class of quantum walks are not obtained, but some properties will be presented in the talk.
## **Complex Analysis**

March 15th (Sat) Confe

Conference Room VIII

### 9:30 - 11:45

Summary: In this article, the integral contours  $C = \{C_{-}, C_{+}\}$  of the N-fractional calculus, the integral interval of the fractional integral of Riemann-Liouville and that of Weyl are discussed. And the N fractional calculus of order  $\alpha$  and  $\pi \in \mathbb{Z}^{+}$  the derivatives of a composite function are reported.

And the N-fractional calculus of order  $\gamma$  and  $n \in \mathbb{Z}_0^+$  the derivatives of a composite function are reported. Moreover, some identities are reported which are obtained by the calculations

$$(((z-b)^4-c)^{-1})_{\gamma} = (((z-b)^4-c)^{-2} \cdot ((z-b)^4-c))_{\gamma}$$

and

$$(((z-b)^4-c)^{-1})_{\gamma} = ((((z-b)^4-c)^{-1})_1)_{\gamma-1}$$

for example.

2 Rikio Yoneda \* The invertible Toeplitz operator and the Berezin transform · · · · · · 10 (Otaru Univ. of Commerce)

Summary: In this talk, we study the invertible Toeplitz operator.

Summary: The semigroup associated with the Dirichlet heat kernel is said to be intrinsic ultracontractive if the Dirichlet realization of the associated self adjoint operator has the first positive eigenvalue with positive  $L^2$  eigenfunction; and the heat kernel is bounded above and below by the product of the eigenfunctions with positive multiplicative constants depending on time.

We give a sharp sufficient integral condition for intrinsic ultracontractivity in terms of capacitary width with the aid of a parabolic box argument. A similar integral condition for the boundary Harnack principle is also obtained.

Summary: Let R be an open Riemann surface of finite genus, and  $\Phi$  an Abelian integral on R which satsifies certain conditions similar to the classical extremal parallel slit mappings. Then, R is extended to a compact Riemann surface S of the same genus and  $\Phi$  is continued to an Abelian integral  $\Psi$  on S, in such a way that  $\Psi$  is holomorphic on the realized ideal boundary  $E := S \setminus R$ . Theorem: For any component  $\delta$  of Ethe number of zeros of  $d\Psi$  on  $\delta$  is constant for all  $\Psi$ 's, rovided that  $\Phi$ 's have the same singularities and the same periods.

#### 32 Complex Analysis

5 Kengo Shimomura (Osaka Univ.) Deformation of a triangle group and the iterated function system · · · · 15 Ryosuke Mineyama (Osaka Univ.)

Summary: Triangle groups can be regarded as Coxeter groups. Classically it is known that Coxeter groups are equipped with actions on vector spaces as like reflections. In this talk we will talk that the projection of such classical action of a triangle group induce some iterated function system. Concretely we shall introduce how the variation of the Hausdorff dimension of the limit set of a triangle group  $W = \langle s_0, s_1, s_2 | s_0^2 = s_1^2 = s_2^2 = 1 \rangle$  depends continuously on the deformation of W.

Summary: We consider the metric  $d_L$  on Teichmüller spaces defined by the length spectrums of Riemann surfaces. It is known that the metric  $d_L$  defines the same topology as that of Teichmüller metric  $d_T$ on Teichmüller spaces of Riemann surfaces of finite type. In 2003, H. Shiga proved that there exists a Teichmüller space  $T(R_0)$  of Riemann surface of infinite type such that  $d_L$  and  $d_T$  do not define the same topology on  $T(R_0)$ . Also he gave a sufficient condition for  $d_L$  and  $d_T$  to define the same topology on Teichmüller space. In this talk, we extend Shiga's result to Teichmüller spaces satisfying a certain geometric condition.

7 Yuki Iguchi (Tokyo Tech) On accumulation points of Teichmüller geodesics · · · · · · · · · 15

Summary: We investigate accumulation points of arbitrary Teichmüller geodesic rays in Thurston's compactification of a Teichmüller space. We find a boundary point to which no ray accumulates. We also showed that an accumulation point of a geodesic is represented by a measured foliation which has the same minimal decomposition of the measured foliation associated with the geodesic.

Summary: A periodic point on a Veech surface is a point whose orbit under the affine group is finite. The number of periodic points on a non-arithmetic Veech surface is finite. We give upper bounds of the numbers of periodic points that depend only on the topological type of Veech surfaces and signatures of the Veech groups.

### 14:15-15:45

 9 <u>Tatsuhiro Honda</u> Growth and distortion theorems on homogeneous unit balls ..... 15 (Hiroshima Inst. of Tech.)
 Hidetaka Hamada (Kyushu Sangyo Univ.)
 Gabriela Kohr (Babeş-Bolyai Univ.)

Summary: In this talk, we obtain growth and distortion theorems for linearly invariant families  $\mathcal{F}$  of locally biholomorphic mappings on the homogeneous unit ball B of an n-dimensional complex Banach space Xwith finite norm-order. Note that the reason for which we use the Euclidean norm  $\|\cdot\|_e$  for the target space instead of the norm on X is that we are able to obtain lower bounds in the two-point distortion theorems forlinearly invariant families on any homogeneous unit ball in  $\mathbb{C}^n$ . Next, we obtain similar results for affine and linearly invariant families of pluriharmonic mappings of the unit ball B into  $\mathbb{C}^n$ . Martin Chuaqui (Catholic Univ. of Chile)
 <u>Hidetaka Hamada</u> (Kyushu Sangyo Univ.)
 Rodrigo Hernández (Univ. Adolfo Ibáñez)
 Gabriela Kohr (Babeş-Bolyai Univ.)

Summary: In this talk, we obtain certain sufficient conditions for the univalence of pluriharmonic mappings defined in the unit ball  $\mathbb{B}^n$  of  $\mathbb{C}^n$ . The results are generalizations of conditions of Chuaqui and Hernández that relate the univalence of planar harmonic mappings with linearly connected domains, and show how such domains can play a role in questions regarding injectivity in higher dimensions.

 11 Ian Graham (Univ. of Toronto) Loewner differential equations in reflexive complex Banach spaces · · · · 15 <u>Hidetaka Hamada</u>

(Kyushu Sangyo Univ.) Gabriela Kohr (Babeş-Bolyai Univ.) Mirela Kohr (Babeş-Bolyai Univ.)

Summary: In this talk, we consider univalent subordination chains in reflexive complex Banach spaces, allowing the chains to be normalized in terms of a positive linear operator. Related adaptations in the generalized Loewner differential equation are also considered. The results in this talk are generalizations to reflexive complex Banach spaces of classical and recent results in the theory of Loewner chains and the Loewner differential equation on the unit ball in  $\mathbb{C}^n$ .

 12
 Ian Graham (Univ. of Toronto)
 Extremal properties associated with univalent subordination chains in

 <u>Hidetaka Hamada</u>
  $\mathbb{C}^n$  15

 (Kyushu Sangyo Univ.)
 Gabriela Kohr (Babeş-Bolyai Univ.)
 15

 Mirela Kohr (Babeş-Bolyai Univ.)
 15

Summary: Under the assumption  $k_+(A) < 2m(A)$ , where  $A \in L(\mathbb{C}^n)$ , we consider the family  $S^0_A(B^n)$  of mappings which have A-parametric representation on the Euclidean unit ball  $B^n$  in  $\mathbb{C}^n$ , i.e.  $f \in S^0_A(B^n)$ if and only if there exists an A-normalized univalent subordination chain f(z,t) such that  $f = f(\cdot,0)$  and  $\{e^{-tA}f(\cdot,t)\}_{t\geq 0}$  is a normal family on  $B^n$ . We prove that if  $f = f(\cdot,0)$  is an extreme point (respectively a support point) of  $S^0_A(B^n)$ , then  $e^{-tA}f(\cdot,t)$  is an extreme point of  $S^0_A(B^n)$  for  $t \geq 0$  (respectively a support point of  $S^0_A(B^n)$  for  $t \geq 0$ ). These results generalize to higher dimensions related results due to Pell and Kirwan. We also consider extremal problems related to bounded mappings in  $S^0_A(B^n)$ .

 13 Atsushi Yamamori (POSTECH)\*
 On holomorphic automorphisms fixing the origin and the Bergman mapping

 15
 15

Summary: In this talk, we prove that every origin-preserving automorphism of normal quasi-circular domains is linear.

### 16:00–17:00 Talk invited by Complex Analysis Section

Hideki Miyachi (Osaka Univ.) Thurston theory on the geometry of Teichmüller space

Summary: I will talk on the "Thurston theory" on the extremal length geometry on Teichmüller space. Indeed, I will give a development on the Teichmüller geometry via the intersection number. Especially, I will explain a relation between the Gromov product with respect to the Teichmüller distance and the intersection number on the space of measured foliations. I will also deal with the rigidity at infinity of the isometries on Teichmüller space.

March 16th (Sun) Conference Room VIII

#### 9:30 - 10:45

14 Sachiko Hamano (Fukushima Univ.) Variation of reproducing kernels for the spaces of holomorphic semiexact

Summary: We study the reproducing kernel for the Hilbert space of all holomorphic semiexact differentials on an open Riemann surface. We show the property of variation of the reproducing kernels with complex parameter under pseudoconvexity.

15 <u>Katsusuke Nabeshima</u> Parametric local cohomology and logarithmic vector fields · · · · · · · 15 (Univ. of Tokushima) Shinichi Tajima (Univ. of Tsukuba)

Summary: We have developed a new framework to study logarithmic vector fields along a hypersurface with an isolated singular point. The key of this approach is the concept of a polar variety. By using parametric local cohomology, we have derived an algorithmic method to compute logarithmic vector fields with parameters.

16 Atsushi Hayashimoto \* Gap theorem for generalized pseudoellipsoids · · · · · · · · · · 15 (Nagano Nat. Coll. of Tech.)

Summary: We show a gap theorem for generalized pseudoellipsoids. It is a generalization of a gap theorem for balls by Faran et al. and for pseudoellipsoids by Ebenfelt–Son.

 

 17 Masanori Adachi (Nagoya Univ.)
 A local formula for the Diederich–Fornaess exponent on domains bounded by Levi-flat real hypersurfaces

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 10

Summary: To understand geometry of Levi-flat real hypersurfaces in complex manifolds, we have two viewpoints: one is from pseudoconvexity of their complements and the other is from dynamics of their foliations. We connect two approaches by quantifying Brunella's correspondence between Takeuchi 1-convexity of their complements and positivity of their normal bundles; we will report a local formula for the Diederich–Fornaess exponents of their boundary distances in terms of certain curvatures of the induced hermitian metrics on their normal bundles.

Summary: We show the existence of continuous Hermitian metrics with semi-positive curvatures on Zariski's example of a line bundle defined over the blow-up of  $\mathbb{P}^2$  at some twelve points which is nef, big, not semi-ample, and whose section ring is not finitely generated. We generalize this result to the higher dimensional case when the base locus D of a line bundle is a smooth hypersurface with a holomorphic tubular neighborhood. More precisely, we write down a minimal singular metric of the line bundle around D by only using some special minimal singular metrics of some  $\mathbb{R}$ -line bundles over D in such a situation.

### 11:00–12:00 Talk invited by Complex Analysis Section

Makoto Abe (Hiroshima Univ.) Meromorphic convexity and Steinness for complex spaces

Summary: We discuss meromorphic convexity and Steinness for complex spaces, especially meromorphic approximation properties and characterizations of Steinness for domains in a Stein space.

March 15th (Sat) Conference Room V

### 9:00-12:00

1	Koh Katagata	Configurations of equilibrium points in complex differential equations	
	(Ichinoseki Nat. Coll. of Tech.)	and the Euler–Jacobi formula · · · · · · · · · · · · · · · · · · ·	10

Summary: In this talk, we study the qualitative theory of first order differential equations consisting of the iteration of complex quadratic rational functions and we focus on the configuration, namely location and stability, of simple equilibrium points which correspond to periodic points of the quadratic rational functions. Our main tools are properties of Julia sets of the quadratic rational functions and the Euler-Jacobi formula.

2	<u>Hideaki Izumi</u> (Chiba Inst. of Tech.)	Analytic solutions of functional equations associated to translative
	Janusz Matkowski	means
	(Univ. of Zielona Góra)	

Summary: We show the existence of analytic solutions to the functional equation associated with translationinvariant means.

Summary: The quotient-difference (qd) method proposed by Rutishauser in 1954 is known as one of the most important algorithms for computing eigenvalues of a tridiagonal matrix in numerical linear algebra. A solution to the recurrence relation appearing in the qd method can be explicitly expressed by a combination of the Hankel determinants. On the basis of it, the asymptotic analysis of the qd recurrence relation has been already completed in the case where a tridiagonal matrix has no multiple eigenvalues, while it has been not enough in the others. In this talk, we clarify the asymptotic behavior of the determinant solution to the qd recurrence relation in the latter case through reconsidering the formal power series in the Hankel determinants.

Summary: A WKB theoretic transformation that brings a Schrödinger equation to the Weber equation near two simple turning points is well-known. In this talk I present a transformation theory to the Bessel equation in a neighborhood of the Stokes curve of loop type and explain some parts of the proof based on the transformation to the Weber equation.

5 Mika Tanda (Kinki Univ.) Alien derivatives for the Gauss hypergeometric differential equation  $\cdots$  12

Summary: We compute alien derivatives of a WKB solution to the Gauss hypergeometric differential equation with a large parameter. To compute them, we use the singularity structure of the Borel transform of a Voros coefficient of the Gauss equation. The alien derivatives describe parametric Stokes phenomena for the WKB solution.

Summary: To study the monodromy representation of a system of hypergeometric differential equations, we investigate variation of twisted cycles (integral regions) along loops in the complement of the singular locus. We determine the monodromy representation of Lauricella's hypergeometric function  $F_C$ , by using the twisted homology groups associated to an integral representation of Euler type. In this talk, I would like to explain how the monodromy representation of  $F_C$  is expressed.

Summary: In this talk we introduce definitions of uniformly asymptotic boundedness for ordinary differential equations and difference equations and show theorems on equivalence conditions for ultimate boundedness of solutions to the equations. Moreover we discuss the globally uniformly asymptotic stability of the equilibrium point for the modified Nicholson–Bailley model.

Summary: Stability analysis on mathematical models for population dynamics has played a significant role for prediction of eventual disease transmission in a host population and mentenance of species. In particular, construction methods of Lyapunov function(al) have been considered as an important approach in order to obtain global stability of endemic steady states of epidemiological models with delays. In this talk, we establish threshold dynamics for compartmental epidemic models by means of Lyapunov functionals based on the LaSalle's invariance principle and its applications. Furthermore, we offer an example that the endemic equilibrium is destabilized due to a Hopf bifurcation when the incidence rate is given by a class of non-monotone functions.

Summary: The equations considered in this talk is  $x'' + h(t)x' + \omega^2 x = 0$ , where the prime denotes d/dt, the damping coefficient h(t) is continuous and nonnegative for  $t \ge 0$ , and the restoring coefficient  $\omega$  is positive. Our result shows that under the assumption that h(t) is integrally positive, if a certain infinite series obtained from h(t) diverges uniformly, then the equilibrium  $(x(t), x'(t)) \equiv (0, 0)$  is uniformly asymptotically stable.

10 Tetsutaro Shibata (Hiroshima Univ.) S-shaped bifurcation curve for semilinear two-parameter problems · · · · 12

Summary: We consider the nonlinear eigenvalue problem with two-parameters, which was introduced by Crandall and Rabinowitz in 1973 as the typical model which develops S-shaped bifurcation curve  $\lambda = \lambda_{\epsilon}(\alpha)$ . We establish the asymptotic formulas for  $\lambda = \lambda_{\epsilon}(\alpha)$  as  $\alpha \to 0, \alpha_{1,\epsilon}, \alpha_{2,\epsilon}, \beta_{\epsilon}$  when  $0 < \epsilon \ll 1$ , where  $\alpha_{1,\epsilon}$  and  $\alpha_{2,\epsilon}$  are two turning points of  $\lambda_{\epsilon}(\alpha)$ , and  $\beta_{\epsilon}$  is the unique positive solution to the algebraic equation associated with our problem.

Summary: We study the one-dimensional generalized Hénon equation under the Dirichlet boundary condition and prove the existence of at least three positive solutions without the assumption of evenness of the coefficient function.

12 Katsuyuki Nishimoto \* The solutions to the homogeneous Bessel equations by means of the (Descartes Press Co.) N-fractional calculus (The calculus in the 21 th century) (Again) · · · · · 6

Summary: In this article, the solutions to the homogeneous Bessel equations are discussed again without the omitting of the additional arbitrary constants of the integration, which is omitted in the previous our article.

Some one of them is shown as follows, for example.

$$\varphi_{[1](K,M)} = z^{\nu} e^{iz} \{ e^{K} (e^{-i2z} \cdot z^{-(\nu+1/2)})_{\nu-1/2} + M \} (\text{fractional differint egrated form})$$
$$= e^{K} (-i2)^{\nu-1/2} z^{-1/2} e^{-iz} {}_{2}F_{0}(1/2 - \nu, 1/2 + \nu; i/2z) + M z^{\nu} e^{iz}, (|i/2z| < 1)$$

where K and M are the additional arbitrary constants of the integrations, and  ${}_{p}F_{q}(\cdots )$  is the generalized Gauss hypergeometric functions.

 13
 Katsuyuki Nishimoto
 \* The solutions to the nonhomogeneous Bessel equations by means of the (Descartes Press Co.)

 N-fractional calculus operator
 6

Summary: In this article, the solutions to the nonhomogeneous Bessel equations

$$\varphi_2 \cdot z^2 + \varphi_1 \cdot z + \varphi \cdot (z^2 - \nu^2) = f, (z \neq 0)$$
$$(\varphi_\alpha = d^\alpha \varphi / dz^\alpha \text{for}\alpha > 0, \varphi_0 = \varphi = \varphi(z), f = f(z) \neq 0)$$

are discussed by means of the N-fractional calculus operator, omitting the additional arbitrary constants of the integration. To the equations above we have a following particular solution for example.

$$\varphi = \varphi_{[1]}^* = z^{\nu} e^{iz} (G \cdot H)_{\nu - 1/2} (\text{fractional differint egrated form})$$

where

$$G = G(z,\nu,i) = (g \cdot z^{\nu+1/2}e^{i2z})_{-1}, (i = \sqrt{-1}), H = H(z,\nu,i) = z^{-(\nu+1/2)}e^{-i2z}$$

and

$$g = g(f, z, \nu, i) = (f \cdot z^{-(\nu+1)} e^{-iz})_{-(\nu+1/2)} \cdot z^{-1}$$

### 14:15-16:30

Summary: The initial problem of the Schrödinger equations and the Dirac equations are studied with electromagnetic potentials depending on parameters.

It is proved that if electromagnetic potentials are continuous with respect to parameters, so are the solutions and if electromagnetic potentials are differentiable with respect to parameters, so are the solutions.

Summary: The Feynman path integral is a very useful method to study the quantum method and in particular the quantum field theory. The mathematical rigorousness of the Feynman path integral for the Schroedinger equations has been given. On the other hand, it is well known (c.f. the Feynman–Hibbs book) that there is no simple way of expressing the Feynman path integral for the Dirac equations in the physical theory. In this talk the simple and rigorous expression of the Feynman path integral for the Dirac equations is given by means of the phase space path integral.

Summary: We consider the magnetic Schrödinger operator in exterior domain  $\Omega \subset R^2$  with star-shaped boundary with respect to the origin. Under suitable decay and smallness conditions on the magnetic field and external potential, the uniform resolvent estimates are proved. The results are then used to obtain smoothing properties for corresponding evolution equations.

 17
 Fumihiko Hirosawa (Yamaguchi Univ.)
 On second order weakly hyperbolic equations and the ultradifferentiable classes

 Haruhisa Ishida
 classes
 12

 (Univ. of Electro-Comm.)
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Summary: We consider second order weakly hyperbolic equations with time dependent coefficients in the ultradifferentiable classes. Our main purpose is to clarify the relation between the classes of the functions to be well-posed and the following properties of the coefficients: the order of degeneration, stabilization to a monotonic function and their smoothness in the ultradifferentiable classes.

Summary: It is well known that the caloric functions possess the mean value property. In this talk, we prove a generalization of the mean value property for caloric functions on one space dimension. We introduce the notion of polycaloric functions and prove a mean value property for polycaloric functions.

Summary: We investigate the shape of the graph of Newton's potential. It is well-known that Newton's potential satisfies Poisson's equation. In particular, we investigate the uniqueness of a maximum point of Newton's potential. Using geometric argument with the moving plane method, we define the heart of a body and give a sufficient condition for the uniqueness.

Summary: We consider well-posedness of the Cauchy problem for the Chern–Simons–Dirac system in one spatial dimension. Bournaveas, Candy, and Machihara proved that local in time well-posedness in  $H^s(\mathbb{R}) \times H^r(\mathbb{R})$  with  $-1/2 < r \le s \le r+1$ . In this talk, we show well-posedness in  $H^s(\mathbb{R}) \times H^r(\mathbb{R})$  with  $(0 \le s < 1/2)$  and r = -1/2 or  $(s = 0 \text{ and } -1 \le r \le -1/2)$  without the special condition of initial data, in which the flow map fails to be locally uniformly continuous. For the proof, we extract the worst part of nonlinearity and handle separately.

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Summary: In this talk, we prove the local well-posedness of the Cauchy problem of a system of quadratic derivative nonlinear Schrödinger equations with periodic initial data at the scaling critical regularity when  $d \ge 5$  and the coefficients of Laplacian in the system satisfy some condition. The same result for the nonperiodic case was obtained by us. But the same argument as the nonperiodic case cannot be used on the several parts of the proof for the periodic case because the admissible pairs of the Strichartz estimate for the periodic case are less than the nonperiodic case. To overcome this difficulty, we show the new bilinear estimate and use it instead of the Strichartz estimate.

Summary: We consider the Cauchy problem of the Zakharov system, which describes the Langmuir turbulence in a plasma. According to Ginibre, Tsutsumi and Velo, the critical values of (k, l) is ((d-3)/2, (d-4)/2).(k, l) represents the regularity of initial datum for Schrödinger equation and wave equation. We prove small data global well-posedness at the critical space in four and more spatial dimensions by using  $U^2$ ,  $V^2$  type Bourgain space. We note that we cannot get crucial bilinear estimate for the nonlinearity of Schrödinger equation only to apply  $U^2$ ,  $V^2$  spaces. The space-time function space  $L_t^2 L_x^{2d/(d-2)}$  which has Strichartz admissible pair, plays an important role in the bilinear estimate.

Summary: In this talk, we consider the Cauchy problem of the weakly dissipative Camassa–Holm equation. More precisely, we show that the weakly dissipative Camassa–Holm equation is locally well-posed in the critical Besov space and blows-up in the sense of the Sobolev space.

#### 16:45–17:45 Talk invited by Functional Equations Section

Haruya Mizutani (Gakushuin Univ.) On Strichartz estimates for Schrödinger equations with variable coefficients

Summary: We discuss recent progress concerning Strichartz estimates for Schrödinger equations, which measure the size and dispersion of solutions for the Cauchy problem. Such estimates are powerful tools for studying nonlinear Schrödinger equations, and hence have been extensively studied both for Schrödinger equations with potentials and Schrödinger equations with variable coefficients. In this talk, after recalling basic notions of Strichartz estimates, we give a unified approach to a combination of these two kinds of cases. In particular we discuss (1) local-in-time Strichartz estimates for long-range metrics combined with growing electromagnetic potentials; (2) global-in-time Strichartz estimates for long-range metrics.

March 16th (Sun) Conference Room V

#### 9:00-12:00

24	<u>Kazumasa Fujiwara</u> (Waseda Univ.)	Global well-posedness of the Cauchy problem for a semirelativistic
	Shuji Machihara (Saitama Univ.)	system · · · · · · · · · · · · · · · · · · ·
	Tohru Ozawa (Waseda Univ.)	

Summary: We study the global well-posedness of the Cauchy problem for systems of semirelativistic equations with quadratic nonlinearity. The problem is shown to be globally well-posed in  $H^{1/2}$  by a compactness argument. In our proof, the charge conservation law and the energy conservation law are important. From the conservation laws, we have the uniform boundness and uniform Hölder continuity for an approximation sequence for a solution. Then the weak limit of a subsequence of the approximation sequence is shown to be the solution of the Cauchy problem. Moreover the solution is shown to be continuous in time with values in  $H^{1/2}$  with continuous dependence on the initial data

Summary: We prove the global existence of analytic solutions to nonlinear Schrödinger equation with quintic nonlinearity in n space dimensions for sufficiently small Cauchy data with exponential decay.

Summary: We consider the transverse instability for a nonlinear Schrödinger equation on  $\mathbb{R} \times \mathbb{T}_L$ , where  $2\pi L$  is a period of the torus  $\mathbb{T}_L$ . There exists a critical period  $L_*$  such that the line standing wave is stable for  $L < L_*$  and the line standing wave is unstable for  $L > L_*$ . In this talk, we farther consider the stability for the boundary  $L = L_*$  between the stability and the instability for line standing waves of the nonlinear Schrödinger equation.

27	Kota Uriya	(Tohoku Univ.)*	Final state	problem	for a	system	of qu	uadratic	$\operatorname{nonlinear}$	Schrödinger	
	Takayoshi Ogawa	(Tohoku Univ.)	equations ·								10

Summary: We consider the final state problem for a system of quadratic nonlinear Schrödinger equations with mass resonance condition. It is known that quadratic nonlinearities are critical between existence and non-existence of asymptotic free solutions. We construct a new modification to show the existence of a solution to the problem. More precisely, we show the behavior of solution which describes that mass of the first component of solution decay to 0 and the second component of solution obtains total mass of the solution.

28 Toshiyuki Suzuki (Tokyo Univ. of Sci.) Blowup for Hartree type equations with inverse-square potentials .... 12

Summary: We consider the blowup in finite time for Hartree type equations (nonlinear Schrödinger equations of nonlocal nonlinearity) with inverse-square potentials  $(\mathbf{HE})_a$  by applying the Glassey method. Key of his method is virial identity. But the identity for  $(\mathbf{HE})_a$  has not proved in consequence of the strongly singular potential  $a|x|^{-2}$ . Thus we give a strict proof of the identity.

Summary: Ibrahim, Masmoudi and Nakanishi classified scattering solutions and blow-up ones for subcritical Klein–Gordon equation with real valued data. We extend this result to complex valued data. In detail, we classify them for cubic Klein–Gordon equation in 3-dimension with complex valued data. Since blow-up result was obtained by Ohta and Todorova, we prove scattering result. This proof is based on the method of Ibrahim, Masmoudi and Nakanishi.

Summary: We consider the linear wave equation with space-dependent damping. Todorova and Yordanov (2009) introduced a weighted energy method and showed that the decay rate of the energy of solutions coincides with that of the corresponding heat equation. In this talk, we give an extension of their result to estimates of higher order derivatives and show that the asymptotic profile of the solution is given by a solution of the corresponding heat equation.

31 Kosuke Ono (Univ. of Tokushima)<sup>\*</sup> Global existence and decay estimates for mildly degenerate Kirchhoff type dissipative wave equations to the Cauchy problem ..... 12

Summary: We consider the global existence and decay estimates of solutions to the Cauchy problem for mildly degenerate dissipative wave equations of Kirchhoff type. In the case that the exponent of the nonlocal term is small, we derive the decay rates of the solutions by using several identities.

Summary: We study the scattering problem of the wave equation of a Hartree type with small initial data with slow decay. We give the sharp conditions needed to define the scattering operator by showing scattering and no scattering results.

Summary: We consider the global solvability to the Cauchy problem of Kirchhoff equation in some special classes of non-analytic functions, which are extensions of Manfrin's class in [Manfrin (JDE2005)] and [Hirosawa (JDE2006)].

Summary: We consider the Cauchy problem for the generalized Ostrovsky–Hunter equation. Time decay estimate of solutions to linear problem was studied. However it is not known that the estimate is sharp or not. We give a sufficient condition which implies the time decay estimate is sharp and as an application of the result we prove non existence of the usual scattering states of the generalized Ostrovsky–Hunter equation.

### 13:15–14:15 Award Lecture for 2013 Analysis Prize

Yoshihiro Tonegawa (Hokkaido Univ.) On the regularity theory for mean curvature flow

Summary: Brakke defined a notion of mean curvature flow valid for non-smooth surfaces. I explain the definition and related existence results as well as our recent partial regularity theorem and  $\varepsilon$ -regularity theorem.

March 17th (Mon) Conference Room V

### 9:00-12:00

Summary: We consider a solution of a Cauchy problem for a semilinear heat equation with an absorption. The initial datum of the problem is bounded and its infimum is more than zero. We study the solution which does not vanish in the total space at the vanishing time. It does only at space infinity.

37 Toshikazu Kuniya (Univ. of Tokyo) Invariance principle and Lyapunov functional for the asymptotic analysis of nonlinear partial differential equations with age variable ..... 12

Summary: In this talk, we are concerned with the asymptotic analysis of some biological models expressed as nonlinear partial differential equations including age variable. In the analysis, the invariance principle combined with some Lyapunov functionals plays an important role. In particular, the necessity of showing the relative compactness of orbits in an infinite dimensional Banach space occurs. We will focus on some recent results obtained by using the invariance principle.

38 Tadashi Kawanago (Tokyo Tech) The Hopf bifurcation theorem for semilinear equations ..... 12

Summary: We established the Hopf bifurcation theorem for abstract semilinear equations, which gives a criterion for the Hopf bifurcation to occur. We may consider it as an improvement of the theorem established by Crandall and Rabinowitz at 1977. Our theorem can be proved by the codimension-m bifurcation theorem established recently by the author.

39Sachiko Ishida (Tokyo Univ. of Sci.)Boundedness of solutions to quasilinear degenerate Keller–Segel systems<br/>of parabolic-parabolic type on non-convex domains39Sachiko Ishida (Tokyo Univ. of Sci.)Boundedness of solutions to quasilinear degenerate Keller–Segel systems<br/>of parabolic-parabolic type on non-convex domains39Tomomi Yokota (Tokyo Univ. of Sci.)Boundedness of solutions to quasilinear degenerate Keller–Segel systems<br/>of parabolic-parabolic type on non-convex domains

Summary: This talk is concerned with quasilinear degenerate Keller–Segel systems of parabolic-parabolic type on non-convex bounded domains. The uniform-in-time boundedness of weak solutions is established under the subcritical condition. The result is a degenerate diffusion and non-convex domain version of the recent result by Tao and Winkler (2012).

Summary: This talk deals with parabolic-elliptic chemotaxis systems with the sensitivity function  $\chi(v)$  and the growth term f(u) under homogeneous Neumann boundary conditions in a smooth bounded domain. Here it is assumed that  $0 < \chi(v) \le \frac{\chi_0}{v^k}$   $(k \ge 1, \chi_0 > 0)$  and  $\lambda_1 - \mu_1 u \le f(u) \le \lambda_2 - \mu_2 u$   $(\lambda_1, \lambda_2, \mu_1, \mu_2 > 0)$ . It is shown that if  $\chi_0$  is sufficiently small, then the system has a unique global-in-time classical solution that is uniformly bounded.

 41
 Yoshiyuki Kagei (Kyushu Univ.)
 Uniqueness theorem on weak solutions to the Keller–Segel system of degenerate and singular types

 41
 Yoshie Sugiyama (Kyushu Univ.)
 Uniqueness theorem on weak solutions to the Keller–Segel system of degenerate and singular types

Summary: The uniqueness of weak solutions to the Keller–Segel systems of degenerate and singular types is proved in the class of Hölder continuous functions. Hölder continuity is expected to be an optimal regularity for weak solutions of the degenerate Keller–Segel systems under consideration. Our proof for the uniqueness result is based on the vanishing viscosity duality method.

42	Yoshie Sugiyama (Kyushu Univ.)	Global	solutions	to a	chemo	taxis	system	with	non-	diffusive	memory	
	Youhei Tsutsui											12
	(Waseda Univ./Osaka City Univ.)											
	Juan J. L. Velázquez (Univ. Bonn)											

Summary: In this talk, we give a small data global existence theorem for a chemotaxis system on the whole space. Our system consists of a chemotaxis equation with a logarithmic term and an ordinary equation without diffusion term.

43 Yoshihisa Morita (Ryukoku Univ.) A reaction-diffusion system with mass conservation · · · · · · 10 <u>Takashi Suzuki</u> (Osaka Univ.)

Summary: We study global-in-time behavior of the solution to a reaction diffusion system with mass conservation proposed in the study of cell polarity. First, we have global-in-time solution with compact orbit and then examine stability and instability of stationary solutions.

Summary: We consider two fast diffusion equations  $\partial_t u = \operatorname{div}(|\nabla u|^{p-2}\nabla u)$  and  $\partial_t u = \Delta u^m$ , where 1and <math>0 < m < 1. Let  $\Omega$  be a domain in  $\mathbb{R}^N$  with  $N \ge 2$ , and let u = u(x,t) be the solution of the initialboundary value problem over  $\Omega$ , where the initial value equals zero and the boundary value is positive. Choose an open ball B in  $\Omega$  whose closure intersects  $\partial\Omega$  only at one point. Then, we derive an asymptotic formula for the integral of some positive power of u over B for short times in terms of principal curvatures of  $\partial\Omega$  at the point, which tells us about the interaction between fast diffusion and geometry of domain. The Cauchy problem is also dealt with.

Norihisa Ikoma (Tohoku Univ.)*	Singular perturbation problems for the Kirchhoff type equations with	
Giovany M. Figueiredo	general nonlinearities · · · · · · · · · · · · · · · · · · ·	12
(Univ. Federal do Pará)		
João R. Santos Junior		
(Univ. Federal do Pará $)$		
	Norihisa Ikoma (Tohoku Univ.)* Giovany M. Figueiredo (Univ. Federal do Pará) João R. Santos Junior (Univ. Federal do Pará)	Norihisa Ikoma       (Tohoku Univ.)*       Singular perturbation problems for the Kirchhoff type equations with general nonlinearities         Giovany M. Figueiredo       general nonlinearities       general nonlinearities         (Univ. Federal do Pará)       João R. Santos Junior       (Univ. Federal do Pará)

Summary: This talk is devoted to the study of the Kirchhoff type equations with potential functions and general nonlinearies. We show the existence of a family of positive solutions which concentrates (up to subsequence) around local minimum points of the potential functions.

46	<u>Norihisa Ikoma</u>	(Tohoku Univ.)*	genvalue problems for ful	ly nonlinear second-order	elliptic PDE on
	Hitoshi Ishii	(Waseda Univ.)	alls		$\cdots \cdots \cdots 12$

Summary: This talk concerns the eigenvalue problems for fully nonlinear second-order elliptic operators on intervals or balls. We prove the existence of sequences of eigenvalues and (radially symmetric) eigenfunctions under various types of boundary conditions. We also show that there is no eigenvalue and (radially symmetric) eigenfunction other than those we find.

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Summary: We investigate the Kirchhff type elliptic boundary value problems in dimension four. In particular we consider the critical case and show the existence of solutions of those. Our method is based on the variational method and the concentration compactness argument for the PS sequences.

Summary: We consider second order linear elliptic equations  $-\operatorname{div}(A(x)\nabla u) + b(x) \cdot \nabla u = 0$  with a strongly singular vector field b. We prove a subsolution estimate and a weak Harnack inequality for weak supersolutions under certain assumptions on b which are best possible in some sense.

#### 14:15-16:15

### 49 Kousuke Kuto (Univ. of Electro-Comm.) Limiting structure of steady-states to the Lotka–Volterra competition model with large diffusion and advection Tohru Tsujikawa (Univ. of Miyazaki) model with large diffusion and advection

Summary: This talk is concerned with the Neumann problem of a stationary Lotka–Volterra competition model with diffusion and advection. First we introduce a limiting system as diffusion and advection of one of the species tend to infinity. The limiting system can be reduced to a semilinear elliptic equation with nonlocal constraint. Next we obtain the bifurcation structure of nonconstant solutions to the limiting system in the simplified 1D case. This structure involves a simple curve of nonconstant solutions which connects two different singularly perturbed states (boundary layer solutions and internal layer solutions).

Summary: In this talk we investigate a semilinear elliptic equation with a logistic nonlinearity and an indefinite nonlinear boundary condition, both depending on a parameter  $\lambda$ . Based on variational and bifurcation techniques, our main results establish the existence of *three* nontrivial non-negative solutions for some values of  $\lambda$ , as well as their asymptotic behavior. These results suggest that the positive solution set contains an *S*-shaped component in some case, as well as a combination of a *C*-shaped and a *S*-shaped components in another case.

Yasuhito Miyamoto (Univ. of Tokyo) Structure of the positive radial solutions for elliptic equations with exponential growth ..... 12

Summary: Let  $B \subset \mathbb{R}^N$ ,  $N \geq 3$ , be the unit ball. We study the global bifurcation diagram of the solutions of

$$\begin{cases} \Delta u + \lambda f(u) = 0 & \text{in } B, \\ u = 0 & \text{on } \partial B, \\ u > 0 & \text{in } B, \end{cases}$$

where  $f(u) = e^u + g(u)$  and g(u) is a lower order term. The solution set is a curve C parametrized by the  $L^{\infty}$ -norm of the solution. We show that this problem has the singular solution  $(\lambda^*, u^*)$  and that the curve C has infinitely many turning points around  $\lambda^*$  if  $3 \leq N \leq 9$ . We show that under a certain condition on g the curve C has no turning point if  $N \geq 10$ . We also study the Morse index of  $u^*$ .

## 52 Shinji Adachi (Shizuoka Univ.)\* Uniqueness and non-degeneracy of positive radial solutions for quasilin-<u>Tatsuya Watanabe</u> ear elliptic equations with exponential nonlinearity ..... 12 (Kyoto Sangyo Univ.)

Summary: We are concerned with the uniqueness and non-degeneracy result of positive solutions for a class of quasilinear elliptic equation with exponential nonlinearity. We convert a quasilinear elliptic equation into a semilinear one and study precise correspondences between two equations. We show the uniqueness and the non-degeneracy of positive solutions by analyzing the converted semilinear problem.

53	Francesca Gladiali	On the number of peaks of the eigenfunctions of the linearized Gel'fand	
	(Univ. degli Studi di Sassari)	problem ·····	12
	Massimo Grossi		
	(Univ. di Roma "La Sapienza")		
	<u>Hiroshi Ohtsuka</u> (Kanazawa Univ.)		

Summary: We derive a second order estimate for the first m eigenvalues of the linearized Gel'fand problem associated to solutions which blow-up at m points. This allows us to determine, in some suitable situations, some qualitative properties of the first m eigenfunctions as the number of points of concentration.

Summary: We study the uniqueness of positive radial solutions of  $\Delta u + \nabla \rho \nabla u / \rho - gu + hu^p = 0$ . We also study its nondegeneracy in an appropriate function space.

Summary: Consider the Liouville–Gelfand type problems with nonlinear Neumann boundary conditions on a smooth bounded domain, with a smooth, strictly positive, convex, increasing nonlinearity which is superlinear at  $+\infty$ . In this talk, after introducing a suitable notion of weak solutions, we prove several properties of so-called extremal solutions of the problem.

Summary: We consider the Liouville–Gelfand type elliptic problem with nonlinear Neumann boundary conditions, the nonlinearity of which is a smooth, strictly positive, convex, increasing function, and is superlinear at infinity. We study the spectral properties of the socalled extremal weak solution and show a phenomenon of weak continuum spectrum for the corresponding linearized eigenvalue problem.

#### 16:30–17:30 Talk invited by Functional Equations Section

Atsushi Tachikawa (Tokyo Univ. of Sci.) On the regularity of p(x)-harmonic maps

Summary: In this talk we discuss the regularity of minimizers for p(x)-growth functionals with special structures.

Let  $\Omega \subset \mathbb{R}^m$   $(m \ge 2)$  be a bounded open set, For maps  $u : \Omega \to \mathbb{R}^n$  we consider the p(x)-energy functional defined as

$$\mathcal{E}(u;\Omega) := \int_{\Omega} \left( g^{\alpha\beta}(x) h_{ij}(u) D_{\alpha} u^{i}(x) D_{\beta} u^{j}(x) \right)^{p(x)/2} dx,$$

where  $(g^{\alpha\beta}(x))$  and  $(h_{ij}(u))$  are symmetric positive definite matrices whose entries are Hölder continuous functions defined on  $\Omega$  and  $\mathbb{R}^n$  respectively, and p(x) a Hölder continuous function on  $\Omega$  with  $p(x) \geq 2$ . We assume that  $(g^{\alpha\beta}(x))$  and  $(h_{ij}(u))$  satisfy, for some positive constants  $\lambda_g \leq \Lambda_g$  and  $\lambda_h \leq \Lambda_h$ ,

$$\begin{split} \lambda_g |\xi|^2 &\leq g^{\alpha\beta}(x)\xi_\alpha\xi_\beta \leq \Lambda_g |\xi|^2, \quad \forall (x,\xi) \in \Omega \times \mathbb{R}^m, \\ \lambda_h |\eta|^2 &\leq h_{ij}(u)\eta^i \eta^j \leq \Lambda_h |\eta|^2 \quad \forall (u,\eta) \in \mathbb{R}^n \times \mathbb{R}^n. \end{split}$$

For a local minimizer u, we show that  $u \in C^{1,\alpha}(\Omega_0)$  for some  $\alpha \in (0,1)$  and an open set  $\Omega_0 \subset \Omega$  with  $\dim^{\mathcal{H}}(\Omega \setminus \Omega_0) < m - \inf p(x)$ , where  $\dim^{\mathcal{H}}$  stands for the Hausdorff dimension. If p(x) is Lipschitz continuous and u is bounded, then we can improve the estimate for the Hausdorff dimension of the singular set of u. Moreover, if  $h_{ij}(u)$  satisfies the so-called *one sided condition*;

$$-\frac{1}{2}u^k\frac{\partial h_{ij}(u)}{\partial u^k}\xi^i\xi^j \le \lambda_h^*|\xi|^2 \quad \forall (u,\xi) \in \mathbb{R}^n \times \mathbb{R}^n \quad \text{for } \lambda_h^* < \lambda_h,$$

then u enjoys full interior regularity.

March 18th (Tue) Conference Room V

### 9:00 - 12:00

Summary: In this talk, we consider the uniqueness of symmetric weak solutions to the stationary Navier– Stokes equation in a two-dimensional exterior domain  $\Omega$ . It is known that, under suitable symmetry condition on the domain and the data, the problem admits at least one symmetric weak solution tending to zero at infinity. Given two symmetric weak solutions u and v, we show that if u satisfies the energy inequality  $\|\nabla u\|_{L^2(\Omega)}^2 \leq (f, u)$  and  $\sup_{x \in \Omega} (|x| + 1)|v(x)|$  is sufficiently small, then u = v. The proof relies upon a density property for the solenoidal vector field and the Hardy inequality for symmetric functions.

Summary: We consider the Hadamard variational formula for the Green function of the Stokes equations on the bounded domain with the smooth boundary. Under the perturbation with preserving its volume and keeping its topological type, we establish a more refined proof of its formula of the Green function not only for the first variation but also the second variation for both velocity and pressure. Our method gives a new systematic proof of the Hadamard variational formula, which enables us to deal with the higher derivatives with respect to the perturbation of domains.

 59
 Hiroki Ueno
 (Keio Univ.)
 On the thin film approximation for the flow of a viscous incompressible

 Akinori Shiraishi
 fluid down an inclined plane
 12

 Tatsuo Iguchi
 (Keio Univ.)
 12

Summary: We consider a two-dimensional motion of liquid film of a viscous and incompressible fluid flowing down an inclined plane under the influence of the gravity and the surface tension on the surface. The problem is mathematically formulated as a free boundary problem for the Navier–Stokes equations. Our purpose is to give a mathematically rigorous justification of a thin film approximation by establishing the error estimate between the solution of the Navier–Stokes equations and that of approximate equations. In this talk, we report that under smallness assumptions on the Reynolds number, the angle of inclination, and the initial fluctuation the solution of the initial value problem for the Navier–Stokes equations satisfies uniform estimates with respect to a thin film parameter.

Summary: We consider the zero-resistivity limit for linearized Hasegawa–Wakatani equations in a cylindrical domain when the initial data are Stepanov-almost-periodic to the axial direction. Hasegawa–Wakatani equations describes the resistive drift wave turbulence. We prove that the Stepanov-almost-periodic solution of linearized Hasegawa–Wakatani equations converges to that of linearized Hasegawa–Mima like equation as the resistivity tends to zero.

61 Masahiro Suzuki (Tokyo Tech)\* Stationary solutions to the equation for a multicomponent plasma  $\cdots$  12

Summary: In this talk, we study a boundary layer, called a sheath, which occurs on the surface of materials with which a multicomponent plasma contacts. For the sheath formation, the generalized Bohm criterion demands that the ions enter the sheath region with a high velocity. The motion of the multicomponent plasma is governed by the Euler–Poisson equations. The sheath is mathematically understood as the stationary solution to the equations. We show the unique existence and the asymptotic stability of the stationary solution under the the generalized Bohm criterion.

62 Masashi Ohnawa (Waseda Univ.) Asymptotic stability of strong traveling waves for a radiating gas model

Summary: We study asymptotic behaviors of perturbations around sufficiently strong shock waves to the Hamer model system of a radiating gas. We obtain global solutions for small initial perturbations and show that they converge uniformly to traveling waves. As a corollary, all super critical shock waves are asymptotically stable to small odd initial perturbations. This work extends previous results by the author on the stability of subcritical shock waves and instability of a critical shock wave and gives a new characterization of the patterns of traveling waves obtained using phase plane analysis.

63 Natsumi Yoshida (Osaka Univ.) Global asymptotic stability of a multiwave pattern for the scalar conservation law with degenerate flux and viscosity · · · · · · · · · · 12

Summary: We study the asymptotic behavior of solutions toward a multiwave pattern (rarefaction wave and viscous contact wave) of the Cauchy problem for one-dimensional viscous conservation law where the far field states are prescribed.

Especially, we deal with the case when the flux function is convex or concave but linearly degenerate on some interval, and also the viscosity is a nonlinearly degenerate one.

The most important thing for the proof is how to obtain the a priori energy estimates.

Summary: We are concerned with the convergence rates of the global strong solution to motionless state with constant density for the compressible Navier–Stokes equations in the whole space  $\mathbb{R}^n$  for  $n \geq 2$ . It is proved that the perturbations decay in critical spaces, if the initial perturbations of density and velocity are small in  $\dot{B}_{2,1}^{\frac{n}{2}}(\mathbb{R}^n) \cap \dot{B}_{1,\infty}^0(\mathbb{R}^n)$  and  $\dot{B}_{2,1}^{\frac{n}{2}-1}(\mathbb{R}^n) \cap \dot{B}_{1,\infty}^0(\mathbb{R}^n)$ , respectively.

Summary: In this talk, we consider the asymptotic stability of the spatial inhomogeneous Navier–Stokes– Boussinesq system with general nonlinearity including both power nonlinear terms and convective terms. We apply an energy inequality and some assumptions to derive the stability of energy solutions of our system.

Summary: We consider the Cauchy problem for the critical Burgers equation in the Besov spaces. We show that the unique global solutions exist for small initial data in  $\dot{B}^0_{\infty,1}(\mathbb{R}^n)$ . We also consider the large time behavior of the solutions for initial data in  $L^1(\mathbb{R}^n) \cap \dot{B}^0_{\infty,1}(\mathbb{R}^n)$  to show that the solutions behave like the Poisson kernel.

Summary: We consider the space-time behavior of the two dimensional Navier–Stokes flow. Carpio, Fujigaki– Miyakawa, and Miyakawa–Schonbek showed the asymptotic expansion and the energy decay of the Navier– Stokes flow under the moment condition on initial data. In this paper, without any moment condition on the initial data, we derive the asymptotic expansion. Moreover, for the critical decay rate, the necessary and sufficient condition on initial data as in Miyakawa–Schonbek is concerned.

### 14:15-15:15

 68
 Takayuki Kubo (Univ. of Tsukuba)
 On the R-boundedness of solution operators for the compressible-compressible two phase problem

 68
 Takayuki Kubo (Univ. of Tsukuba)
 On the R-boundedness of solution operators for the compressible-compressible two phase problem

 70
 Kohei Soga (CNRS-ENS Lyon)
 The R-boundedness of solution operators for the compressible two phase problem

Summary: In this talk, we will consider the model problem for the two phase problem in cases of compressiblecompressible fluid flows without surface tension. In order to prove the local in time existence of this problem, the generation of analytic semigroup for linearlized problem and its maximal  $L_p - L_q$  regularity are needed in our method. The key step of our method is to prove the existence of  $\mathcal{R}$ -bounded solution operator to the generalized resolvent problem corresponding the linearized problem. In this talk, we will report  $\mathcal{R}$ -boundedness for solution operator.

 $\begin{array}{ll} 69 \quad \mbox{Yoshihiro Shibata (Waseda Univ.)} & \mathcal{R}\mbox{-bounded solution operators for the Stokes equations with free bound-ary condition and its application, Incompressible case \cdots 10 \end{array}$ 

Summary: I would like to talk about the existence of  $\mathcal{R}$  bounded solution operators for the Stokes equations with free boundary condition, which combined with Weis' operator valued Fourier multiplier theorem furnishes the generation of analytic semigroup and maximal  $L_p$ - $L_q$  regularity of the time dependent problem. Moreover, as an application, I will talk about a local in time unique existence theorem for some free boundary problem of the Navier–Stokes equations in a uniform  $W_q^{2-1/q}$  domain in  $\mathbb{R}^N$  without surface tension.

 

 70
 <u>Yoshihiro Shibata</u> (Waseda Univ.)
 *R*-bounded solution operators for the Stokes equations with free boundary condition and its application, Compressible case

 70
 <u>Yuko Enomoto</u> (Shibaura Inst. of Tech.)
 *R*-bounded solution operators for the Stokes equations with free boundary condition and its application, Compressible case

Summary: I would like to talk about the existence  $\mathcal{R}$ -bounded solution operators for the Stokes equations with free boundary condition arising from some free boundary problem of compressible barotropic viscous fluid flows without surface tension in a uniform  $W_q^{2-1/q}$  domain. As an application, we have the generation of analytic semigroup and maximal  $L_p$ - $L_q$  regularity theorem for the time dependent problem. And also, we have a local in time unique existence theorem in any uniform  $W_q^{2-1/q}$  domain and a global in time unique existence theorem for some initial data closed to trivial state in a bounded domain.

71 Yoshihiro Shibata (Waseda Univ.) On a global in time unique existence theorem for some free boundary problem of the Navier–Stokes equations without surface tension · · · · · 10

Summary: I would like to talk about a global in time unique existence theorem for some free boundary problem of the Navier–Stokes equations without surface tension in a bounded domain in  $\mathbb{R}^N$ , whose boundary is a hypersurface of  $W_q^{2-1/q}$  class initially. The result was obtained by Prof. Solonnikov: Math. USSR Izvestiya 31 (1988), 381–405. Since he proved maximal regularity only for local in time, his argument is rather complicated to show the prolongation of local in time solutions. But, I proved some exponential decay estimate of solutions to the linearized problem, and my prolongation argument relies on this decay theorem, which makes the argument rather simpler than Prof. Solinnikov's one.

Summary: In this talk, we consider the motion of viscous compressible barotropic fluid in a uniform  $W_q^{3-1/q}$  domain  $\Omega \subset \mathbb{R}^N$   $(2 \leq N < q < \infty)$  with boundary  $\Gamma$ . Our purpose is a local in time unique existence of solutions in the  $L_p$  in time and  $L_q$  in space framework with  $2 , <math>N < q < \infty$ .

### 15:30–16:30 Talk invited by Functional Equations Section

Takeshi Wada (Kumamoto Univ.) Smoothing effects and global well-posedness of Maxwell–Schrödinger equations

Summary: In this talk, we consider the Maxwell–Schräingier equations in  $\mathbb{R}^{1+n}$ . This system describes the time evolution of the interaction between a charged particle and electro-magnetic field generated by the motion of this particle. We mainly aim at showing the well-posedness of this system in low regularity Sobolev spaces. To do this, we need some smoothing estimates of Kato type for magnetic Schrödingier equations with low regularity potentials and Koch–Tzvetkov type estimates, which are some modification of Strichartz type estimates. Applying such estimates together with modified Strichartz estimates for wave equations, we prove global well-posedness of Maxwell–Schräingier equations for  $n \leq 3$ .

# **Real Analysis**

March 17th (Mon)

Conference Room III

### 9:00-12:05

1 Yukino Tomizawa (Chuo Univ.) Non-Lipschitzian mappings with respect to the Bregman distance · · · · 15

Summary: In this lecture, we introduce new extension of asymptotically quasi-nonexpansive mappings in the intermediate sense with respect to the Bregman distance. The extension mapping is not Lipschitz continuous. We can have the following results: In certain conditions, the set of fixed points of the extension mapping is closed and convex. Moreover, we have a strong convergence theorem of the shrinking projection method for finding a fixed point of the extension mapping in real reflexive Banach spaces. These results are extension of results of asymptotically quasi-nonexpansive mappings in the intermediate sense with respect to particular distance-like functions.

Summary: In this talk, we consider the variational inequality problem for a countable family of inversestrongly-monotone mappings in a Hilbert space. Then we provide an iterative algorithm to find a solution of this problem. Moreover, we also establish strong convergence theorems for the variational inequality problem for an inverse-strongly-monotone mapping and the zero point problem for a maximal monotone operator.

3 Ryotaro Tanaka (Niigata Univ.) A geometric approach to two-dimensional Tingley's problem ..... 15

Summary: Tingley's problem, also known as the isometric extension problem, has been studied by many mathematicians since 1987. In this talk, we propose a new geometric approach to two-dimensional Tingley's problem.

4 <u>Kenichi Mitani</u> (Okayama Pref. Univ.) James constant of two dimensional Lorentz sequence space and its dual Kichi-Suke Saito (Niigata Univ.) IS Ryotaro Tanaka (Niigata Univ.)

Summary: The James constant of a Banach space was introduced by Gao and Lau. In this talk we present some recent results on James constant of 2-dimensional Lorentz sequence space and its dual space.

Summary: Mitani and Saito introduced and studied a geometric constant  $\gamma_{X,\psi}$  of a Banach space X, by using the notion of  $\psi$ -ditect sum. For  $t \in [0, 1]$ , the constant  $\gamma_{X,\psi}(t)$  is defined as a supremum taken over all elements in the unit sphere of X. We obtain that, for a Banach space with a predual Banach space, the supremum can be taken over all extreme points of the unit ball.

6	Toshikazu Watanabe (Niigata Univ.)	Fixed point theorem for set-valued Kannan mappings with a vector-
	Masashi Toyoda (Tamagawa Univ.)	valued distance · · · · · · 15

Summary: In this talk, we consider fixed point theorems for set-valued Kannan mappings using v-distances.

 $\frac{\text{Toshiharu Ikeda}}{\text{Mikio Kato}} \begin{array}{l} \text{(Kyushu Inst. of Tech.)} & \text{On von Neumann-Jordan and James constants for absolute norms on} \\ \mathbb{R}^2 & \cdots & 15 \end{array}$ 

Summary: Let  $\|\cdot\|_{\psi}$  be the absolute norm on  $\mathbb{R}^2$  corresponding to a convex function  $\psi$  on [0,1] and  $C_{\mathrm{NJ}}(\|\cdot\|_{\psi})$  its von Neumann–Jordan constant. It is known that  $\max\{M_1^2, M_2^2\} \leq C_{\mathrm{NJ}}(\|\cdot\|_{\psi}) \leq M_1^2 M_2^2$ , where  $M_1 = \max_{0 \leq t \leq 1} \psi(t)/\psi_2(t)$ ,  $M_2 = \max_{0 \leq t \leq 1} \psi_2(t)/\psi(t)$  and  $\psi_2$  is the corresponding function to the  $\ell_2$ -norm. In this talk, we shall discuss equality-attainedness of the above inequalities. In particular we shall present a characterization for the the right inequality to attain equality. Similar results for the James constant will be presented.

8 Sachiko Atsushiba (Univ. of Yamanashi) Strong convergence theorems for nonlinear mappings by iterative schemes

Summary: In this talk, we study common attractive points and prove convergence theorems for nonlinear mappings. We also prove strong convergence theorems for nonexpansive semigroups by some iterative schemes. Using these results, we obtain new and well-known convergence theorems.

Summary: The class of non-atomic finite measure spaces with the saturation property, as developed in Maharam (1942) and Hoover–Keisler (1984), is characterized by the Fatou (and Lebesgue) property of a well-dominated sequence of multifunctions taking values in a Banach space. With multifunctions reduced to functions, this Fatou characterization also extends to a variant of the closure property found in optimal control theory. The results are developed through a considered overview of the relevant literature on the exact and approximate Fatou lemma phrased in terms of Bochner integration.

10 Yoichi Miyazaki (Nihon Univ.)\* Introduction to complex interpolation between Sobolev spaces ..... 15

Summary: We give a simple proof of the theorem on complex interpolation between  $L_p$ -based Sobolev spaces of integral order, using Muramatu's first integral formula. Muramatu proved the theorem for Sobolev spaces of fractional order by Muramatu's second integral formula. He characterized a Sobolev function in terms of its regularization and reduced the problem to finding the complex interpolation between weighted  $L_p(L_2)$ spaces. Compared to Muramatu's method, ours is straightforward.

11Yōhei YamasakiThe commutation of limit and singular integral, avoiding the dominating<br/>functions15

Summary: This talk give examples to treat the commutation of limit and singular integral of primitive functions in plural variables. The result is frequently commutative, but in some cases it fails.

### 14:15 - 16:25

12	<u>Toshiharu Kawasaki</u> (Nihon Univ.)	Criteria for the C-integral · · · · · · · · · · · · · · · · · · ·	j
	Shizu Nakanishi (Osaka Pref. Univ.)		
	Ichiro Suzuki (Nihon Bunka Univ.)		

Summary: We will give new criteria for the C-integral.

13Takanori Yamamoto\*Majorization of singular integral operators with Cauchy kernel on  $L^2$ <br/>(Hokkai-Gakuen Univ.)\*Majorization of singular integral operators with Cauchy kernel on  $L^2$ 

Summary: Let a, b, c and d be functions in  $L^2 = L^2(\mathbb{T}, d\theta/2\pi)$ , where  $\mathbb{T}$  denotes the unit circle. Let  $\mathcal{P}$  denote the set of all trigonometric polynomials. Suppose the singular integral operators A and B are defined by A = aP + bQ and B = cP + dQ on  $\mathcal{P}$ , where P is an analytic projection and Q = I - P is a co-analytic projection. In this paper, we use the Helson–Szegő type set (HS)(r) to establish the condition of a, b, c and d satisfying  $||Af||_2 \geq ||Bf||_2$  for all f in  $\mathcal{P}$ . If a, b, c and d are bounded measurable functions, then A and Bare bounded operators, and this is equivalent to that B is majorized by A on  $L^2$ , i.e.,  $A^*A \geq B^*B$  on  $L^2$ . Applications are then presented for the majorization of singular integral operators on weighted  $L^2$  spaces.

Hiroshi Sato (Kyushu Univ.\*)

Summary: The notion of the linear quasi-metric is introduced. If a linear space admits a translation invariant linear quasi-metric, then it becomes a topological linear space. The main interest is the linear topology of the Shepp space which is studied systematically as a linear quasi-metric topology. The linear quasi-metric topologies on the approximation spaces of the Shepp space are also considered.

Summary: We determined optimal inclusion relations between  $L^p$ -Sobolev and Wiener amalgam spaces. As an application we discuss mapping properties of unimodular Fourier operators  $e^{i|D|^{\alpha}}$  between  $L^p$ -Sobolev and Wiener amalgam spaces.

Summary: We show several properties of BLO martingales. In particular, we give a new characterization of BLO martingales.

Summary: Around thirty years ago, block spaces, which are the predual of Morrey spaces, had been considered. However, it seems that there is no proof that block spaces satisfy the Fatou property. In this talk the Fatou property for block spaces is verified and the predual of block spaces is characterized.

#### 56 Real Analysis

Summary: We have investigated a kind of generalization of the Shannon's sampling theorem, i.e.  $\mathbb{R}, \mathbb{Z}$  are replaced respectively by  $\mathbb{R}^2, X$ , where X consists of (irregularly) scattered countably infinite points of  $\mathbb{R}^2$ . We shall show that under suitable conditions, a robust interpolation formula is provided by means of a linear combination of a suitable positive definite functions. Moreover, an error estimate by the Besov norm will be given whose proof is reduced to the case of the regular lattice.

 19
 <u>Hiroki Saito</u> (Tokyo Metro. Univ.)
 Boundedness of the Kakeya maximal operators on the variable Lebesgue

 Hitoshi Tanaka (Univ. of Tokyo)
 spaces
 15

Summary: In this talk, we shall verify the Kakeya (Nikodym) maximal operator  $K_N$  is bounded on the variable Lebesgue space  $L^{p(\cdot)}(\mathbb{R}^2)$  whenever the exponent function  $p(\cdot)$  satisfies log-Hölder continuity conditions.

### 16:45–17:45 Talk invited by Real Analysis Section

Mitsuo Izuki (Tokyo Denki Univ.) A real analytic study of various function spaces with variable exponent

Summary: The aim of this talk is to introduce some recent results on function spaces with variable exponent in terms of real analysis. The main result consists of wavelet application to variable function spaces and generalization of the BMO norm using variable exponent.

If we use wavelets with proper decay and smoothness, then we can characterize and get bases of various function spaces. Recently approximation theory with bases given by wavelets is applied and marked in many areas, for example image analysis, signal analysis, statistical estimation and numerical analysis of partial differential equations. We discuss wavelet characterization and construction of bases of function spaces with variable exponent. Additionally we state modular inequalities arising from wavelets on Lebesgue spaces with variable exponent.

The BMO space is known as the dual space of the Hardy space  $H^1$  and one of the most important function spaces on real analysis. It is also known that the BMO norm is generalized to the scale of the  $L^p$  norm  $(1 \le p < \infty)$  by virtue of an argument with the John–Nirenberg inequality. We can generalize the BMO norm in terms of variable exponent satisfying suitable conditions. The study on catching the BMO norm in the context of general Banach function spaces has recently been progressed. The equivalent expressions of the BMO norm will be applied to get boundedess of commutators involving BMO functions on various function spaces and to new characterizations of function spaces.

March 18th (Tue) Conference Room III

### 9:00-12:20

Summary: In this talk, we show you the existence of solutions for nonlinear variational inequalities and quasi-variational inequalities that are generated by quasi-subdifferential operators. Quasi-variational inequality is a variational inequality whose constraint set depends upon unknown functions self.

Summary: In this talk, we discuss the solvability of the initial boundary value problem of a system which describes double-diffusive convection in some porous medium in general space domains. In our previous work, the solvability of the system in bounded domains was considered and the existence of a unique global solution is proved, where we relied on an abstract result based on the Schauder's fixed point argument, which can not work for the general (unbounded) domains. Instead of the previous argument, we here apply Banach contraction mapping principle.

Summary: This talk is concerned with the system of nonlinear heat equations with constraints coupled with Navier–Stokes equations. The existence and uniqueness of solutions have been already proved for several types of the system in 2-dimensional domains. This talk gives the existence result in 3-dimensional domains, where the diffusion term on heat equations is the *p*-Laplacian with  $p \ge 3$ .

Summary: We consider the abstract Cauchy problem for linear evolution equations of the form

$$\begin{cases} B(t)(d/dt)u(t) + A(t)u(t) = f(t), & t \in I, \\ u(0) = u_0. \end{cases}$$

Here  $\{A(t); t \in I\}$  and  $\{B(t); t \in I\}$  are families of closed linear operators in a complex Hilbert space.

24 Tetsuya Koyama On a regularity theorem for non-smooth domains · · · · · · · · · 15 (Hiroshima Inst. of Tech.)

Summary: A regularity theorem for second order elliptic equations on domains which are convex and have polygon boundary is discussed.

Summary: We prove  $L^1$  maximal regularity of the Cauchy problem in the Besov space  $\dot{B}_{p,1}^0(\mathbb{R}^n)$  with  $1 \leq p \leq \infty$ . The estimate obtained here is not available by abstract theory in the class of UMD since the end-point Besov space is included. Besides, we discuss the optimality of maximal regularity in  $L^1$ .

 26
 Ken Shirakawa (Chiba Univ.)
 Mathematic

 Hiroshi Watanabe (Salesian Polytech.)
 ......

 Noriaki Yamazaki (Kanagawa Univ.)

Summary: In this talk, a mathematical model of the grain boundary motion involving solidification effect is considered. The major theme of this study is to ensure qualitative properties for the mathematical model from the theoretical viewpoint in mathematics. As a part of this theme, we here focus on an analytical approach based on the time-discretization, and conclude the existence theorem of our mathematical model. Furthermore, we will mention about the problems in future with some supplemental comments.

Summary: We study a grain boundary motion model of Kobayashi–Warren–Carter type, which is a phasefield system of a nonlinear parabolic partial differential equation and a nonlinear parabolic variational inequality. In this talk we study non-autonomous systems of grain boundary motion. More precisely, we consider the time-dependent mobility function for the mean orientation of the crystalline. Then, we show the existence-uniqueness and large-time behavior of solutions to our non-autonomous systems.

Summary: This talk is concerned with the global existence of solutions to the Cauchy problem for  $n \times n$  hyperbolic systems of conservation laws with initial data having sufficiently small total variation. We show the global existence of solutions by improving the wave-front tracking algorithm.

29Dai Noboriguchi (Waseda Univ.)Uniqueness for the initial-boundary value problem for conservation laws<br/>with a multiplicative noise29Mazuo kobayasi (Waseda Univ.)With a multiplicative noise

Summary: We consider the initial-boundary value problem for a randomly forced scalar conservation laws with multiplicative noise on a bounded domain D in  $\mathbb{R}^d$ :  $du + \operatorname{div}(A(u)) dt = \Phi(u) dW(t)$  in  $(0,T) \times D$ ,  $u(0,\cdot) = u_0(\cdot)$  on D,  $u \cong u_b$  on  $(0,T) \times \partial D$ . We give the contraction property for kinetic solutions  $u_1$  and  $u_2$  of the problem associated with data  $(u_{1,0}, u_{1,b})$  and  $(u_{2,0}, u_{2,b})$ , respectivery:  $E \int_D |u_1(t) - u_2(t)| dx \leq E \int_D |u_{1,0} - u_{2,0}| dx + ME \int_0^t \int_{\partial D} |u_{1,b}(s) - u_{2,b}(s)| d\sigma(x) ds$  In particular, uniqueness of kinetic solutions is obtained.

Summary: The inverse function theorem requires the differentiation. This talk improves the core part of this theorem in the continuity class.

31 Shigehiro Sakata (Tokyo Metro. Univ.) Uniqueness of a maximizer of Riesz potential and the heart of a body

Summary: We investigate the uniqueness of a maximum point of the Riesz potential. A maximum point of the Riesz potential defines a center of a body, and the uniqueness has been studied by many geometers. We give a new sufficient condition for the uniqueness.

#### 14:15-15:55

32	<u>Takeshi Fukao</u> (Kyo	to Univ. of Edu.)	Allen–Cahn equation with dynamic boundary conditions and mass con-
	Pierluigi Colli	(Pavia Univ.)	straints · · · · · 15

Summary: The Allen–Cahn equation coupled with the dynamic boundary condition was treated by many papers, recently. The new issue of this talk is the setting of the mass constraint which can involve either the solution inside of the domain or its counterpart on the boundary.

Summary: We consider the initial value problem (CP) for strongly degenerate parabolic equations with diffusion term depending on the spatial variable. Strongly degenerate parabolic equations are regarded as a linear combination of the time-dependent conservation laws (quasilinear hyperbolic equations) and the porous medium type equations (nonlinear degenerate parabolic equations). Thus, this equation has both properties of hyperbolic equation and those of parabolic equations and describes various nonlinear convective diffusion phenomena such as filtration problems, Stefan problems and so on.

In this talk, we employ a new entropy pair and entropy solutions associated with (CP). Our purpose is to prove the uniqueness and existence of new entropy solutions in the space BV.

34Yoji Yamashita (Tokyo Univ. of Sci.)Existence of solutions to some degenerate parabolic equation associatedTomomi Yokota (Tokyo Univ. of Sci.)with the p-Laplacian in the critical case15

Summary: This talk is concerned with the initial-boundary value problem for the following degenerate parabolic equation:  $u_t(x,t) - \Delta_p u(x,t) - |u|^{q-2}u(x,t) = f(x,t)$  with initial data  $u_0 \in L^r(\Omega)$ ,  $\Omega \subset \mathbb{R}^N$ . Akagi (2007) established the existence of local (in time) solutions to this problem in the case r > N(q-p)/p; however, the critical case r = N(q-p)/p has been left as an open problem. In this talk, even in the critical case r = N(q-p)/p, the existence of solutions to the problem is established under a certain restriction on  $u_0$ . The key to our proof is Tartar's inequality, which enables us to derive desired convergences of approximate solutions to the problem from the compactness of the embedding  $W_0^{1,p}(\Omega) \subset L^2(\Omega)$ . Incidentally, any smoothness is not imposed on  $\partial\Omega$  at all while smooth boundary is needed in Akagi's result.

 35
 Toyohiko Aiki (Japan Women's Univ.)
 Smoluchowski population balance equation modified for hot colloids

 Oleh Krehel (TU Eindhoven)
 Adrian Muntean (TU Eindhoven)
 15

Summary: In this we consider a system of partial differential equations describing a mass conservation law for colloids in a small part of a porous medium. Here, we treat the Smoluchowski population balance equation as a reaction rate of generation of colloid particles. The aim of this talk is to show modeling process of the system and to establish the existence and uniqueness of a solution to initial boundary value problem for the system. Since some terms of the equations for the balance law are approximated and neglected in this result, it is open problem to improve the result.

 36
 Kentarou Fujie (Tokyo Univ. of Sci.)
 Existence and uniqueness of local-in-time classical solutions to a math 

 Akio Ito
 (Kinki Univ.)
 ematical model on tumor invasion phenomenon ······ 15

 Tomomi Yokota (Tokyo Univ. of Sci.)
 Sci.)
 Tomomi Yokota (Tokyo Univ. of Sci.)

Summary: The present work is concerned with the questions of local existence and uniqueness of solutions to the PDEs-ODE system to model a tumor invasion phenomenon. Using some estimate for  $e^{t\Delta}\nabla$ , we prove that the system possesses a unique local-in-time classical solution easily.

37 Risei Kano (Kochi Univ.) The solvability of the evolution problems for the tumor invasion models

Summary: In this talk, we discuss the solvability for weak solutions in the tumor invasion models. We have already showed the existence of solutions using the method of quasi-variational inequalities. But we do not show some propositions of solutions (for example, uniqueness), since its method has great nonlinearity. Then we show the existence of weak solutions for solutions for tumor invasion models.

### 16:15–17:15 Talk invited by Real Analysis Section

Kota Kumazaki \* A mathematical model for concrete carbonation phenomenon (Tomakomai Nat. Coll. of Tech.)

Summary: Concrete is made of sand, gravel, cement and water, and is a materical which shows alkalinity due to calcium hydrate which is the main ingradient of cement. Concrete carbonation is a phenomenon that this alkalinity changes into acidity due to carbon dioxide. This phenomenon is a big serious damage to the concrete buildings so that it is a important problem from the civil engineering point of view. In this talk, we consider a mathematical model for concrete carbonation phenomenon. This phenomenon occurs in the volds inside of concrete with some chemical reaction, the whole concrete carbonates due to the liquid of water generated by this reaction. Therefore, we focus on the moisture and carbon dioxide tranport, and consider two models in three dimensional cases. In this talk, we discuss a mathematical model for two transports and its mathematical analysis.

# **Functional Analysis**

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March 15th (Sat)
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Conference Room II

### 9:30 - 11:50

1	Kazuo Takemura (Nihon Univ.)* The best constants of discrete Sobolev inequalities on the finite <i>d</i> -regular
	weighted graph · · · · · · · · 10
	Summary: Two kinds of discrete Sobolev inequalities, corresponding to a Laplacian matrix on the finite
	d-regular weighted graph, are obtained. The best constants are calculated by using a Green matrix of the
	discrete heat equation and a pseudo Green matrix of the stationary state discrete heat equation.

 $\begin{array}{cccc} 2 & \mbox{Akito Suzuki} & (\mbox{Shinshu Univ.})^* & \mbox{Spectra of graphs obtained from the $d$-dimensional lattice by periodically adding pendant vertices} & \mbox{.} & \mbo$ 

Summary: We consider a graph obtained by adding pendant vertices to the *d*-dimensional lattice. We give a sufficient condition under which the Laplacian on such a graph has a spectral gap.

 3 <u>Hiroyuki Yamagishi</u> (Tokyo Metropolitan Coll. of Indus. Tech.)
 Kohtaro Watanabe (Nat. Defense Acad. of Japan)
 Yoshinori Kametaka (Osaka Univ.\*)

Summary: For an element of Sobolev space with Dirichlet-Neumann boundary condition, we have obtained the best constant of  $L^p$  Sobolev inequality including *j*-th derivative. The best constant is expressed by Bernoulli polynomials.

 

 4
 Hiroyuki Yamagishi (Tokyo Metropolitan Coll. of Indus. Tech.)
 The best constant of discrete Sobolev inequality corresponding to a bending problem of a string

 Atsushi Nagai (Nihon Univ.)
 Nihon Univ.)

 Yoshinori Kametaka (Osaka Univ.\*)

Summary: We obtain the best constants of discrete Sobolev inequalities corresponding to the second order difference equation, which describes a bending phenomenon of a string. We introduce a discrete Laplacian corresponding to the boundary value problem of the second order difference equation. We treat Dirichlet, Dirichlet-Neumann and Neumann boundary conditions. The best constants are given by Chebyshev polynomial.

Summary: The massless  $\phi^4$  model with the ultraviolet cutoff and the spatial cutoff is investigated. Under infrared regularity condition, it is proven that the ground state exists for all valued of coupling constants. It is also shown that the multiplicity of the ground state is finite.

radiation fields. The ultraviolet cutoffs are imposed on both the Dirac field and the radiation field, and the spatial cutoffs are also introduced. Under infrared regularity condition, the existence of the gournd state is shown for all values of coupling constants. It is also proven that the multiplicity of the ground state is finite.

- 7 Takuya Mine (Kyoto Inst. Tech.) Computation of the scattering amplitude in the elliptic coordinate ··· 15 Summary: We consider the Schrödinger operators with scalar potentials or magnetic vector potentials. Provided that the eigenequation can be solved by separation of variables in the elliptic coordinate, we give a formula for the quantum mechanical scattering amplitude in terms of the phase shift of the eigenfunctions and the angular Mathieu functions. In particular, we give a formula for the scattering amplitude of the magnetic Schrödinger operator with the two-solenoidal Aharonov–Bohm magnetic field with the quantized magnetic fluxes.

Summary: We consider a scattering problem under the Hamiltonian,  $p^2 - x^2 + V$ . In this system, we can see the characteristic property in which the particle disperse in an exponential order in time. This implies that scattering can arise even if we impose a weak decay condition on the potential V. In this talk, I will mention one of the multidimensional inverse scattering problems and report that the scattering operator can determin uniquely the potential V by the Enss-Weder time-dependent method.

Summary: H. Komatsu introduce Laplace hyperfunctions in one variable and their Laplace transforms which play a part in solving both linear ordinary differential equations and partial differential equations. Roughly speaking, a Laplace hyperfunction is presented as a difference of boundary values of holomorphic functions with exponential growth at infinity from a complex domain to a real domain. By the theory of Laplace hyperfunctions, we can treat Laplace transforms for functions without any growth conditions in a framework of hyperfunctions. In this talk, we introduce the sheaf of Laplace hyperfunctions in several variables, and we also show several properties of this sheaf.

### 14:15–15:15 Talk invited by Functional Analysis Section

Kenichi Ito (Univ. of Tsukuba) Classification of threshold properties of one-dimensional discrete Schrödinger operators

Summary: We study the relation between the generalized eigenspace and the asymptotic expansion of the resolvent around the threshold 0 for the one-dimensional discrete Schrödinger operator on  $\mathbb{Z}$ . We decompose the generalized eigenspace into the subspaces corresponding to the eigenstates and the resonance states only by their asymptotics at infinity, and classify the coefficient operators of the singlar part of resolvent expansion completely in terms of these eigenspaces. Here the generalized eigenspace we consider is largest possible. For an explicit computation of the resolvent expansion we apply the expansion scheme of Jensen–Nenciu (2001). This talk is based on the recent joint work with Arne Jensen (Aalborg University).

## March 16th (Sun) Conference Room II

### 10:00 - 11:50

Summary: We introduce a two-parameter deformation of the ordinary determinant and give an expansion formula with respect to immanants. Using this expansion, (i) we show an averaging formula of certain alpha-determinants, and (ii) we present several "determinantal" formulas for irreducible characters of the symmetric group associated with rectangular diagrams.

Summary: The Hecke–Clifford superalgebra is a super version of the Iwahori–Hecke algebra of type A, which is a q-analogue of the symmetric group algebra. Its irreducible representations are classified by Brundan, Kleshchev and Tsuchioka using a method of categorification of Lie algebras. However their constructions are too abstract to study. We here introduce a more concrete way to produce its irreducible representations using a generalized cellular structure on the superalgebra. It is a generalization of one first applied to the Iwahori–Hecke algebra by Murphy, and developed as theory of cellular algebras by Graham and Lehrer.

Summary: The coinvariant algebras of real reflection groups are already proved to have the strong Lefschetz property. In this talk we show that the coinvariant algebras of complex reflection groups except five primitive groups have the strong Lefschetz property. We also conjecture that these five types have the strong Lefschetz property.

13Yuichiro Tanaka (Univ. of Tokyo)Geometry of multiplicity-free representations of SO(N) and visible<br/>actions15

Summary: For a connected compact simple Lie group of type B or D, we find pairs  $(V_1, V_2)$  of irreducible representations of G such that the tensor product representation  $V_1 \otimes V_2$  is multiplicity-free by a geometric consideration based on a notion of visible actions on complex manifolds, introduced by T. Kobayashi. The pairs we find exhaust all the multiplicity-free pairs by an earlier combinatorial classification due to Stembridge.

14 Toshihisa Kubo (Univ. of Tokyo) The Dynkin index and parabolic subalgebras of Heisenberg type ..... 15

Summary: Barchini, Kable, and Zierau constructed a number of conformally invariant systems of differential operators associated to parabolic subalgebras of Heisenberg type. When they constructed such systems of operators, two constants, which play a role for the construction, were defined as the constants of proportionality between two expressions. In this talk we give concrete and uniform expressions for these constants. To do so we introduce a new constant inspired by a formula on the Dynkin index of a finite dimensional representation of a complex simple Lie algebra.

Summary: We construct the scattering theory for the Laplacian on symmetric spaces of noncompact type. We study an asymptotic expansion for the Poisson operator and the resolvent of the Laplacian. Our approach is based on precise analysis for the Helgason Fourier transform and generalized spherical functions (or Eisenstein integrals) on symmetric spaces of noncompact type. As an application of the scattering theory, we prove a conjecture suggested by Strichartz concerning a characterization of a family of generalized eigenfunctions of the Laplacian.

### 13:15–14:15 Talk invited by Functional Analysis Section

Kazuki Hiroe (Josai Univ.) Additive Deligne–Simpson problem and root systems

Summary: I will explain additive Deligne–Simpson problem which is a kind of inverse problem of Fuchsian differential equations on the Riemann sphere. The existence of the solution of this problem is completely characterized by the language of root systems after W. Crawley-Boevey. He found a relationship between Fuchsian differential equations and representations of quivers and applied the quiver theory to this problem. The aim of this talk is to consider an generalization of this problem to differential equations having an arbitrary number of unramified irregular singular points with poles of any order. After fix our generalized problems, I will discuss a relation between differential equations with irregular singularities and representations of quivers. As an application, the existence of the solutions of the generalized problems will be discussed.

March 17th (Mon) Conference Room II

### 9:30 - 12:00

Summary: All biunitary connections between ADE Dynkin diagrams were classified by Ocneanu. Here we will call them 'inter-Dynkin connections' for short. In this talk we will show computation of flat parts of all inter-Dynkin connections.

 17
 Hiroshi Ando (Univ. Copenhagen)
 Ultraproducts, QWEP von Neumann algebras and the Effros-Maréchal topology

 17
 Hiroshi Ando (Univ. Copenhagen)
 Ultraproducts, QWEP von Neumann algebras and the Effros-Maréchal topology

 17
 Garl Winsløw (Univ. Copenhagen)
 Ultraproducts, QWEP von Neumann algebras and the Effros-Maréchal topology

Summary: Haagerup and Winsløw studied topological properties of the Polish space vN(H) of von Neumann algebras acting on the separable infinite-dimensional Hilbert space H. Motivated by the work of Effros, this topology was introduced by Marechal. Among other interesting results, they proved that Kirhchberg's QWEP conjecture is equivalent to the assertion that the set  $\mathcal{F}_{inj}$  of injective factors on H is dense in vN(H), and moreover a II<sub>1</sub> factor M on H is  $R^{\omega}$ -embeddable if and only if M is the Effros–Maréchal limit of a sequence of injective factors. Based on the work of Haagerup–Winsløw and the recent work of the speaker and Haagerup on ultraproducts, we give new characterizations of QWEP von Neumann algebras.

#### 65 Functional Analysis

Summary: We give a classification theorem of actions of locally compact abelian groups with the Rohlin property on factors. This generalizes a recent work of Masuda and Tomatsu about Rohlin flows on von Neumann algebras.

Summary: We attempt presenting a notion of the Haagerup approximation property for an arbitrary von Neumann algebra by using its standard form.

Summary: We will show that for each Hecke pair of ergodic discrete measured equivalence relations, there exits a Hecke pair of groups determined by an index cocycle assosiated with the given pair.

Summary: In this series of talks with Hiroki Sako, we study coarse disjoint unions of discrete groups. Our main strategy is to exploit the Cayley topology. The topology allows us to regard a group as a point in a compact Hausdorff space. The subject of Part II is generalized embeddability of metric spaces, which is called fibered coarse embeddability. We observe that fibered coarse embeddability of a sequence of finite Cayley graphs can be described by its Cayley boundary groups. As an application, we construct an explicit example of such sequence which does not admit fibered coarse embedding into any uniformly convex Banach spaces or into any Hadamard manifolds.

Summary: We shall introduce the Rohlin property for finite group actions on stably projectionless C<sup>\*</sup>-algebras and study their basic properties. We shall give some examples of finite group actions on  $W_2$  and show some classification results of these actions.

Summary: We revisit and study the Euler characteristic for  $C^*$ -algebras and obtain the Euler–Poincaré formula for  $C^*$ -algebras, as a noncommutative version of the classical Euler–Poincaré formula for spaces.

#### 14:15-15:00

24	<u>Tsuyoshi Kajiwara</u> (Okayama Univ.)	Matrix representations and K-groups of the cores of C*-algebras as-
	Yasuo Watatani (Kyushu Univ.)	solated with self-similar maps 15

Summary: We write down explicitly matrix forms of the finite cores of C\*-algebras associated with two examples of self-similar maps, the tent map and Sierpinski Gasket, using a general method of matrix representations of the cores of C\*-algebras associated with self-similar maps with branched points. We also present a method of calculating matrix forms of the finite cores for general cases. Using explicit matrix forms and their inclusions of the finite cores for the above two examples, we do calculation of K-groups of the cores of C\*-algebras associated with them.

Summary: Let R be a rational function with degree at least two, let  $J_R$  be the Julia set of R and let  $\mu^L$  be the Lyubich measure of R. We study the C<sup>\*</sup>-algebra  $\mathcal{MC}_R$  generated by all multiplication operators by continuous functions in  $C(J_R)$  and the composition operator  $C_R$  induced by R on  $L^2(J_R, \mu^L)$ . We show that the C<sup>\*</sup>-algebra  $\mathcal{MC}_R$  is isomorphic to the C<sup>\*</sup>-algebra  $\mathcal{O}_R(J_R)$  associated with the complex dynamical system  $\{R^{\circ n}\}_{n=1}^{\infty}$ .

 

 26
 Kei Ji Izuchi (Niigata Univ.)\* Path connected components in the space of weighted composition op-Yuko Izuchi erators on the disk algebra

 Shûichi Ohno (Nippon Inst. of Tech.)
 15

Summary: We here study path connected components in the space of weighted composition operators on the disk algebra. We show that the structures of path connected components on the disk algebra and  $H^{\infty}$  are different.

### 15:15–16:15 Award Lecture for 2013 Analysis Prize

Yasuo Watatani (Kyushu Univ.) Singularities in operator algebras

Summary: We study singularities in operator algebras. Iteration of a rational function gives a complex dynamical system. The associated C\*-algebra has some information of the branched points of the rational function. A self-similar map also give a C\*-algebra. The structure of the core of the C\*-algbra is described in terms of the branched points. We also study Hilbert representations of quivers.

### 16:30–17:30 Talk invited by Functional Analysis Section

Sei-Ichiro Ueki (Ibaraki Univ.) Composition and Integral operators on Bargmann–Fock spaces

Summary: In this talk, we consider composition, weighted composition and Volterra-type integral operators on Bargmann–Fock spaces over the complex plane.
# March 18th (Tue) Conference Room II

# 10:00-11:40

27Wataru Ichinose (Shinshu Univ.)On the uniqueness of the polar decomposition of bounded operators in<br/>Hilbert spacesKanako Iwashita (Shinshu Univ.)Hilbert spaces15

Summary: It is well known that a bounded operator in Hilbert spaces has a polar decomposition, i.e. the product of a partially isometric operator and its square root. Its polar decomposition is not unique in general. In this talk a necessary and sufficient condition is given for an operator to have the unique polar decomposition.

28 Yuki Seo (Osaka Kyoiku Univ.) Buzano inequality in inner product  $C^*$ -modules via the operator geometric mean  $\cdots 10$ 

Summary: In this talk, we present a Buzano type inequality in an inner product  $C^*$ -module, which is an extension of the Cauchy–Schwarz inequality in an inner product  $C^*$ -module.

29	Junichi Fujii (Osaka Kyoiku Univ.)	Reproducing property of interpolational operator means in a Karcher	
		equation ·····	15

Summary: For positive invertible operators A and B, the two-terms Karcher equation for an operator monotone function F with F(1) = 0 and F'(1) = 1 has the solution which is a mean-like binary operation for A and B. But it is not always an operator mean in the sense of Kubo–Ando. We show that if F is induced by the derivative of interpolational path  $f_t$ , then the solution is an operator mean induced by  $f_t$ .

Summary: We give a 'local' integral representation of a matrix connection of order n corresponding to an interpolation function of the same order. Applying this property, for each integer n, we can describe an one to one corresponding from the class of matrix connections of order n to the class of positive n-monotone functions on  $(0, \infty)$  and the range of this corresponding covers the class of interpolation functions of order 2n. In particular, the space of symmetric connections is isomorphic to the space of symmetric positive n-monotone functions.

Summary: Let J be an open interval on  $\mathbb{R}$  and f a real valued  $C^k$ -function. We denote  $H_n = \{A \in M_n(\mathbb{C}) \mid A = A^*\}$  and  $H_n(J) = \{A \in H_n \mid \operatorname{Sp}(A) \subset J\}$ . We consider the condition for  $A, B \in H_n$ , which implies  $A \leq B$ . This problem is motivated by the consideration of reverse order of operator monotone functions. Our main results is, for  $C \in H_n(J)$  with C(A - B) = (A - B)C,  $Df(C)(A) \leq Df(C)(B)$  implies  $A \leq B$ , if f'(c) > 0  $(c \in J)$ , where Df(C)(A) means the directional Fréchet derivative of f at C to A.

## 68 Functional Analysis

Summary: The operator monotonicity of the following function

$$S(t) = t^{\gamma} \frac{(t^{\alpha_1} - 1)(t^{\alpha_2} - 1)\cdots(t^{\alpha_n} - 1)}{(t^{\beta_1} - 1)(t^{\beta_2} - 1)\cdots(t^{\beta_n} - 1)} \qquad t \in [0, \infty)$$

which was investigated by Szabó is studied. We first estimate the bounds of

$$\arg \frac{(z^{\alpha} - 1)}{(z^{\beta} - 1)} \qquad 0 \le \arg z \le \pi$$

by an elementary but a bit complicated calculus and apply this result to check the monotonicity.

# 14:15 - 15:15

33 Takeaki Yamazaki (Toyo Univ.) Generalized Ando-Hiai inequality for matrix power mean ...... 10

Summary: In this talk, we shall introduce the definition of generalized matrix power mean. Then we shall introduce some properties of it. Especially, we shall introduce generalized Ando-Hiai inequality for generalized matrix power mean.

 34 <u>Hiroshi Isa</u> (Maebashi Inst. of Tech.) Masatoshi Ito (Maebashi Inst. of Tech.)
 A Masatoshi Ito (Maebashi Inst. of Tech.)
 A Masatoshi Ito (Maebashi Inst. of Tech.)
 A Masayuki Watanabe (Maebashi Inst. of Tech.)

Summary: For strictly positive operators, an operator valued  $\alpha$ -divergence is defined based on the difference between the weighted arithmetric mean and the weighted geometric mean. In this report, we show some relations between operator valued  $\alpha$ -divergence and some relative operator entropies. For any  $w \in \mathbf{R}$ , the same forms as the relations between operator valued  $\alpha$ -divergence and relative operator entropies arise on path  $A \natural_w B$ . Moerover, we introduce a sequence version of operator valued  $\alpha$ -divergence for strictly positive operator sequences, and show the relations among sequence version of some operator entropies.

Summary: We define some symmetric homogeneous means and then derive unitarily invariant norm inequalities for them applying the powerful method established by Hiai and Kosaki. Our inequalities give the tighter bounds of logarithmic mean than the inequalities given by Hiai and Kosaki.

Summary: In quantum mechanics the expectation value of an observable H in a quantum system  $\rho$  is expressed by  $Tr[\rho H]$  and the variance is given by  $Tr[\rho(A - (Tr[\rho H])I)^2]$ , respectively. We assume that the observable is not hermitian. Then we study the corresponding uncertainty relation.

# **Statistics and Probability**

March 15th (Sat)

Conference Room VI

# 9:30 - 12:00

 1
 Dai Taguchi (Ritsumeikan Univ.)
 Strong rate of convergence for the Euler-Maruyama approximation of

 Hoang-Long Ngo
 stochastic differential equations with irregular coefficients

 (Hanoi Nat. Univ. of Edu.)
 Hoang-Long Ngo

Summary: We consider the Euler–Maruyama approximation for multi-dimensional stochastic differential equations with irregular coefficients. We provide the rate of strong convergence where the possibly discontinuous drift coefficient satisfies a one-sided Lipschitz condition and the diffusion coefficient is Hölder continuous.

Summary: We investigate asymptotic behavior of sums of independent and truncated random variables specified by  $P(0 \le X < \infty) = 1$  and  $P(X > x) \asymp x^{-\alpha}$  for  $\alpha > 0$ . By varying truncation levels we study strong laws of large numbers and central limit theorems. These are extensions of the results of Györfi and Kevei (2011) concerning the St. Petersburg game.

3 <u>Katusi Fukuyama</u> (Kobe Univ.)\* The central limit theorem for subsequences of Erdős–Fortet sequence Takafumi Minohara (Taiyo Elec Co.) 5

Summary: We give the equivalent condition for the central limit theorem for subsequences of Erdős–Fortet sequence.

Summary: We consider the percolation problem in the high-temperature Ising model on the two-dimensional square lattice at or near critical external fields. The incipient infinite cluster (IIC) measure in the sense of Kesten is constructed. As a consequence, we can obtain some geometric properties of IIC. The result holds also for the triangular lattice.

 $\frac{\text{Taro Murayama}}{\text{Takashi Ichinose}} (\text{Kanazawa Univ.})^* \text{ The zero mass limit problem for a relativistic spinless quantum particle} in an electromagnetic field \cdots 15$ 

Summary: We consider mass-parameter-dependent solutions of the imaginary time magnetic relativistic Schrödinger equation which describes a spinless quantum particle. It is shown that they converge as functionals of Lévy processes represented by stochastic integrals of stationary Poisson point processes if the mass-parameter goes to zero.

# 70 Statistics and Probability

6 Nariyuki Minami (Keio Univ.) Definition and self-adjointness of the stochastic Airy operator ..... 15

Summary: It has been shown that the stochastic Airy operator, which was considered by Ramirez, Rider and Virag, and which is the "Schroedinger operator" on the half line whose potential term consists of Gaussian white noise plus a linear term tending to plus infinity, can naturally be realized as a closed symmetric operator in the Hilbert space of square integrable functions and is self-adjoint with probability one. Moreover, it has purely discrete spectrum.

Summary: A notion of covergence of excursion measures is introduced. It is proved that convergence of excursion measures imply convergence in law on the càdlàg path space for the processes pieced together from excursions accompanied with the local time at the origin and its inverse. This general theorem is applied to obtain homogenization theorems of jumping-in extensions for self-similar processes.

Summary: On the basis of fractional calculus, we will introduce an alternative proof of Lyons' extension theorem for Geometric Hölder rough paths together with an explicit expression of the extension map. The proofs of constructing the extension of rough paths and the continuity of the extension map due to Lyons (1998) are based on discrete approximating arguments such as dealing with limits of Riemann sums. However, our approach will not use the arguments and will be more straightforward. In fact, the explicit expression of the extension map introduced in this talk will be provided as the usual Lebesgue integral by using the fractional derivatives.

Summary: Consider stochastic functional differential equations depending on past histories, which determines the non-Markovian process. We shall study the large deviations for the family of the solution process, and apply it to the study on the asymptotic behavior of the density. The Malliavin calculus plays a crucial role in our argument.

Masaaki Fukasawa (Osaka Univ.) Whittle likelihood for high frequency data

Summary: We consider statistical estimation of the diffusion coefficient of an Ito process from high frequency data. This has been thoroughly investigated in the case that the values of the Ito process are available as data. A quasi likelihood based on the Euler–Maruyama approximation works there. Here we are interested in the case where only available are integrated values of the Ito process. We encountered this situation at the very beginning of the history of stochastic differential equation modeling, namely, the Langevin dynamics of molecular system. Even if the Ito process is a diffusion, the integrated process is not Markov any more. The Euler–Maruyama approximation fails to give a consistent estimate. Only a few studies have been done and no efficient estimator has been available so far. In this study, we construct a new quasi likelihood inspired by Whittle's approximation to the covariance function of stationary Gaussian time series. We show the consistency, asymptotic mixed normality and asymptotic efficiency of our estimator. Technical difficulties come from the fact that the Whittle likelihood is not a martingale estimating function and so, beyond the standard framework of high frequency data analysis. Also, the model is LAMN but not LAN. Therefore results for Gaussian time series are not useful here.

# 15:45–16:45 Award Lecture for 2013 Analysis Prize

Toshiro Watanabe (Univ. of Aizu) Relation between infinitely divisible distributions and their Lévy measures

March 16th (Sun) Conference Room VI

# 9:00 - 11:25

10 Shin-Ichiro Takazawa (Kobe Univ.)\* The convergence rate of the strong law of large numbers by a finite number of strategies in the unbounded forecasting game ..... 10

Summary: We consider the convergence rate of the strong law of large numbers in the framework of gametheoretic probability of Shafer and Vovk. We show that in the predictably unbounded forecasting game Skeptic can weakly force the strong law of large numbers by a single strategy.

11 Xiao-Nan Lu (Nagoya Univ.) On affine-invariant strictly cyclic Steiner quadruple systems ...... 15

Summary: A Steiner quadruple system denoted by SQS(v), is a pair  $(V, \mathcal{B})$ , where V is a finite set of v points, and  $\mathcal{B}$  is a collection of 4-subsets of V, called blocks or quadruples, such that each 3-subset of V appears exactly once in  $\mathcal{B}$ . If SQS(v) admits a cyclic permutation whose stabilizer of any block is trivial, it is said to be strictly cyclic, denoted by sSQS(v). In this talk, we consider an sSQS(2p) over  $\mathbb{Z}_{2p}$  admitting all the units of  $\mathbb{Z}_{2p}$  as multipliers, which is said to be affine-invariant. A new family of graphs related to the special projective linear groups over finite fields is introduced for the construction of an affine-invariant sSQS(2p). The 1-factors of such graphs give rise up to the base blocks of an affine-invariant sSQS(2p).  

 12
 Kiyotaka Iki (Tokyo Univ. of Sci.)
 Quasi-diagonal exponent symmetry model for ordinal square contingency tables.

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 Sadao Tomizawa (Tokyo Univ. of Sci.)
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Summary: For square contingency tables with ordered categories, we propose a simple quasi-symmetry model in which the expected frequency has an exponential form along every subdiagonal of the table. It also give the theorem such that Tomizawa's (1992) diagonal exponent symmetry (DES) model holds if and only if the proposed model and the model of equality of row and column marginal means hold.

13 <u>Shoko Chisaki</u> (Tokyo Univ. of Sci.) Difference system of sets with size 3 · · · · · · · · · · 10 Nobuko Miyamoto (Tokyo Univ. of Sci.)

Summary: Difference systems of sets (DSS) are combinatorial structures introduced by Levenshtein in 1971, which are a generalization of cyclic difference sets and arise in connection with code synchronization. A DSS is a collection of t disjoint subsets  $Q_i, 0 \le i \le t - 1$ , of any finite abelian group G of order v such that every element of  $G \setminus \{0\}$  appears at least  $\rho$  times in the multiset  $\{a - b | a \in Q_i, b \in Q_j, 0 \le i \ne j \le t - 1\}$ . In this talk, we define new blocks with size 3 and present the conditions that these blocks form a perfect DSS.

14 <u>Kohei Yamada</u> (Tokyo Univ. of Sci.) A construction of orthogonal arrays from Baer subplanes ..... 15 Nobuko Miyamoto (Tokyo Univ. of Sci.)

Summary: It is a fundamental and important problem in combinatorics and incidence geometry to find construction methods of orthogonal arrays. Fuji-hara and Kamimura (1993) proposed a construction method of orthogonal arrays with non-prime power number of symbols. In this talk, we improved this method and thereby experimentally give many new orthogonal arrays with much smaller runs and indices, compared with the arrays obtained from the earlier work. These new arrays also have a non-prime power number of symbols.

 15
 Takeshi Torii (Osaka Pref. Univ.)
 Two construction methods of a nested row-column design with split

 Shinji Kuriki (Osaka Pref. Univ.)
 units
 15

Summary: We consider two construction methods of a nested row-column design with split units for a two-factor experiment. The whole plot treatments occur in a generalized Youden design and a bottom stratum universally optimum nested row and column design. The subplot treatments occur in a proper block design. We consider a mixed linear model for the observations with a four-step randomization and we give the stratum efficiency factors for such nested row-column designs with split units, which have the general balance property.

10 Satoru Nauowaki	16	Satoru	Kadowaki
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Sanpei Kageyama

(Hiroshima Inst. of Tech.)

(Matsue Coll. of Tech.)

Summary: Much construction of (affine) resolvable PBIB designs with their combinatorial properties has been discussed in literature. Kadowaki and Kageyama (2009) provided some methods of construction of such block designs.

**Theorem 1.1 [Kadowaki and Kageyama (2009)].** The existence of a Hadamard matrix of order 2x is equivalent to the existence of an affine resolvable symmetric SRGD design with parameters  $v = b = 4x, r = k = 2x, \lambda_1 = 0, \lambda_2 = x, q = x; m = 2x, n = 2$ .

We can show the following as a generalization of Theorem 1.1.

**Theorem 2.1.** Let s be a prime or a prime power. Then the existence of a DS(m, s; x) is equivalent to the existence of an affine resolvable symmetric SRGD design with parameters  $v = b = xs^2$ , r = k = xs,  $\lambda_1 = 0$ ,  $\lambda_2 = x$ , q = x; m = xs, n = s.

Masahide Kuwada (Int. Inst. for Nat. Sci.)
 Yoshifumi Hyodo (Okayama Univ. of Sci./Int. Inst. for Nat. Sci.)
 <u>Hiromu Yumiba</u> (Int. Inst. for Nat. Sci.)

Summary: We consider a fractional  $3^m$  factorial design derived from an SA $(m; \{\lambda_{xm-x-yy}\})$ , where  $m \ge 4$ . In this situation, we give a necessary and sufficient condition for an SA to be a balanced fractional  $3^m$  factorial design of resolution R( $\{00, 10, 01, 20, 11\}$ ). Such a design is characterized by the suffixes x and y of the index  $\lambda_{xm-x-yy}$  of an SA.

18	Masatake Hirao	Characterizing optimum designs in terms of finite irreducible reflection
	(Tokyo Woman's Christian Univ.)	groups · · · · · · 15
	Masanori Sawa (Nagoya Univ.)	

Summary: In this talk we give a geometric characterization of D-optimal experimental designs on the unit ball that consist of corner vectors associated with finite irreducible reflection groups.

 <u>Kazuki Matsubara</u> (Hiroshima Univ.) Constructions of pairwise additive cyclic BIB designs ..... 10
 Sanpei Kageyama (Hiroshima Inst. of Tech.)

Summary: The existence of pairwise additive balanced incomplete block (BIB) designs has been discussed with direct and recursive constructions in Matsubara et al. (2007, 2013). In this talk, pairwise additive cyclic BIB designs and a special array are proposed and some recursive methods of constructing such designs with the special array are provided. It is finally shown that 2 PACB( $2^m 3^n t, 2, 1$ ) for any integers  $m \geq 0$ ,  $n \geq 0$ and  $t \geq 1$  such that  $m \not\equiv 1 \pmod{4}$ ,  $n \neq 1, 2$ , gcd(t, 6) = 1 and  $(m, n, t) \neq (0, 0, 1)$  can be constructed.

# March 17th (Mon) Conference Room VI

# 9:00-12:00

Summary: The probability content of a convex polyhedron with a multivariate normal distribution can be regarded as a real analytic function. We give a system of linear partial differential equations with polynomial coefficients for the function and show that the system induces a holonomic module. The rank of the holonomic module is equal to the number of nonempty faces of the convex polyhedron, and we provide an explicit Pfaffian equation (an integrable connection) that is associated with the holonomic module.

Summary: In directional statistics, the wrapped Cauchy family is known as the family of probability distributions on the unit circle induced by the Moebius transformations. In this talk, we derive a family on higher-dimensional spheres by using the transformations. The family is shown to have a hyperbolic structure with respect to the Fisher–Rao information metric. The distribution is not characterized by the Brownian exiting distribution as opposed to the circle case.

22 <u>Sigeo Aki</u> (Kansai Univ.) Coupon collector's problems with statistical applications ..... 10 Katuomi Hirano (Josai Univ.)

Summary: Some new exact distributions on coupon collector's waiting time problems are given based on a generalized Polya urn sampling. In coupon collector's waiting time problems with m kinds of coupons, the observed order of m kinds of coupons corresponds to a permutation of m letters uniquely. Using the property of coupon collector's problems, a statistical model on the permutation group of m letters is proposed for analyzing ranked data. In the model, as the parameters mean the proportion of the m kinds of coupons, the observed ranking can be intuitively understood.

Summary: We introduce a class of a directed acyclic graph on the assumption that the collection of random variables indexed by the vertices has a Markov property. We present a flexible approach for the study of the exact distributions of runs and scans on the directed acyclic graph by extending the method of conditional probability generating functions. The results presented here provide a wide framework for developing the exact distribution theory of runs and scans on the graphical models. We also show that our theoretical results can easily be carried out through some computer algebra systems and give some numerical results for run and scan statistics in order to demonstrate the feasibility of our theoretical results. Finally, we address the parameter estimation in the distributions of runs and scans.

24	<u>Koji Tsukuda</u>	An $L^2$ approach to detect a change of parameters in an ergodic diffusion	
	(Grad. Univ. for Adv. Stud.)	process model · · · · · · · 15	
	Yoichi Nishiyama		
	(Inst. of Stat. Math /Grad. Univ. for Adv. Stud.)		

Summary: In this presentation, to test a change of drift parameters in an ergodic diffusion process model is discussed. For this problem, past studies chose  $\ell^{\infty}$  space as the framework of weak convergences of proposed *sup* type test statistics. On the other, we will develop an approach by limit theorems in  $L^2$  space and propose a weighted integral type test statistic, which is expected to have better power in many cases.

Summary: In this talk, we develop the testing theory for second order stationary processes with spectral restriction. The model concerned is defined nonparametrically and the functional of the spectral density summarizes information about pivotal quantities of the model. It is known that many important quantities in stationary time series are often expressed as a functional of the spectral density. We apply the approach which is mainly based on the local asymptotic normality (LAN) to the frequency domain generalized method of moments (GMM) framework, and elucidate the local power of tests to discuss local asymptotic optimality.

Summary: In this talk, we give the asymptotics for M-estimators in time domain of the time series analysis without the assumption that the objective function is differentiable with respect to the parameter at the true value. Especially, we define the objective function of M-estimator as two-variate function, i.e. the function of scale parameters and coefficient parameters, which may be transformed to correspond to the Whittle estimator in frequency domain. The result can be extended to  $M_m$  estimators or be corresponded to the estimators in frequency domain approach. Examples and the applications of the result will also be presented.

27 <u>Akio Tanikawa</u> (Osaka Inst. of Tech.) Identification of partially unknown system matrix of discrete-time sto-Yuichi Sawada (Kyoto Inst. Tech.) chastic systems via pseudomeasurement approach ..... 10

Summary: A new identification method of discrete-time linear stochastic systems is proposed. We assume that some entries of the system matrix are unknown and propose a new method which identifies those unknown entries and the state vector of the system simultaneously. The key idea of the proposed method is the use of pseudomeasurement which is a fictitious observation process on the unknown entries and has been introduced by Kameyama and Ohsumi for continuous-time linear stochastic systems.

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Summary: We consider the problem of testing equality of two mean vectors when the data have three-step monotone pattern missing observations. The maximum likelihood estimators of the mean vector and the covariance matrix for the case of two sample problem with a three-step monotone missing data are given. In this paper, we propose an approximate upper percentile of the Hotelling's  $T^2$  type statistic where the each of data set has a three-step monotone missing data and the population covariance matrices are equal. This result is an extension of one sample problem given in Yagi and Seo (2013). Further, we obtain the approximate simultaneous confidence intervals for all linear compounds of the difference of two mean vectors. Finally, the accuracy of the approximation is investigated by Monte Carlo simulation.

# 29 <u>Kazuyoshi Yata</u> (Univ. of Tsukuba) Quadratic-type classifiers for high-dimensional data · · · · · · · · · 15 Makoto Aoshima (Univ. of Tsukuba)

Summary: In this talk, we consider a quadratic-type classifier for multiclass, high-dimensional data. We first show that the classifier holds the consistency in misclassification rates for multiclass, high-dimensional classification. We also show that the classifier is asymptotically distributed as a normal distribution when the data dimension goes to infinity. The classifier contains a function of scale parameters. We propose a criterion to evaluate the performance of the classifier and choose the optimal function to define the best classifier.

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Summary: For a truncated exponential family of distributions with a natural parameter and a truncation parameter as a nuisance parameter, it is known that the maximum likelihood estimators (MLEs) of the natural parameter for known truncation parameter and unknown truncation one and the maximum conditional likelihood estimator (MCLE) of the natural parameter for unknown truncation one are asymptotically equivalent. Here, the asymptotic expansions of the MLEs and MCLE are derived up to the second order, and their second order asymptotic variances are obtained. A bias-adjusted MLE and the MCLE of the natural parameter for unknown truncation parameter are also shown to be second order asymptotically equivalent, and further the second order asymptotic loss of the bias-adjusted MLE for unknown truncation parameter relative to the MLE for known truncation one is given. <u>Masafumi Akahira</u> (Univ. of Tsukuba)
 Shintaro Hashimoto (Univ. of Tsukuba)
 Ken-ichi Koike (Univ. of Tsukuba)
 Nao Ohyauchi (Univ. of Tsukuba)

Asymptotic comparison of the MLE and MCLE up to the second order for a two-sided truncated exponential family ..... 10

Summary: In a similar way to Akahira (2013, Math. Res. Note 2013-001, Inst. Math., Univ. Tsukuba), for a two-sided truncated exponential family of distributions with a natural parameter and two truncation parameters as nuisance parameters, the asymptotic expansions of the maximum likelihood estimator (MLE) of the natural parameter for known truncation parameters, the MLE and the maximum conditional likelihood estimator (MCLE) of the natural parameter for unknown truncation parameters are derived, their asymptotic variances are obtained up to the second order, a bias-adjusted MLE and the MCLE of the natural parameter for unknown truncation parameters relative to the second order asymptotic loss of the bias-adjusted MLE for unknown truncation parameters relative to the MLE for known truncation ones is given.

# 14:30–15:30 Talk invited by Statistics and Probability Section

Hisayuki Tsukuma (Toho Univ.) Decision-theoretic estimation of parameter matrices

Summary: The estimation problems of parameter matrices in multivariate models are considered from a decision-theoretic perspective. We first treat the problem of estimating mean matrix and discuss minimaxity, admissibility and inadmissibility of Bayes estimators relative to a quadratic loss. Next, the estimation problem of normal covariance matrix is addressed, and we provide an alternative proof for minimaxity and an improvement method on the minimax estimator.

# 15:45–16:45 Talk invited by Statistics and Probability Section

Taiji Suzuki (Tokyo Tech) Statistical properties of multiple kernel learning and sparse estimation

Summary: We discuss statistical properties of multiple kernel learning (MKL) which has been developed in the machine learning community. Kernel methods utilize the inner product defined on a reproducing kernel Hilbert space as an inner-product between data points to realize non-linear flexible data analysis. The performance of a kernel method is affected by the choice of the inner-product associated with the kernel function. MKL is a method that automatically selects and constructs an appropriate kernel from observed data. MKL is closely related to  $L_1$ -regularized sparse estimation. In this presentation, we overview the recent theoretical developments about statistical performances of MKL.

# **Applied Mathematics**

March 15th (Sat)

Conference Room IX

# 9:30 - 11:50

Summary: In graph theory, the decomposition problem of graphs is a very important topic. Various type of decompositions of many graphs can be seen in the literature of graph theory. This paper gives balanced  $C_4$ -foil designs and related designs.

2	Iwao Sato (Oyama Nat. Coll. of Tech.)	А	no	ote	on	ı t	he	di	scre	ete-	-tim	e e	evolutions	for	· q	ıar	ntur	n '	wal	k	on	$\mathbf{a}$	grap	h	
	Norio Konno (Yokohama Nat. Univ.)			• •		•		• •		••		• •				••		••		••				•	15
	Yusuke Higuchi (Showa Univ.)																								
	Etsuo Segawa (Tohoku Univ.)																								

Summary: For a quantum walk on a graph, there exist many kinds of operators for the discrete-time evolution. We give a general relation between the characteristic polynomial of the evolution matrix of a quantum walk on edges and that of a kind of transition matrix of a classical random walk on vertices. Furthermore we determine the structure of the positive support of the cube of some evolution matrix, which is said to be useful for isospectral problem in graphs, under a certain condition.

Summary: The notion of travel groupoids was introduced by L. Nebeský in 2006 in connection with a study on geodetic graphs. A travel groupoid is a pair of a set V and a binary operation \* on V satisfying two axioms. For a travel groupoid, we can associate a graph. We say that a graph G has a travel groupoid if the graph associated with the travel groupoid is equal to G. Nebeský gave a characterization for finite graphs to have a travel groupoid.

In this talk, we consider travel groupoids on infinite graphs. We answer a question posed by Nebeský, and we also give a characterization for infinite graphs to have a travel groupoid.

4 Jung-Rae Cho (Pusan Nat. Univ.) The non-confusing travel groupoids on a finite connected graph ..... 10
 Jeongmi Park (Pusan Nat. Univ.)
 Yoshio Sano (Univ. of Tsukuba)

Summary: The notion of travel groupoids was introduced by L. Nebeský in 2006 in connection with a study on geodetic graphs. A travel groupoid is a pair of a set V and a binary operation \* on V satisfying two axioms. For a travel groupoid, we can associate a graph. We say that a graph G has a travel groupoid if the graph associated with the travel groupoid is equal to G. A travel groupoid is said to be non-confusing if it has no confusing pairs. Nebeský showed that every finite connected graph has at least one non-confusing travel groupoid.

In this talk, we consider non-confusing travel groupoids on a given finite connected graph, and we give a one-to-one correspondence between the set of all non-confusing travel groupoids on a finite connected graph and a combinatorial structure in terms of the given graph.

# 79 Applied Mathematics

5

Summary: Let  $\alpha(G)$  be the independence number of a graph G. A graph G is said to be contraction-critical (with respect to the independence number) if  $\alpha(G/e) < \alpha(G)$  holds for every edge e in G, where G/e is the graph obtained from G by the contraction of G. In this talk, we give a characterization of the contraction-critical graphs.

Summary: A map of a surface  $F^2$  is a graph with a fixed 2-cell embedding on  $F^2$ . A triangulation of a surface  $F^2$  is a map on  $F^2$  in which every face is triangular. We call it even if every vertex degree is even. A quadrangulation of a surface  $F^2$  is a map on  $F^2$  in which every face is quadrangular. We consider the following two problems; For a given quadrangulation G of a surface  $F^2$ , can we get an even triangulation by adding a diagonal edge to each face of G? For a given triangulation G of a surface  $F^2$ , can we find a bipartite quadrangulation of  $F^2$  as a subgraph of G?

7 Yusuke Suzuki (Niigata Univ.) Reductional operations for polyhedral quadrangulations ..... 15

Summary: We show that for any nonspherical surface  $F^2$ , there exists only finitely many irreducible polyhedral quadrangulations of  $F^2$ , up to homeomorphism, by using seven reductional operations.

 8 Guantao Chen (Georgia State Univ.) Plane triangulations without spanning Halin subgraphs ...... 15 Hikoe Enomoto (Waseda Univ.)
 Kenta Ozeki (Nat. Inst. of Information/JST ERATO)
 <u>Shoichi Tsuchiya</u> (Tokyo Univ. of Sci.)

Summary: A Halin graph, defined by Halin, is a plane graph  $H = T \cup C$  such that T is a spanning tree of H with no vertices of degree 2 where  $|T| \ge 4$  and C is a cycle whose vertex set is the set of leaves of T. Halin graphs are edge-minimal 3-connected graphs with many interesting properties. In 1975, Lovász and Plummer conjectured that every 4-connected plane triangulation has a spanning Halin subgraph. In this talk, we show that there is an infinite family of 5-connected plane triangulations which have no spanning Halin subgraph. Consequently, the Lovász and Plummer conjecture does not hold.

# 14:30-16:40

9	Chie Nara	(Tokai Univ.)	Transformability and reversibility of unfoldings of doubly-covered poly-
	Jin-ichi Itoh (K	umamoto Univ.)	hedra

Summary: If a convex polyhedron W is dissected into a finite number of pieces which can be rearranged to form a convex polyhedron X with hinges, W is called *transformable* to X, and if the surface of Wis transformed to the interior of X except some edges of pieces, W is called *reversible* to X. Our main result is that for a reflective space-filler P, any convex unfolding W of a doubly covered polyhedron of P is transformable to any convex unfolding X of a doubly covered polyhedron of a mirror image  $P^m$  of P, where we assume both W and X include P and  $P^m$  respectively.

 10
 <u>Maki Furukado</u> (Yokohama Nat. Univ.)
 The condition for the generation of the stepped surfaces in terms of the modified Jacobi–Perron algorithm

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 Shin-ichi Yasutomi (Toho Univ.)
 The condition for the generation of the stepped surfaces in terms of the modified Jacobi–Perron algorithm

Summary: P. Arnoux and S. Ito introduce the tiling substitution on the stepped surface related to the irreducible and Pisot substitution in 2001. We are especially interested in the condition for the generation of the stepped surface by the sequence of the tiling substitution in terms of the modified Jacobi–Perron algorithm. We observe the geometrical property of the patches which construct the stepped surface and we have succeeded in getting the admissible sequence of the tiling substitution which generates the stepped surface in terms of the modified Jacobi–Perron algorithm.

11 Masato Mimura (Tohoku Univ.)\* Spehere equivalence, Banach spectral gaps, and extrapolation · · · · · 12

Summary: We introduce the notion of sphere equivalence between Banach spaces, and show that the spectral gap property is stable under this equivalence relation. As a byproduct, we obtain certain generalization of Matousek's extrapolation, and prove that a family of expanders realizes the owrst order of the distortions for a certainlarge class of Banach spaces.

Summary: We prove certain inequalities between multi-way isomeprimetries of vertex-transitive grpahs. As a byproduct, we show the existence of system of imprimitivity of certain size if there is a gap between multi-way isoperimetric constants.

13 Hidefumi Ohsugi (Rikkyo Univ.) The maximum number of edges of an edge polytope ..... 20
 Akihiro Shikama (Osaka Univ.)
 Takayuki Hibi (Osaka Univ.)
 <u>Aki Mori</u> (Osaka Univ.)

Summary: Let  $[d] = \{1, \ldots, d\}$  be the vertex set and  $\Omega_d$  the set of finite simple graphs on [d], where  $d \geq 3$ . We write  $\varepsilon(G)$  for the number of edges of the edge polytope  $\mathcal{P}_G \subset \mathbb{R}^d$  of  $G \in \Omega_d$ . For example,  $\varepsilon(K_d) = d(d-1)(d-2)/2$ , where  $K_d$  is the complete graph on [d]. Let  $\mu_d = \max\{\varepsilon(G) : G \in \Omega_d\}$ . We wish to find  $G \in \Omega_d$  with  $\mu_d = \varepsilon(G)$  and to compute  $\mu_d$ . One may expect  $\mu_d = \varepsilon(K_d)$ . In fact, it turns out to be true that  $\mu_d = \varepsilon(K_d)$  for each  $3 \leq d \leq 14$ . However, it will be proved that, for each  $d \geq 15$ , one has  $\mu_d \geq \varepsilon(K_d) + 50(d-14)$ . It remains unsolved to find  $G \in \Omega_d$  with  $\mu_d = \varepsilon(G)$  and to compute  $\mu_d$  if  $d \geq 15$ .

### 81 Applied Mathematics

14 <u>Satoshi Murai</u> (Yamaguchi Univ.) On flag *f*-vectors of polyhedral complexes · · · · · · · · · 10 Kohji Yanagawa (Kansai Univ.)

Summary: In 1985, Bayer and Billera proved that the dimension of the vector space spanned by all flag f-vectors of d-dimensional polytopes is a Fibonacci number. We introduce an analogue of this result for polyhedral complexes.

 

 15
 Masahiro Hachimori (Univ. of Tsukuba)
 b
 Hereditary-shellability and vertex decomposability of simplicial complexes

 15
 Kenji Kashiwabara (Univ. of Tokyo)
 b
 Hereditary-shellability and vertex decomposability of simplicial complexes

Summary: We say a simplicial complex is hereditary-P if every restriction to a subset of the vertex set satisfies the property P. In this talk we discuss the relation between hereditary-shellability and vertex decomposability of simplicial complexes. The main result is to show the existence of 2- and higher dimensional simplicial complexes that are hereditary-shellable but not vertex decomposable. This especially shows that hereditary-shellability and hereditary-vertex decomposability are different for 2- and higher dimensions.

16 Masaya Tomie (Morioka Univ.) Poset structures for pattern avoiding set partitions ..... 10

Summary: In this talk we consider poset structures of the set partitions which avoid a pattern of length 3. Sagan introduced the concept of pattern avoiding set partitions and Goyt and Sagan developed their statistics. There are five patterns of length 3 and especially we focus on 12/3-avoiding set partitions. The number of maximal chains of the posets are enumerated by the Catalan numbers. The posets are lattices and self dual. Furthermore they are flag-symmetric posets. We also calculate the Mobius numbers of the intervals of the posets.

# 16:50–17:50 Talk invited by Applied Mathematics Section

Yoshio Okamoto Free edge lengths in plane graphs (Univ. of Electro-Comm.)

Summary: We study the impact of metric constraints on the realizability of planar graphs. Let G be a subgraph of a planar graph H (where H is the "host" of G). The graph G is *free* in H if for every choice of positive lengths for the edges of G, the host H has a planar straight-line embedding that realizes these lengths; and G is *extrinsically free* in H if all constraints on the edge lengths of G depend on G only, irrespective of additional edges of the host H.

We characterize all planar graphs G that are free in every host  $H, G \subseteq H$ , and all the planar graphs G that are extrinsically free in every host  $H, G \subseteq H$ . The case of cycles  $G = C_k$ , provides a new version of the celebrated carpenter's rule problem. Even though cycles  $C_k, k \geq 4$ , are not extrinsically free in some triangulations, every "nondegenerate" choice of edge lengths are relaizable, where the lengths are considered degenerate if the cycle can be flattened (in 1-dimensions) in two different ways.

Separating triangles, and separating cycles in general, play an important role in our arguments. We show that every star is free in a 4-connected triangulation (which has no separating triangle).

Joint work with Zachary Abel, Robert Connelly, Sarah Eisenstat, Radolav Fulek, Filip Morić, Tibor Szabó, and Csaba D. Tóth.

# March 16th (Sun) Conference Room IX

# 9:30 - 11:30

Summary: Zeta(3) is not known as elementary expression using elementary constants. we got the expression in Maple Soft environment. Namely, Zeta(3) is expressed by using Pi and ln(2) and fractional numbers. We report this maple Pg and It's Output list.

Summary: To detect scratches of sintered parts is achieved by human's sight, even if science and technology are developing in this day. We consider how to detect scratches of sintered parts by using adjusted residuals of  $\chi^2$  test.

<u>Yoshihiro Mizoguchi</u> (Kyushu Univ.)
 <u>Hisaharu Tanaka</u> (Saga Univ.)
 Issei Sakashita (Kyushu Univ.)
 Shuichi Inokuchi (Kyushu Univ.)

Summary: We implemented operations appeared in the theory of automata using the Coq proof-assistant. A language which contains infinite elements is defined using ssreflect (a Small Scale Reflection Extension for the Coq system). We also implemented the modules for sticker systems. Păun and Rozenberg introduced a concrete method to transform an automaton to a sticker system in 1998. One of our aims is to present formal proofs of the correctness of their transformation. We modified some of their definitions to improve their insufficient results. We note that all of our formulation are written in Coq and we show some examples of machine-checkable proofs.

Summary: The concept of primitive chaos was proposed in the field of physics [1]. In this talk, the emergence of two contrast spaces from the primitive chaos is shown from a topological viewpoint [2,3]. References [1] Y. Ogasawara: J. Phys. Soc. Jpn. 79 (2010) 15002. [2] Y. Ogasawara and S. Oishi: RIMS Kôkyûroku 1833 (2013) 98. [3] Y. Ogasawara and S. Oishi: J. Phys. Soc. Jpn., in print.

21	Guillaume Bacquela (Nihon Univ.)	Offensive alliances in trees	
	Yoshimi Egawa (Tokyo Univ. of Sci.)		
	Shigeki Imamura (Nihon Univ.)		
	Kenji Kimura (Tokyo Univ. of Sci.)		
	Akira Saito (Nihon Univ.)		

Summary: Let G = (V, E) be a graph having vertex set V and edge set E. We denote by N(v) the neighbourhood of a vertex v. For  $S \subset V$  we denote  $N(S) = \bigcup_{v \in S} N(v)$ . We define the boundary  $\partial S$  as the set N(S) - S. A non-empty set of vertices  $S \subset V$  is said to be an offensive alliance if for every vertex  $v \in \partial S$ ,  $|N(v) \cap S| > |N(v) \cap (V - S)|$ .

Favaron et al. [Offensive alliances in graphs, *Discuss. Math. Graph Theory* **24** (2004), no 2, 263–275] have proved that every graph of order  $n \ge 2$  has an offensive alliance of order at most 2n/3. For a path on nvertices, it has an offensive alliance of order at most  $\lfloor n/2 \rfloor$ . In this talk, we consider a tree other than a path. We prove that a tree of order n that is not a path has an offensive alliance of order at most 3n/8+9/8.

22 Yoshimi Egawa (Tokyo Univ. of Sci.) Spanning trees with vertices having large degrees ..... 15 <u>Kenta Ozeki</u> (Nat. Inst. of Information/JST ERATO)

Summary: Because of its relationship to problems on Hamiltonian cycles, a spanning tree with degree constraint is one of the most important and attractive topics in graph theory and computer science. The purpose of this talk is to study a necessary and "almost" sufficient condition for the existence of spanning trees satisfying lower bounds on degrees.

# 13:00 - 14:30

Summary: A box in Euclidean k-space is the Cartesian product I1 \*I2\*...\*Ik, where Ij is a closed interval on the real line. The boxicity of a graph G, denoted by box(G), is the minimum integer k such that G can be represented as the intersection graph of a family of boxes in Euclidean k-space. In this talk, for every positive integer k, we present how one constructs a new graph whose boxicity is more than k, where one starts with any graph. Our main result is that for a graph G with a focal vertex, the boxicity of the Mycielski graph M2(G) is more than that of G.

24	Valentin Borozan (Univ. Paris-Sud 11)	From edge-coloring to strong edge-coloring 10
	Gerard Jennhwa Chang	
	(National Taiwan Univ.)	
	Nathann Cohen (Univ. Paris-Sud 11)	
	Shinya Fujita (Yokohama City Univ.)	
	N. Narayanan	
	(Indian Institute of Tech.)	
	Reza Naserasr (Univ. Paris-Sud 11)	
	Petru Valicov (Univ. Paris-Sud 11)	

Summary: Some recent results on strong edge-coloring will be reviewed.

# 84 Applied Mathematics

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Summary: We study quasi-Monte Carlo (QMC) rules for numerical integration of high smooth integrands defined over the s-dimensional unit cube. As a dyadic n-digit discretized version of Dick's inequality for n-smooth integrands, Matsumoto, Saito, and Matoba have later introduced Walsh figure of merit (WAFOM) WAFOM(P) for an  $\mathbb{F}_2$ -digital net P that can be employed as a practically computable quality criterion of QMC point sets. The key ingredient for obtaining WAFOM is the Dick weight. We generalize the notion of the Dick weight and WAFOM for digital nets over a general finite abelian group and we give the MacWilliams identity of weight enumerator polynomials for the Dick weight, with which we can obtain a computable formula of WAFOM.

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Summary: Matsumoto, Saito, and Matoba recently proposed the Walsh figure of merit (WAFOM), which is a criterion of quasi-Monte Carlo point sets constructed by digital nets. WAFOM is quickly computable, so that it enables us to search for quasi-Monte Carlo point sets by random search. In this talk, we search for low-WAFOM point sets with small discrepancy. For this, we consider digital (t, m, s)-nets, and apply random linear scrambling with non-singular lower triangular matrices. Our approach is to select good point sets from scrambled digital (t, m, s)-nets in terms of WAFOM. By numerical experiments, we show that the obtained point sets improve the rates of convergence for smooth functions and are robust for non-smooth functions.

March 17th (Mon) Conference Room IX

# 9:00 - 12:00

Summary: We extend the Halley method. We give the formulas to compare the convergence of the Halley method and extended the Halley method (Tsuchikura–Horiguchi–Murase–Halley method) (in the case of an equation). We found the extended Halley method from Murase's recurrence formulas of the square x\*x in 1673.

# 29 Shunzi Horiguchi

(Niigata Sangyo Univ.)

Numerical calculations of the formulas to compare the convergence of Halley method and the extended Halley method (Tsuchikura–Horiguchi– Murase–Halley method) (in the case of an equation) · · · · · · · · · · 10

Summary: We extend the Halley method. We will give the numerical calculations of the formulas to compare the convergence of the Halley method and extended the Halley method (Tsuchikura–Horiguchi–Murase–Halley method) (in the case of an equation). We found the extended Halley method from Murase's recurrence formulas of the square x\*x in 1673.

Summary: The author teaches mathematics/statistics and chemistry at a medical technology school. Mathematics, especially statistics, and chemistry are not necessarily the favorite subjects of Japanese students receiving paramedical education. So, the author taught mathematics/statistics needed for medical technologist in regular classes. Moreover, the author taught remedial mathematics learned at elementary schools, junior high schools and high school in Science I. Additionally, the author conducted supplementary separate classes for students who had poor results of the proficiency test of admission immediately. As a result, in the final exam of mathematics/statistics, it can be all pass. So they had a positive impact to the national examination. The author would like to contribute to the Medical technologists training.

Summary: This article describes some dynamic aspects on dynastic utility incorporating two-sided altruism with an OLG setting. We analyzed the special case where the weights of two-sided altruism are dynamically inconsistent. The Bellman equation for two-sided altruism proves to be reduced to one-sided dynamic problem, but the effective discount factor is different only in the current generation. We show that a contraction mapping result of value function cannot be achieved in general, and that there can locally exist an infinite number of self-consistent policy functions with distinct steady states (indeterminacy of self-consistent policy functions).

Summary: In 1970's Dr. Schumacher appealed that the atomic power generation should be immediately abolished because of the various poinsonous influence due to radition. The purpose of this paper is to innovate a mathematical model of the economy of the atomic power generation in our society and to conduct Schumacher's appeal as a theorem.

## 86 Applied Mathematics

# 33 Shy Der Lin Caputo fractional derivative and its applications ...... 15 (Chung Yuan Christian Univ.)

Summary: Abstract The main objective of this talk is to present the Caputo type fractional derivatives and integrals in the theory of fractional mathematical analysis, and use the techniques of special intergal transform to get the solutions of fractional differential and integral equations in various fields. In the past two decades, the widely-investigated subject of fractional calculus has remarkably gained importance and popularity due to its demonstrated applications in numerous diverse fields of science and engineering, and the fields of special functions. In this talk is also to present in the fields of Caputo Laplace transform of the fractional derivative to solve the useful fractional-order differential equations in the fields of applied mathematics which allied topics of mathematical analysis and applicable mathematics with the theoretic and applicable aspects of the associated Riemann–Liouville fractional integrals and fractional derivatives.

34 Noriaki Umeda (Meiji Univ.) On non-well-definedness of the diffusive sign by the heat equation .... 15

Summary: We consider a solution of a simple Cauchy problem for a semilinear heat equation, and we consider a sign of the solution. The diffusive sign by the equation is defined by the limit of sign of the solution as time tend to zero. In this lecture we consider the case when the diffusive sign is not well-defined.

Summary: In predicting the financial market and pricing financial derivatives, the volatility, dividend rate, and covariance of the underlying financial assets are very important parameters. However, they can not be directly observed from the market data. One way of obtaining these parameters is to calculate, or in other words, to identify them from the option prices. This is called the inverse problem of option pricing. There are researches which had been working on identifying asset volatility and also researches on identifying dividend on the Sobolev space satisfying Lipschitz condition from option prices, and we will focus on how to identify dividend rate on the Sobolev space in this study.

36 Naoharu Ito (Nara Univ. of Edu.) A note on generalized Sylvester equations over Bezout domains ..... 15

Summary: This paper studies the consistency of the generalized Sylvester equation over Bezout domains. A result on rank minimization which extends Roth's equivalence theorem is given.

<u>Takamichi Sushida</u> (Ryukoku Univ.)
 <u>Akio Hizume</u> (Ryukoku Univ.)
 Yoshikazu Yamagishi (Ryukoku Univ.)

Voronoi spiral tilings	 	•••	 •••	•••	• •	 •••	•••	•••	• •	• •	•	•••	•	• •	 	1	5

Summary: We study the topology and geometry of the Voronoi tiling of the punctured plane  $\mathbb{C}^* := \mathbb{C} \setminus \{0\}$  with the spiral sequence  $S = \{\zeta^j\}_{j \in \mathbb{Z}}$  generated by a single element  $\zeta = r e^{i\theta}$ , 0 < r < 1. It is intimately related to the phyllotaxis theory. A Voronoi spiral tiling forms a hexgonal or quadrilateral tiling. In particular, the case of quadrilateral tilings is a special case of the Voronoi spiral tilings called degenerate. The set of the generators  $\zeta$  of quadrilateral tilings is a countable union of real algebraic curves parameterized by the divergence angle  $\theta$ . When  $\theta/2\pi$  is a fixed quadratic irrational, we consider the set of the plastochrone ratios r such that the generators  $\zeta$  give rise to quadrilateral tilings, then it is shown that the limit set of the shapes of the quadrilaterals, as  $r \to 1$ , is a finite set. In particular, if  $\theta/2\pi$  is linearly equivalent to the golden section  $\tau = \frac{1+\sqrt{5}}{2}$ , then the limit of the shapes of the quadrilaterals, as  $r \to 1$ , is a finite set.

# 14:30 - 16:30

38 Hideki Murakawa (Kyushu Univ.) Mathematical models of cell-cell adhesion: diffusion or advection · · · · 15

Summary: Cells adhere to each other through the binding of cell adhesion molecules at the cell surface. This process, known as cell-cell adhesion, is fundamental in many areas of biology, including early embryo development, tissue homeostasis and tumour growth. In this talk we consider mathematical models of this phenomenon.

Summary: In considering the morphogenesis of tissue of multicellular organisms, the orientation of the cell placement is very important. For example, in the inner ear of a person, a function [hear the sound] is produced by cells called hair cells arranged in a particular direction. This is a phenomenon caused by the individual cells have an asymmetry spatial pattern, behavior of such cells are called PCP (Planar cell polarity). Recently, in hair cells other than, PCP is a universal phenomenon seen in the various organisms and tissue. Hence many researchers study about PCP phenomena. In this session, we will introduce our mathematical model for PCP.

 40 <u>Tatsuki Mori</u> (Ryukoku Univ.) Kousuke Kuto
 40 <u>Tatsuki Mori</u> (Ryukoku Univ.)
 50 Kructure and stability of stationary solutions to a reaction-diffusion model for cell polarization
 51 Masaharu Nagayama (Hokkaido Univ.)
 52 Shoji Yotsutani (Ryukoku Univ.)

Summary: We are interested in the structure and stability of stationary solutions to a reaction-diffusion model for cell polarization by Y. Mori, A. Jilkine and L. Edelstein-Keshet in SIAM J. Appl. Math (2011). We have proposed a new method to represent the bifurcation sheets which determine the global bifurcation structure including all bifurcation branches. We investigate the stability of them numerically.

## 88 Applied Mathematics

41 <u>Masaji Watanabe</u> (Okayama Univ.) Mathematica Fusako Kawai (Kyoto Inst. Tech.) ization proce

Summary: A mathematical model for a microbial depolymerization process is described. Experimental results are introduced into analysis to solve inverse problems numerically for the molecular factor and the time factor of a degradation rate. An initial value problem is solved to simulate the microbial depolymerization process.

42 <u>Masaharu Nagayama</u> (Hokkaido Univ.) Ken Wakai (Kanazawa Univ.) Kei Nishi (Hokkaido Univ.) Yasuaki Kobayashi (Hokkaido Univ.) Yumihiko Ikura (Hokkaido Univ.) Satoshi Nakata (Hiroshima Univ.)

Mathematical analysis for the collective motion of camp hor disks  $\ \cdots \ 15$ 

Summary: We consider the collective motion of camphor disks in an annulus water channel. As an experimental result, when the radius of the water channel is small, two camphor disks move in opposite directions, while if the radius of one is large, the two camphor disks move in the same direction. Moreover, some camphor disks display a billiard phenomenon when put on the water channel. We will investigate the mechanism of these collective motions by means of numerical simulation, reduction methods and linearized stability analysis of the mathematical model for the camphor motion.

Summary: Unidirectional motion along an annular water channel can be observed in an experiment. Moreover, the collective motion of camphor boats in the water channel exhibits a homogeneous and an inhomogeneous state, depending on the number of boats. In a theoretical research, the unidirectional motion is represented by a traveling wave solution in a model. Hence it suffices to investigate a linearized eigenvalue problem in order to prove the destabilization of a traveling wave solution. However, the eigenvalue problem is too difficult to analyze even if the number of camphor boats is 2. Hence we need to make a reduction on the model. In this work, we reduce the model to an ordinary differential system by the center manifold theory.

# 16:45–17:45 Talk invited by Applied Mathematics Section

Karel Svadlenka (Kanazawa Univ.) On the method of semidiscretization in time for nonlinear evolutionary problems

Summary: When a semidiscretization in time is applied, initial boundary value problems for evolutionary partial differential equations with variational structure can be approximated by a sequence of stationary problems. The resulting stationary problems are usually of elliptic type and can be written as minimization problems. This fact often provides a great advantage when dealing with various types of nonlinearities in the original equation, both from the viewpoint of mathematical analysis and from the viewpoint of numerical solution.

In this talk, an outline of the semidiscretization method for parabolic and hyperbolic partial differential equations of second order will be presented, and its application to existence and regularity analysis and numerical simulation will be explained. Several examples will be shown, covering nonlinear problems such as evolutions with global constraints, evolutionary free boundary problems with contact angle condition, motion of elastic curves around obstacles and constrained multiphase mean curvature flow.

March 18th (Tue) Conference Room IX

# 10:00 - 11:30

44 Kiyohisa Tokunaga Approximate values of a triangular double integral · · · · · · · 15 (Fukuoka Inst. of Tech.)

Summary: The advantage of our triangular integral over the conventional rectangular integral is to have only one limit at infinity. An approximate value is uniquely determined because it has only one limit. Approximate values of a triangular double integral are shown in the table and in the graph. The calculation processes of limit at infinity in detal are shown in the appendix.

Summary: In this talk, we consider the dipole simulation method (DSM) applied to a boundary value problem for the Laplace operator in a two-dimensional Jordan region. We prove that if we use an interior mapping function of the region to determine the collocation points and the charge points, then DSM gives a solution which converges to the exact solution under a hypothesis that the boundary curve is real analytic. We also obtain an error estimate which says that if the boundary data is real analytic, then an exponential convergence occurs.

Summary: A linear finite volume scheme for a simplified Keller–Segel system of chemotaxis is considered. The conservation of positivity and total of mass of the scheme is proved. We then derive the error estimates. Numerical experiments are preformed to verify the theoretical results and the numerical blow-up of the solution of large mass is investigated.

- 90 Applied Mathematics

Summary: We introduce a method for computing interfacial motions governed by curvature dependent acceleration. Our method is a thresholding algorithm of the BMO-type which, instead of utilizing a diffusion process, thresholds evolution by the wave equation to obtain the desired interfacial dynamics. We also develop the numerical method and present the results of its application, including an investigation of the volume preserving motions.

48 Khoji Ohtsuka Shape optimization using GJ-integral · · · · · · · · · 15 (Hiroshima Kokusai Gakuin Univ.)

Summary: There is difficulty of shape optimization in mixed boundary value problems by the reason of the singularity at the intersection between different boundary conditions. Using GJ-integral, we can get the optimal shape in such cases.

 

 49 Yoshihiro Saito (Gifu Shotoku Gakuen Univ.)
 Improved Heun method for systems of stochastic differential equations

 10

Summary: The stochastic Heun method is an explicit method for stochastic differential equations. It is known that the Heun method cannot attain strong order 1, except for special case. In this talk we propose an strong first order scheme which add a correction term to the Heun method.

# 14:15-15:45

50Takaharu Yaguchi (Kobe Univ.)On well-posedness of the weak form of the finite element exterior cal-<br/>culus on manifolds with boundaries50Takuya Tsuchiya (Ehime Univ.)Con well-posedness of the weak form of the finite element exterior cal-<br/>culus on manifolds with boundaries

Summary: The finite element exterior calculus (FEEC) is a unified approach to deriving finite element schemes for a class of elliptic partial differential equations by using geometric tools, such as the Hodge decomposition and the Poincaré inequality. In order to extend this framework to the PDEs on manifolds with boundaries, in this talk, we introduce a weak form of the PDEs that is same as the weak form of FEEC, and investigate its well-posedness.

51	Yoshitaka Watanabe (Kyushu Univ.)	An improvement of invertibility verifications for linear elliptic operators
	<u>Takehiko Kinoshita</u> (Kyoto Univ.)	
	Mitsuhiro T. Nakao	
	(Sasebo Nat. Coll. of Tech.)	

Summary: The aim of this lecture is to propose a procedure to verify the invertibility of linear elliptic partial differential operators with computable upper bound. We have already proposed a numerical method to verify the invertibility and to bound which is based on a projection and its constructive a priori error estimates. We will give an improvement of our previous method with numerical examples.

52 Yoshiki Sugitani (Univ. of Tokyo) Guanyu Zhou (Univ. of Tokyo) Norikazu Saito (Univ. of Tokyo) Summary: As an open boundary condition (a kind of artificial boundary conditions) for viscous incompressible fluids flow simulation, we propose a unilateral boundary condition. With our boundary condition, the Navier–Stokes equation satisfies an energy inequality so that we can avoid numerical instability in 3D simulations. In this paper, we consider a model Stokes problem and establish the well-posedness by using a variational inequality. The treatment of a pressure part is of particular interest. We also study the penalty method as a practical numerical method.

Summary: As is well-known, solutions of some nonlinear PDEs blow up in finite time. From the viewpoint of numerical analysis, calculating the maximal existence time is of particular interest. So, there are many researches about methods of calculating maximal existence time numerically. In particular, there are many such researches for nonlinear parabolic equations. Recently, Cho proposed an explicit finite difference scheme that can approximate the maximal existence time for a nonlinear wave equation. However, the convergence of Cho's scheme, which is a crucial part of the theory, is open at present. In this paper, we propose a linear implicit scheme for nonlinear wave equations. We show that our scheme can be proven to be convergent and can calculate the numerical maximal existence time.

54Shinya Uchiumi (Waseda Univ.)Behavior of characteristics finite element solutions for small time incre-<br/>mentsMasahisa Tabata (Waseda Univ.)ments15

Summary: We study behavior of solutions of two characteristics finite element schemes for small time increments. Our recently developed scheme free from numerical quadrature is always stable for any time increment. The conventional scheme using numerical quadrature is unstable for time increments of medium size, but it is proved to recover the stability for sufficiently small time increments for each fixed element size h.

# 16:00–17:00 Talk invited by Applied Mathematics Section

Yoshitaka Watanabe (Kyushu Univ.) Computer-assisted stability and instability proofs for the Orr–Sommerfeld probmem

Summary: The Orr–Sommerfeld equation is one of the central equations governing the linearized stability theory of incompressible flows. The Orr–Sommerfeld equation is a non-selfadjoint eigenvalue problem for the eigenpair, and within the frame of linearized stability theory, the flow is stable if the spectrum is located in the right complex half-plane, otherwise unstable.

In this talk, we focus on the case of plane Poiseuille flow and propose a numerical verification method for computing eigenpair enclosures and eigenvalue exclosures for the Orr-Sommerfeld problem. Some verification results confirm the effectiveness of the method. We also note that our principle can be applied to other nonlinear problems including partial differential operators.

# Topology

March 15th (Sat)

Conference Room IV

# 10:00 - 12:00

- 2 <u>Makoto Ozawa</u> (Komazawa Univ.) Dehn surgery and Seifert surface system · · · · · · · · · · 10 Koya Shimokawa (Saitama Univ.)

Summary: For a compact connected 3-submanifold with connected boundary in the 3-sphere, we relate the existence of a Seifert surface system with a Dehn surgery along a null-homologous link. As its corollary, we obtain the Fox's re-embedding theorem.

 <u>Kazuhiro Ichihara</u> (Nihon Univ.) Strong cylindricality and the monodromy of bundles ..... 10 Tsuyoshi Kobayashi (Nara Women's Univ.)
 Yo'av Rieck (Univ. of Arkansas)

Summary: A surface F in a 3-manifold M is called cylindrical if M cut open along F admits an essential annulus A. If, in addition,  $(A, \partial A)$  is embedded in (M, F), then we say that F is strongly cylindrical. Let M be a connected 3-manifold that admits a triangulation using t tetrahedra and F a two-sided connected essential closed surface of genus g(F). We show that if g(F) is at least 38t, then F is strongly cylindrical. As a corollary, it is shown that a closed hyperbolic manifold admits only finitely many fibrations over the circle with connected fiber whose translation distance is not one. Similar results were obtained by Saul Schleimer.

Summary: For a given cusped 3-manifold M admitting an ideal triangulation, we describe a method to rigorously prove that either M or a filling of M admits a complete hyperbolic structure via verified computer calculations. Central to our method are an implementation of interval arithmetic and Krawczyk's Test. These techniques represent an improvement over existing algorithms as they are faster while accounting for error accumulation in a more direct and user friendly way.

# 93 Topology

Summary: By the work of Epstein–Penner and Weeks, every finite-volume cusped hyperbolic manifold is decomposed in a canonical way into ideal polyhedra, called the canonical decomposition. Jørgensen showed that the canonical decompositions of once-punctured torus bundles over  $S^1$  are "layered" triangulations. In this talk, we prove that the canonical decompositions of hyperbolic fibered two-bridge link complements are "layered" triangulations. To prove this result, we use A'Campo's criterion for detecting fiberedness.

Summary: Jorgensen gave a complete description of the combinatorial structure of the Ford domains of quasi-fuchsian once-punctured torus groups. In this talk, we give a construction of the Ford domains of fuchsian once-punctured Klein bottle groups by using Jorgensen's method. We also show that there are quasi-fuchsian once-punctured Klein bottle groups whose Ford domains have quite different nature compared with these of quasi-fuchsian once-punctured torus groups.

7 Eiji Ogasa (Meiji Gakuin Univ.)\* New developments of local move identities of knot polynomials ..... 10

Summary: It is well-known the Alexander polynomial A(K) of 1-links K satisfies the identity  $A(K_+) - A(K_-) = (t-1) \cdot A(K_0)$  associated with a kind of local moves of knots. (The Jones polynomial of 1-links satisfies a similar one.)

We found that the *l*-Alexander polynomial  $\Delta_l(K)$  of *n*-knots K satisfies some identities associated with some kinds of local moves. The identities are as follows

 $\begin{aligned} \Delta_l(K_+) - \Delta_l(K_-) &= (t-1) \cdot \Delta_l + 1(K_0) \\ \Delta_l(K_+) - \Delta_l(K_-) &= (t+1) \cdot \Delta_{l+1}(K_0) \text{ These forms depend on } l \text{ and kinds of local moves.} \\ \operatorname{Arf} K_+ - \operatorname{Arf} K_- &= \{ |bP_{4k+2} \cap I(K_0)| + 1 \} \text{mod}2, \text{ where } I() \text{ is the inertia group and } bP() \text{ the } bP \text{-subgroup.} \end{aligned}$ 

8 <u>Taizo Kanenobu</u> (Osaka City Univ.) Evaluations of Gordian distances of knots by polynomial invariants · · · 10 Hiromasa Moriuchi (Kinki Univ.)

Summary: The Gordian distance of two knots is the minimum number of crossing changes needed to transform one into the other. We introduce several criterion using the Jones and HOMFLYPT polynomials. Then making use of them, we improve the table of the Gordian distances between knots with up to seven crossings given by Darcy. 9

Sumiko Horiuchi (Tokyo Woman's Christian Univ.) Yoshiyuki Ohyama (Tokyo Woman's Christian Univ.)

A lattice of virtual knots by crossing changes ..... 15 Jniv.)

Summary: If two virtual knots  $K_1$  and  $K_2$  are transformed into each other by a finite sequence of crossing changes,  $d_G(K_1, K_2)$  denotes the minimal number of times of crossing changes needed to transform  $K_1$  into  $K_2$ . A *n* dimensional lattice of virtual knots by crossing changes is the *n* dimensional lattice graph which satisfies the following: The vertex set consists of oriented virtual knots and for any two vertices  $K_1$  and  $K_2$ , the distance on the graph from  $K_1$  to  $K_2$  coincides with  $d_G(K_1, K_2)$ , where the distance on the graph means the number of edges of the shortest path which connects the two virtual knots. In this talk, we show that for any given natural number N and any given virtual knot K, there exists a N dimensional lattice of virtual knots by crossing changes with the vertex K.

# 14:15-16:30

Summary: Any knot  $K \subset S^3$  bounds a clasp disk that is an immersed disk whose singularity set consists of only clasp singularity. Then we can define a knot invariant c(K) called the clasp number. In 1974, T. Shibuya proved that the genus and the unknotting number are lower bounds of the clasp number, that is,  $\max\{g(K), u(K)\} \leq c(K)$ . In this talk, we introduce a characterization of the Alexander module via the clasp disk introduced by K. Morimoto. Moreover, we show that  $\max\{g(10_{97}), u(10_{97})\} < c(10_{97})$ .

# 11 Hideo Takioka (Osaka City Univ.) The cable Γ-polynomials of mutant knots ······ 10

Summary: The  $\Gamma$ -polynomial is an invariant of an oriented link, which is the common zeroth coefficient polynomial of the HOMFLYPT and Kauffman polynomials. It is known that the HOMFLYPT and Kauffman polynomials, their 2-cable versions, and the satellite versions of the Alexander and Jones polynomials are invariant under mutation. Moreover, it is also known that the 3-cable version of the HOMFLYPT polynomial distinguishes a mutant knot pair. In this talk, we show that the 3-cable version of the  $\Gamma$ -polynomial is invariant under mutation.

# 12 Takuji Nakamura

On the number of colors in effective Fox 9-colorings for knots ..... 10

(Osaka Electro-Comm. Univ.) Yasutaka Nakanishi (Kobe Univ.) Shin Satoh (Kobe Univ.)

Summary: For a composite n, we define an effective n-coloring of knots and give a lower bound  $\log_2 n + 1$  for the minimal number of colors for all effective n-colorings. In particular, we prove that any effectively 9-colorable knot is represented by a diagram where exactly five colors of nine are assigned to the arcs.

# 95 Topology

13 Migiwa Sakurai A polynomial invariant and the forbidden move of virtual knots · · · · · 10 (Tokyo Woman's Christian Univ.)

Summary: Satoh and Taniguchi introduced a numerical invariant called an n-writhe and we can define a polynomial invariant by using the n-writhes. In this talk, we provides the difference of the values obtained from the polynomials between two virtual knots which can be transformed into each other by a single forbidden move. As a result, we make it possible for many virtual knots to determine the unknotting numbers by forbidden moves.

- 14 Keiji Tagami (Tokyo Tech) A categorification of the Miyazawa polynomial ······ 10 Summary: In this talk, we construct a link homology for each stable equivalence class, that is, virtual link by using Bar-Natan's geometric complex and a homotopy quantum field theory (HQFT for short). In particular, if we take a certain HQFT, it is isomorphic to Dye–Kauffman–Manturov's categorification of the Miyazawa polynomial.

Summary: Ishii and Masuoka introduced the braided monoidal category  $\mathcal{T}$  of handlebody tangles. According to their results, a commutative Frobenius algebra in a braided monoidal category  $\mathcal{B}$  yields a  $\mathcal{B}$ -valued handlebody-TQFT, *i.e.*, a braided monoidal functor from  $\mathcal{T}$  to  $\mathcal{B}$ . In this talk, we give a new construction of commutative Frobenius algebras in braided finite tensor categories, which largely extends a construction due to Ishii and Masuoka. As an application, we propose the Dijkgraaf–Witten theory for handlebody-links by using the twisted Drinfeld double quasi-Hopf algebras.

Summary: We consider Reidemeister move 1, 2 on  $S^2$  and obtain necessary and sufficient condition for two knot projections to transform into each other by these moves.

 <u>Yusuke Takimura</u> (Waseda Univ.)<sup>b</sup> Strong and weak (1, 3) homotopies on knot projections ..... 15 Noboru Ito (Waseda Univ.)
 Kouki Taniyama (Waseda Univ.)

Summary: We consider Reidemeister moves 1, strong 3, weak 3 for knot projections on  $S^2$ . We define equivalence relations that are called weak (1, 3) and strong (1, 3) homotopies. For each equivalence relation, we determine which knot projections are trivialized. We also treat general cases and introduce invariants to classify knot projections.

18 Takefumi Nosaka (Kyushu Univ.)Longitudes in  $SL_2$ -representations of link groups and Milnor-Witt  $K_2$ -<br/>groups of fields15

Summary: We introduce an arithmetic  $K_2$ -value appearing in longitudes of a link via a  $SL_2$ -representation of the link group. Furthermore we prove the non-triviality, and compute the values for some link groups. In application, we give relatively simple computations of parabolic representations and a state sum formula of their cusp shapes.

# 17:00–18:00 Talk invited by Topology Section

Takefumi Nosaka (Kyushu Univ.) Low dimensional topological invariants of bilinear forms from quandle theory

Summary: We introduce some low dimensional topological invariants of bilinear forms. The construction for the invariants is based on quandle which is a certain algebraic system, and we define the invariants as "quandle cocycle invariants" of bilinear forms. So the construction is applicable to several low dimensional topological objects: 3-dimensional knots, knotted surfaces, handlebody links in  $S^3$ , surface braids. Furthermore, in knot case, we show that the invariants are, roughly speaking, bilinear forms on twisted Alexander "dual" modules; we hope that it is an interesting problem to analyse topological interpretations of the bilinear forms and to develop their applications.

As an application, we introduce bilinear-invariants of Hurwitz equivalence classes with respect to any group G. The invariants are constructed from any right G-modules M and any G-invariant bilinear functions on M. For instance, when G is the mapping class group of a closed surface,  $M_g$ , we get an invariant of Lefschetz fibrations over the 2-sphere. Moreover, the construction can be applied to the quantum representations of level k derived from the Chern–Simons quantum field theory. In particular, concerning the U(1)- or SU(2)-gauge groups, by the help of computers, we can compute many invariants in low fiber-genus case and we find new pairs of non-isomorphic Lefschetz fibrations. Furthermore we see that the invariant does not admit an additivity with respect to fiber sums.

In this talk, we explain the construction for the invariant of bilinear form, and demonstrate our idea to define the invariants of Hurwitz equivalence classes. Furthermore we present some computations.

March 16th (Sun) Conference Room IV

# 9:30 - 11:45

19	<u>Shin Kiriki</u>	(Tokai Univ.)	Blenders in center unstable Hénon-like families: with an application to
	Lorenzo J. Díaz	(PUC-Rio)	heterodimensional bifurcations · · · · · · · · · · · · · · · · · · ·
	Katsutoshi Shinohar	a (JST FIRST)	

Summary: We give an explicit family of polynomial maps called center unstable Hénon-like maps and prove that they exhibits *blenders* for some parameter values, which only appear in dimension greater than or equal to 3 and are special type of hyperbolic sets of diffeomorphisms. Using this family, we also prove the occurrence of blenders near certain *non-transverse heterodimensional cycles* under high regularity assumptions. The proof involves a *renormalization scheme* along heteroclinic orbits. We also investigate the connection between the blender and the original heterodimensional cycle.

20 Kentaro Saji (Kobe Univ.)\* Isotopy of Morin singularities ..... 10

Summary: In this talk, I introduce an equivalence relation called A-isotopy between finitely determined map-germs, which is a strengthened version of A-equivalence. I consider the number of A-isotopy classes of equidimensional Morin singularities.

21 <u>Tetsuya Itoh</u> (Kyoto Univ.) Overtwisted disc in planar open books · · · · · · · · · 10 Keiko Kawamuro (Univ. Iowa)

Summary: Using open book foliation machinery, we show that an overtwisted disc in planar open books can be put in a topologically nice position. As a corollary, we show that a planar open book whose fractional Dehn twist coefficients along any boundary components grater than one supports a tight contact structure.

22 Takahiro Oba (Tokyo Tech) Stein fillings of homology spheres with planar open books ..... 10

Summary: It is well-known that the complex structure on a compact Stein surface induces a contact structure on the boundary and there is one to one correspondence between the set of contact structures on a given 3-manifold and the set of open books of the same manifold. In this talk, considering Lefschetz fibrations over  $D^2$  obtained from compact Stein surfaces and supporting open books of these boundaries, I will present a necessary and sufficient condition for the boundary of a compact Stein surface to be an integral homology 3-sphere.

Summary: For a given collection of simple closed curves in a bounded surface that contains certain six curves, after stabilizing these curves and the surface, and adding auxiliary curves to the collection, we construct infinitely many pairwise exotic positive allowable Lefschetz fibrations (PALFs) so that the resulting curves are vanishing cycles of one of the PALFs. As a corollary, we show that topological invariants (fundamental groups, homology groups, boundary homology groups, and intersection forms) of many 4-dimensional compact oriented 2-handlebodies are realized as those of infinitely many pairwise exotic Stein fillings.

24 Takuya Ukida (Tokyo Tech) PALF structure on Akbulut–Yasui plugs and plug twist ..... 10

Summary: Loi and Piergallini proved that every compact Stein surface admits a PALF (positive allowable Lefschetz fibration) over a 2-disk. Akbulut and Yasui introduced cork twist and plug twist to construct various families of arbitrary many compact Stein surfaces which are mutually homeomorphic but not diffeomorphic. In this talk, we construct an explicit PALF of genus 1 on every Akbulut–Yasui plug and describe monodromies of PALF's on two Stein surfaces related by a plug twist.

Summary: It follows from results of Gompf and Donaldson that every finitely presented group is the fundamental group of the total space of a Lefschetz fibration with a (-1)-section. In our work, we constructed Lefschetz fibrations with a (-1)-section whose fundamental groups are a given finitely presented group, by providing genus and monodromy explicitly.

Summary: Given a real, smooth, closed 4-manifold M, a primitive problem is to ask whether the number of deformation equivalence classes of surfaces homotopy equivalent to M is finite. Friedman and Morgan have proven that if  $b_1(M) \neq 1$ , then the number of deformation equivalence classes of surfaces homotopy equivalent to M is finite except in the case when M is homotopy equivalent to a elliptic surface whose fundamental group is finite cyclic. The problem remains open for manifolds with  $b_1 = 1$ . In this talk, we will like to prove that if M satisfies  $b_1(M) = 1$  and  $b_2(M) = 0$ , the number is finite.

Summary: By using a canonical metric on the space of symplectic invariants, we give a detailed structure of the symplectic invariant part of the symplectic derivation Lie algebra of a free Lie algebra.

# 13:30–14:30 Talk invited by Topology Section

Taro Yoshino (Univ. of Tokyo)<sup>b</sup> On topological blowups

March 17th (Mon) Conference Room IV

## 10:00 - 12:00

Summary: Let X be an infinite, locally connected, compact metrizable space and Y be a dendrite with an end point v. For each continuous map  $f: X \to Y$ , we define the hypograph  $\downarrow f = \bigcup_{x \in X} \{x\} \times [v, f(x)]$ , where [v, f(x)] is the unique arc from v to f(x) in Y. Then we can regard  $\downarrow C(X, Y) = \{\downarrow f \mid f : X \to Y \text{ is a continuous map}\}$  as the subspace of the hyperspace  $Cld(X \times Y)$  of non-empty closed sets in  $X \times Y$  endowed with the Vietoris topology. Let  $\overline{\downarrow C(X,Y)}$  be the closure of  $\downarrow C(X,Y)$  in  $Cld(X \times Y)$ . In this talk, we show that the pair  $(\overline{\downarrow C(X,Y)}, \downarrow C(X,Y))$  is homeomorphic to  $(\mathbf{Q}, \mathbf{c_0})$ , where  $\mathbf{Q} = [0,1]^{\mathbb{N}}$  is the Hilbert cube and  $\mathbf{c_0} = \{(x_i)_{i \in \mathbb{N}} \in \mathbf{Q} \mid \lim_{i \to \infty} x_i = 0\}$ .

Summary: James calculated vecat $(k\gamma_{\mathbb{R}})$ , the L-S category of  $k\gamma_{\mathbb{R}}$ , for  $k = 2^t$  and  $\gamma_{\mathbb{R}}$ , the canonical line bundle over the  $(2^t - 1)$ -dimensional real projective space. In this work, we calculated vecat $(k\gamma_{\mathbb{R}})$  for integers kand  $\gamma_{\mathbb{R}}$ , the canonical line bundle over real projective spaces. We also calculated vecat $_{\mathbb{F}}\xi$ , the L-S category of  $\xi$  as an  $\mathbb{F}$ -vector bundle, where  $\mathbb{F} = \mathbb{R}$  or  $\mathbb{C}$ , for  $\xi$ , multiple Whitney sums of canonical line bundles over complex and quaternion projective spaces. 30Tadayuki HaraguchiAbout introduction and geralization of a model structure on the cate-<br/>gory of numerically generated spaces30Tadayuki Haraguchi(Internat. Pacific Univ.)gory of numerically generated spaces

Summary: Let  $\mathbf{C}$  be a coreflective subcategory of a cofibrantly generated model category  $\mathbf{D}$ . In this talk we introduce that under suitable conditions  $\mathbf{C}$  admits a cofibrantly generated model structure which is left Quillen adjunction to the model structure on  $\mathbf{D}$ . As an application, we give that the category of numerically generated spaces admit a cofibrantly generated model structure which is Quillen equivalent to the standard model structure on the category **Top** of topological spaces.

31 <u>Yasuhiro Momose</u> (Shinshu Univ.) On quasi-schemoids and the Baues–Wirsching cohomology ..... 15 Yasuhide Numata (Shinshu Univ.)

Summary: A quasi-schemoid is a generalization of an association scheme, and a schemoid algebra is an analogue of the Bose–Mesner algebra for an association scheme. Our aim is to study quasi-schemoids and schemoid algebras via cohomologies. We describe the Baues–Wirsching cohomology of some poset, and apply the description to some example of schemoids.

Summary: I talk about semi-direct product of little *n*-cubes spaces. This is inspired by a result of P. Salvatore which states existence of some twist on operadic structures on the space of long knots and their variants.

33 Syunji Moriya (Kyoto Univ.) Homology of long knots and multiplicative formality ..... 15

Summary: I talk about homology of spaces of long knots and multiplicative formality of little n-cubes operads

Summary: We determine the 2-primary components in 32-stem unstable homotopy groups of spheres  $\pi_{n+32}^n$  for  $n \geq 9$ . This work begins with Toda: Composition methods in the homotopy groups of spheres, Ann. of Math. Studies, 49(1962) and was relayed by Mimura, Mori and Oda. Oda: Unstable homotopy groups of spheres, Inst. Adv. Res. Fukuoka Univ. 44(1979) determined  $\pi_{n+32}^n$  for  $2 \leq n \leq 8$ .

# 14:15-15:15

Summary: We study complex contact similarity geometry (G, X) consisting of a complex nilpotent Lie group X with invariant complex contact structure and G is a transitive group of similarity transformations. A manifold locally modelled on (G, X) is said to be a complex contact similarity manifold. Among them, there exist an infranilmanifold and an infra-Hopf manifold. We give a classification theorem on complex contact similarity manifolds. Our examples are different from those known previously as the complex Boothby–Wang fibration or the twistor fibration.

Summary: A vector in  $\mathbb{Z}^2$  is called primitive if its components are relatively prime. We give a formula on the rotation number of a sequence of primitive vectors around the origin.

37 Yusuke Suyama (Osaka City Univ.) Examples of toric manifolds which are not quasitoric manifolds ..... 10

Summary: It is known that if a toric manifold is projective or has complex dimension  $n \leq 3$ , then it is a quasitoric manifold. We show that there are infinitily many toric manifolds which are not quasitoric manifolds for any complex dimension  $n \geq 4$ .

38 Miho Hatanaka (Osaka City Univ.) Gluing construction of topological toric manifolds ..... 15

Summary: A topological toric manifold is a smooth manifold of even dimension with effective smooth action of a complex torus, having an open dense orbit, and locally equivariantly diffeomorphic to a smooth representation space of the complex torus. The notion of topological toric manifolds was introduced by Ishida–Fukukawa–Masuda as a topological analogue of toric manifolds. They construct topological toric manifolds by generalizing the quotient construction in toric geometry. In this talk, I am going to construct topological toric manifolds by generalizing the gluing construction in toric geometry.

# 15:45–16:45 Talk invited by Topology Section

Megumi Harada (McMaster Univ.)\* Okounkov bodies and toric degenerations

# Infinite Analysis

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March 17th (Mon)
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Conference Room VIII

# 10:00-11:30

1 Diogo Kendy Matsumoto Idempotent Yang–Baxter Maps · · · · · · · · · · · · · · · · · 10 (Waseda Univ.)

Summary: In this talk, we introduce a way to construct idempotent Yang–Baxter maps by using an algebraic system that contain the distributive lattice as a special case.

2 Tetsuya Itoh (Kyoto Univ.) Generic quantum braid representations and Garside theory ..... 15

Summary: We show that generic quantum representations of the braid groups nicely reflect the dual Garside structure of braid groups, a combinatorial structure of braids producing a nice normal form. In particular, we show that generic quantum representations are faithful.

 $\begin{array}{ccc} 3 & \underline{\text{Takuya Matsumoto}}\left(\text{Utrecht Univ.}\right) & \text{The Drinfeld realization of the Yangian algebra associated with the} \\ & \underline{\text{Alexander Molev}}\left(\text{Univ. of Sydney}\right) & \text{centrally extended } \text{sl}(2|2) \text{ Lie superalgebra } \cdots \cdots \cdots \cdots \cdots \cdots \cdots 15 \end{array}$ 

Summary: The Lie superalgebra sl(2|2) is known as the only superalgebra which allows two dimensional central extensions. This algebra and the associated Yangian symmetries appear in the important integrable models such as one-dimensional Hubbard model and the AdS/CFT spin-chian model. In this talk, we propose the Drinfeld second realization based on the Levendorskii's realization, which allows us to introduce the coproduct structure of the Yangian. We also have classified the finite dimensional irreducible representations of the centrally extended superalgebra sl(2|2) by using technique of the Michelsson-Zhelobenko algebra, where we have found that atypical modules which is longer than that of sl(2|2) but shorter than the typical modules of sl(2|2).

4 <u>Hiroyuki Yamane</u> (Univ. of Toyama)\* Irreducible representations of generalized quantized algebras ..... 15 Saeid Azam (Univ. of Isfahan) Malihe Yousofzadeh (Univ. of Isfahan)

Summary: We give a list of the finite dimensional (graded) irreducible representations of generalized quantized algebras.

5 Yoshihiro Takeyama A discrete analogue of periodic delta Bose gas and affine Hecke algebra (Univ. of Tsukuba) 15

Summary: We consider an eigenvalue problem for a discrete analogue of the Hamiltonian of the non-ideal Bose gas with delta-potentials on a circle. It is a two-parameter deformation of the discrete Hamiltonian for joint moments of the partition function of the O'Connell–Yor semi-discrete polymer. We construct the propagation operator by using integral-reflection operators, which give a representation of the affine Hecke algebra. We also construct eigenfunctions by means of the Bethe ansatz method. In the case where one parameter of our Hamiltonian is equal to zero, the eigenfunctions are given by specializations of the Hall–Littlewood polynomials.

# 14:15-15:00

6 Tatsuya Hayashi

Non-symmetric commuting differential operators ..... 15 (Aoyama Gakuin Univ.)

Summary: The Calogero–Moser–Sutherland (CMS) models are well known as completely integrable quantum models. For these models, the operators of such models are invariant under the action of some Weyl groups. On the other hand, it is known that there exist deformations of the CMS models which are not invariant under the action of Weyl groups. In this research, we investigate deformations of the CMS models associated with the root system of B2 type. In this case, if certain coupling constants are one or two, then it is known that there exist non-symmetric deformations of CMS models. When some of coupling constants are set three, we construct a completely integrable differential operator.

Kanehisa Takasaki (Kyoto Univ.) Generalized Ablowitz–Ladik hierarchy in topological string theory  $\cdots 20$ 7

Summary: Last year, I reported that a modified melting crystal model gives a solution of the Ablowtiz–Ladik hierarchy. This talk presents a generalization of last year's result to topological string theory on the so called generalized conifolds. Amplitude functions of this model are related to a special tau function of the 2D Toda hierarchy. The associated factorization problem for the dressing operators  $W, \overline{W}$  can be solved explicitly at the initial time  $t = \bar{t} = 0$ . One can thereby find a precise form of the initial values of the Lax operators  $L, \bar{L}$ . The structure of the initial values shows that this model gives a solution of a generalization of the Ablowitz–Ladik hierarchy.

#### Talk invited by Infinite Analysis Special Session 15:15-16:15

Todor Eliseev Milanov (Univ. of Tokyo) Hirota bilinear equations in singularity theory

Summary: Motivated by Gromov-Witten theory, Dubrovin and Zhang have introduced a new class of integrable systems parameterized by semi-simple Frobenius manifolds. The hierarchies admit the notion of tau-functions and the problem that I would like to address in my lecture is whether the tau-functions can be characterized by Hirota bilinear equations (HBE). I am working in the settings of singularity theory where K. Saito's theory of primitive forms can be used to construct a large class of semi-simple Frobenius manifolds. My goal is to give an overview of a general construction, which reduces the problem of constructing the HBE to finding a certain global residue formula. I would like also to describe several cases in which an appropriate global residue formula exists. The main difficulty is hidden in the monodromy representation on the vanishing cohomology and in the generalized root system corresponding to the set of vanishing cycles. Only for very few classes of singularities, such as simple singularities, the above objects are well understood, which in particular allowed us to find a global residue formula. In general, however very little is known and this is probably one of the main motivations to pursue this project. Namely, we would like to understand the role of vanishing cycles, the corresponding period integrals, and the monodromy representation in the Dubrovin–Zhang's integrable system.
## March 18th (Tue) Conference Room VIII

## 10:00 - 11:30

8 <u>Kohei Motegi</u> Integrable models and Grothendieck polynomials · · · · · · · · 15 (Okayama Inst. for Quant. Phy.) Kazumitsu Sakai (Univ. of Tokyo)

Summary: We investigate the algebraic structures of a class of quantum integrable models including many particle stochastic processes such as the totally asymmetric simple exclusion process and the totally zero range process. We find that the wavefunctions of the models are equivalent to the Grothendieck polynomials, which are polynomial representatives of Schubert classes in the Grothendieck ring of the Grassmann variety. As applications of this equivalence, we derive a Cauchy formula and orthogonality of the Grothendieck polynomials by using the techniques of quantum integrable models.

Summary: Using analysis on symmetric cones, we introduce some new multivariate orthogonal polynomials which are 2-parameter deformations of the spherical polynomials. These are also regarded as a multivariate analogue of the circular Jacobi polynomials. Furthermore, these weight function coincides with the circular Jacobi ensemble defined by P. Bourgade, et. al [IMRN. 23, (2009)].

10 Takeshi Morita (Osaka Univ.) A connection formula of a divergent basic hypergeometric function  $_{3}\varphi_{0}(a_{1}, a_{2}, a_{3}; -; q, x) \cdots 15$ 

Summary: We show a new connection formula of a divergent basic hypergeometric function  ${}_{3}\varphi_{0}(a_{1}, a_{2}, a_{3}; -; q, x)$ . In the study of connection problems on linear q-difference equations, the q-Borel–Laplace resummation methods are powerful tools. We introduce the extended q-Borel–Laplace transformations to obtain the connection formula.

 11
 Atsuo Kuniba (Univ. of Tokyo)
 Tetrahedron equation and quantum R matrices for q-oscillator repre 

 Masato Okado (Osaka City Univ.)
 sentations
 15

Summary: The intertwiner of the quantized coordinate ring  $A_q(sl_3)$  is known to yield a solution to the tetrahedron equation. By evaluating their *n*-fold composition with special boundary vectors we generate series of solutions to the Yang–Baxter equation. Finding their origin in conventional quantum group theory is a clue to the link between two and three dimensional integrable systems. We identify them with the quantum R matrices associated with the q-oscillator representations of  $U_q(A_{2n}^{(2)}), U_q(C_n^{(1)})$  and  $U_q(D_{n+1}^{(2)})$ .

Summary: It is a big problem to distinguish between integrable and non-integrable Hamiltonian systems. We provide a new approach to prove the non-integrability of homogeneous Hamiltonian systems with two degrees of freedom. The homogeneous degree can be chosen from real values (not necessarily integer). The proof is based on the blowing-up theory which McGehee established in the collinear three-body problem. We also compare our result with Molares–Ramis theory which is the strongest theory in this field.

## 14:15–15:15 Talk invited by Infinite Analysis Special Session

Takao Suzuki (Kinki Univ.) Higher order Painlevé system, rigid system and hypergeometric function

Summary: Recently, higher order generalizations of  $P_{\rm VI}$  has been studied from two viewpoints, similarity reductions of infinite dimensional integrable hierarchies and monodromy preserving deformations of Fuchsian systems. In this talk, we discuss their particular solutions in terms of the hypergeometric functions defined by rigid systems. Among those hypergeometric functions, we can find the classical ones; e.g. Thomae's  $_{n+1}F_n$ , Appell's  $F_1, F_2, F_3, F_4$  and Simpson's even-odd family.